

$$C_{12}(p)f=\partial_{\lambda}f(\lambda p,(1-\lambda)p,p_3,\dots,p_N)=0$$