

A deep field image of the universe, showing a vast field of galaxies and stars. The galaxies are of various shapes and sizes, some appearing as bright, elongated structures, while others are smaller and more distant. The stars are scattered throughout the field, with some appearing as bright, multi-colored points of light. The overall scene is a rich, multi-colored tapestry of cosmic objects.

Overview of Theoretical Explanations of Dark Matter

Hitoshi Murayama
290E, September 11, 2019

Five empirical evidences for physics beyond SM

- at least five missing pieces in the SM:

- dark matter

- neutrino mass

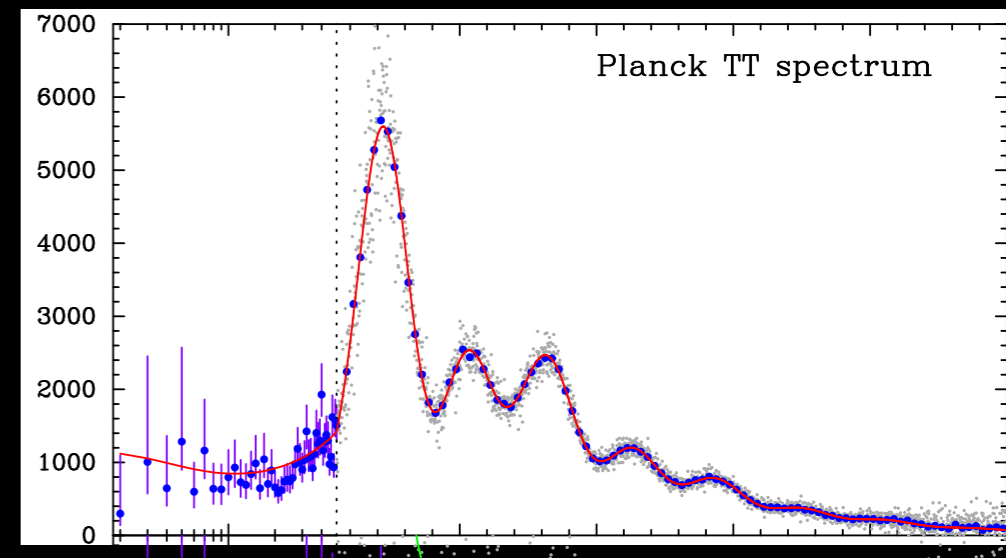
- dark energy galaxy surveys
DESI, PFS, Euclid,
LSST, WFIRST

- apparently acausal density fluctuations

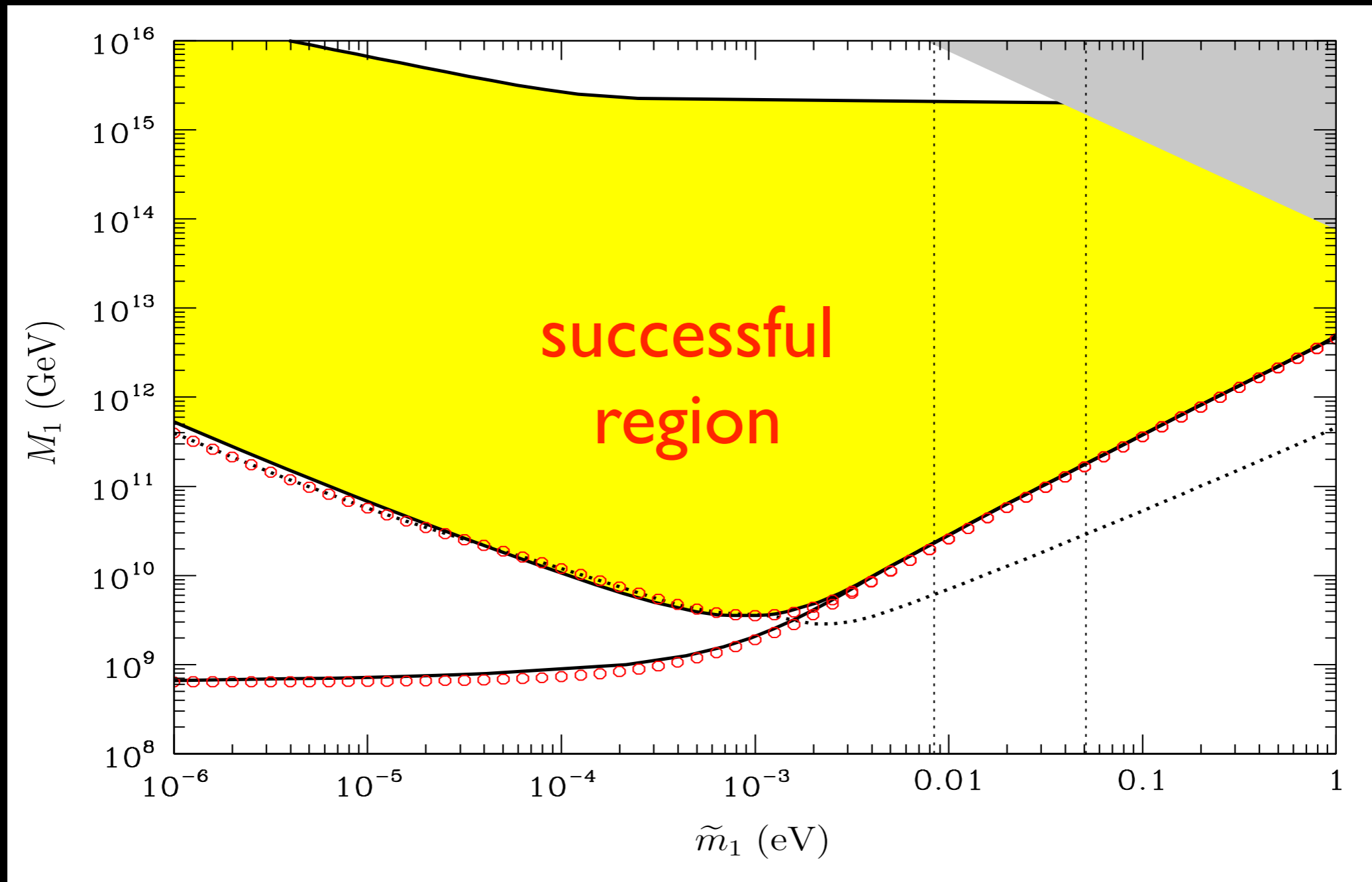
- baryon asymmetry HyperK, DUNE
LHCb, Belle II

$0\nu\beta\beta$
gravitational wave

Simons Array
CMB S4
LiteBIRD

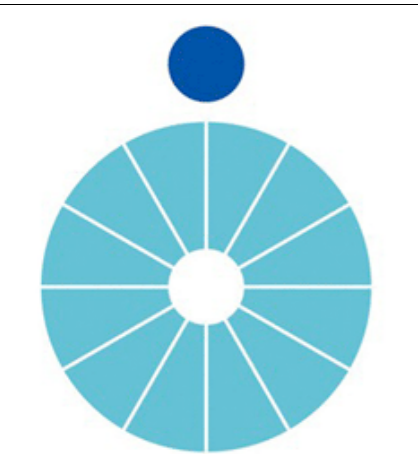


Leptogenesis



$$\tilde{m}_1 = \frac{(m_D^\dagger m_D)_{11}}{M_1}$$

di Bari, Plümacher,
Buchmüller

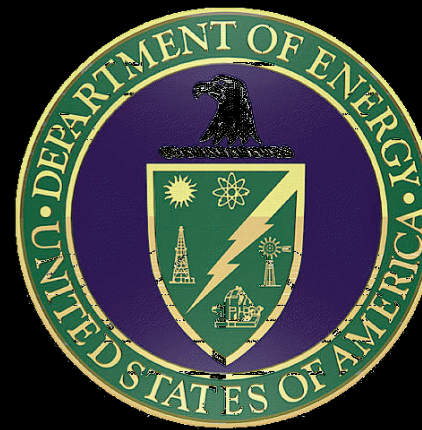


文部科学省

MEXT

MINISTRY OF EDUCATION,
CULTURE, SPORTS,
SCIENCE AND TECHNOLOGY-JAPAN

How do we test it?

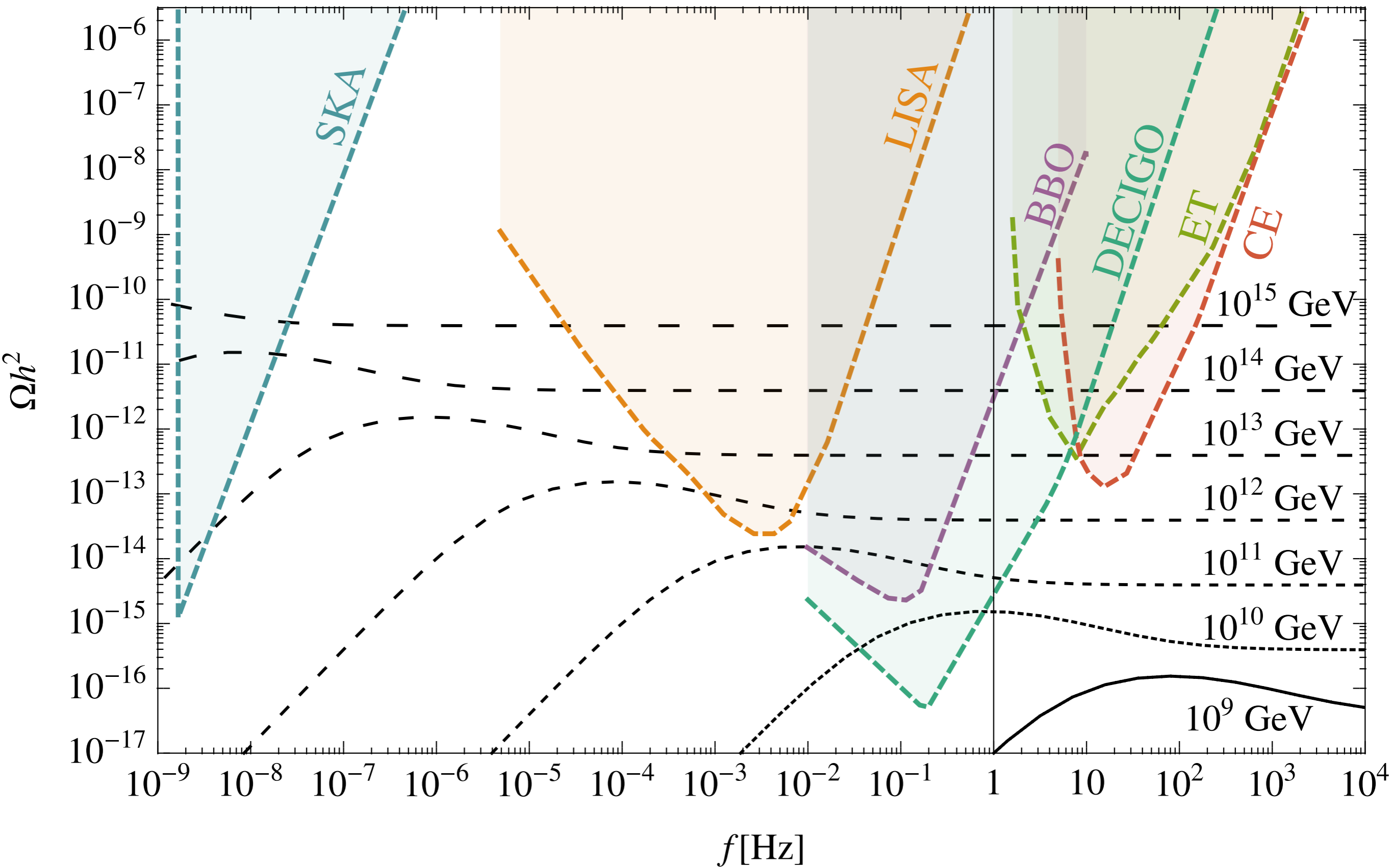


build a 10^{14} GeV collider

how do we test it?

- possible three circumstantial evidences
 - $0\nu\beta\beta$
 - CP violation in neutrino oscillation
 - other impacts e.g. LFV (requires new particles/interactions < 100 TeV)
- *archeology*
- *any more circumstantial evidences?*





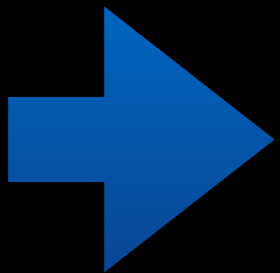
J. Dror, T. Hiramatsu, K. Kohri, HM, G. White, arXiv:1908.03227

covers pretty much the entire range for leptogenesis!

caveat: particle emission from cosmic strings

Five empirical evidences for physics beyond SM

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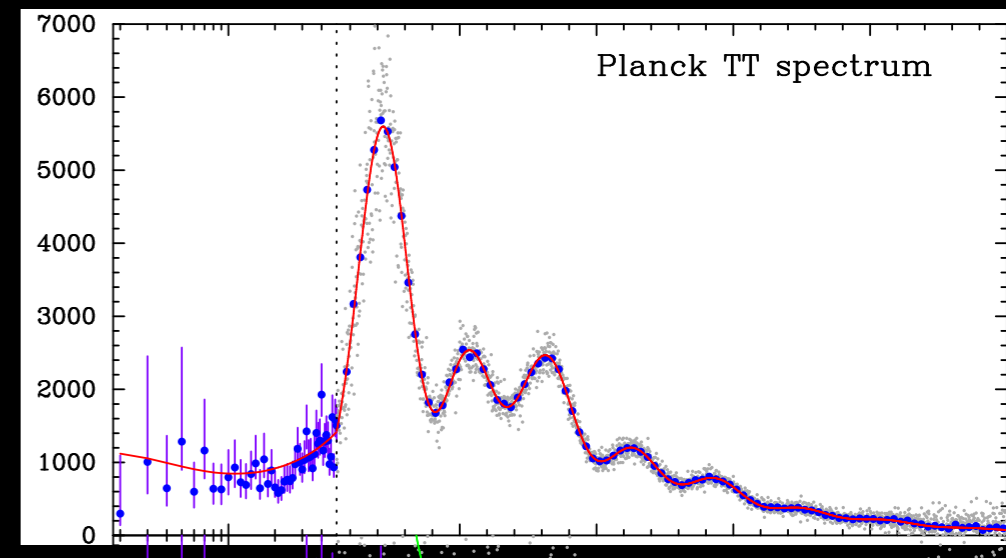
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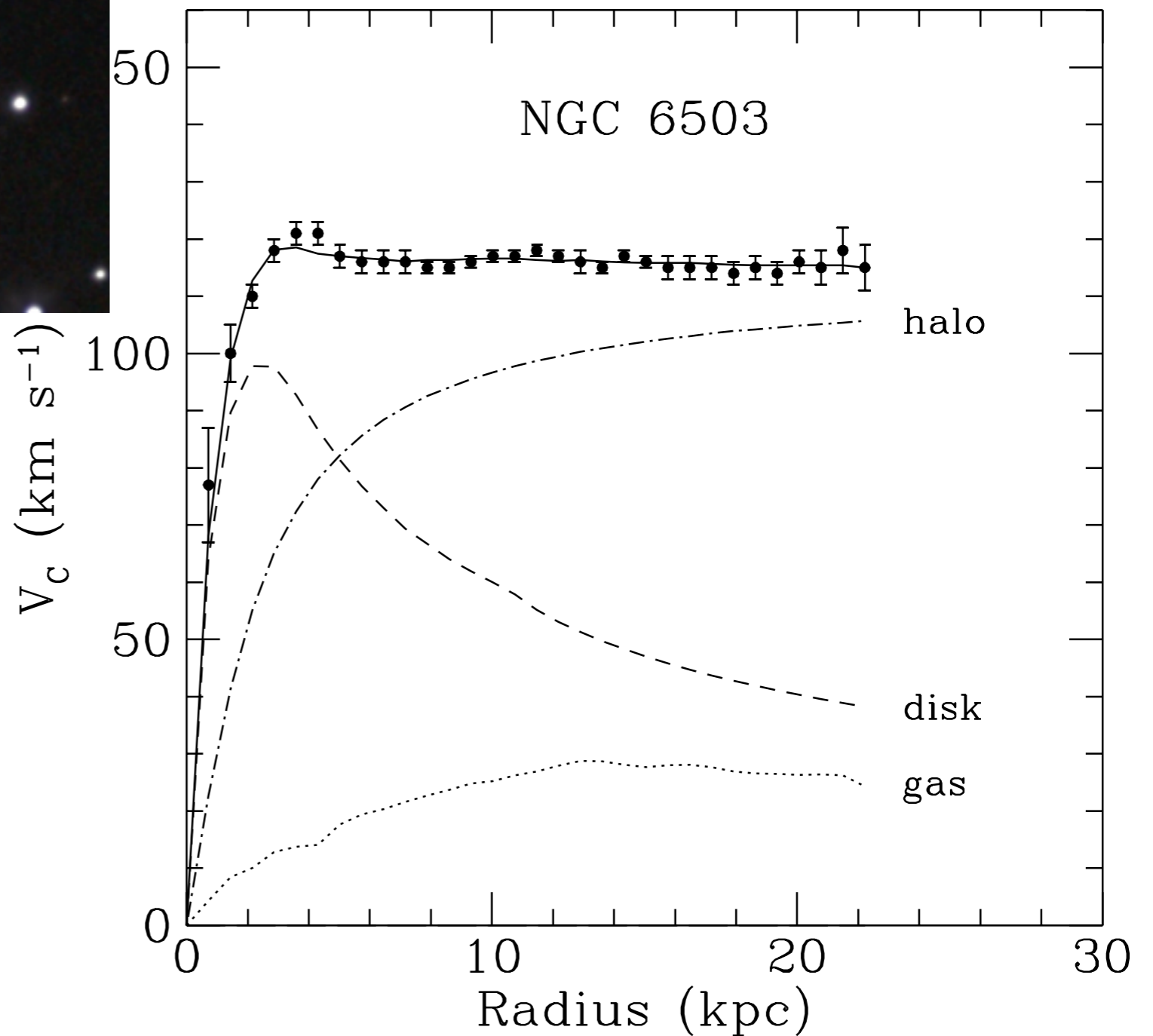
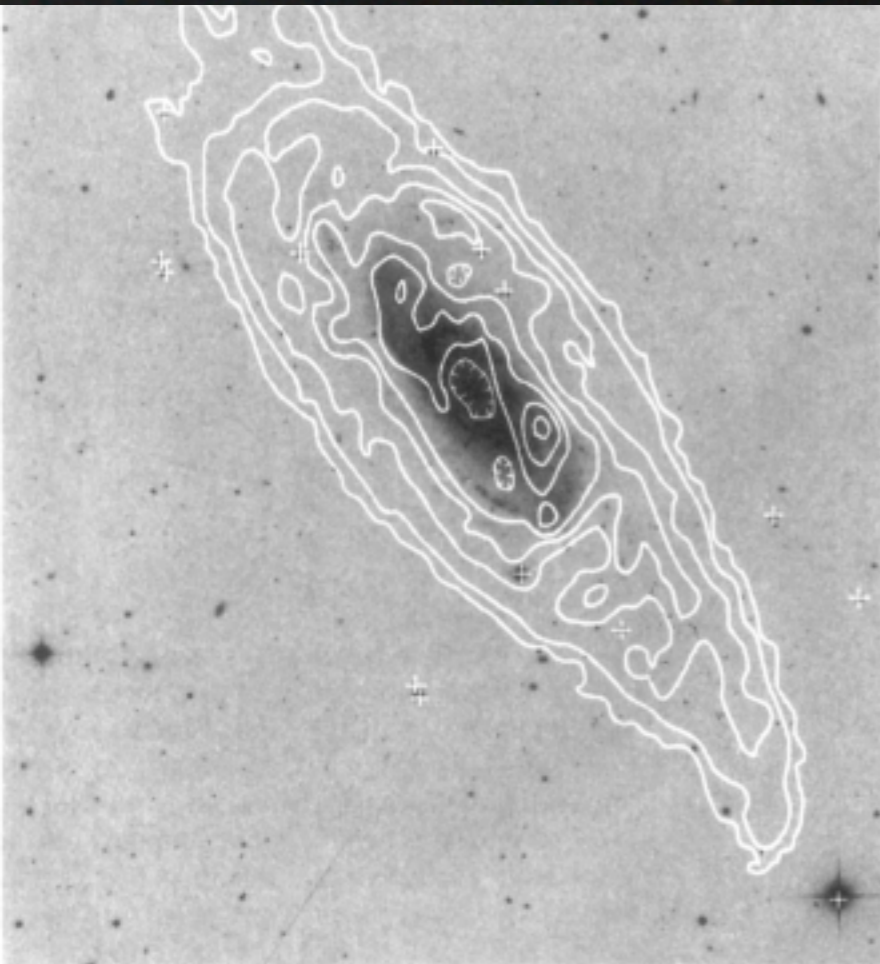


$0\nu\beta\beta$
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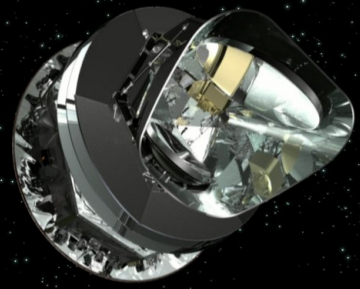
galactic rotation curves



cluster of galaxies

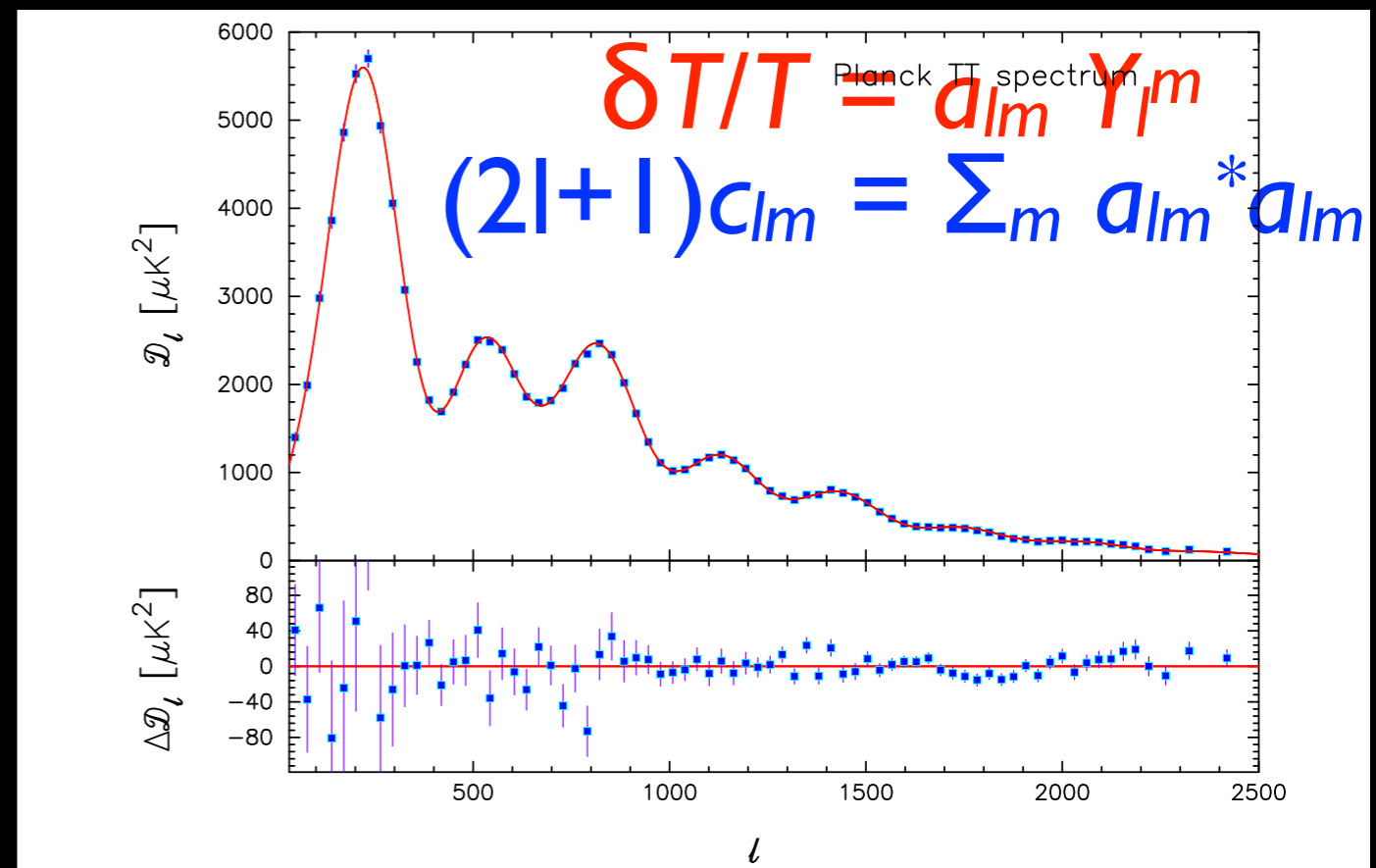
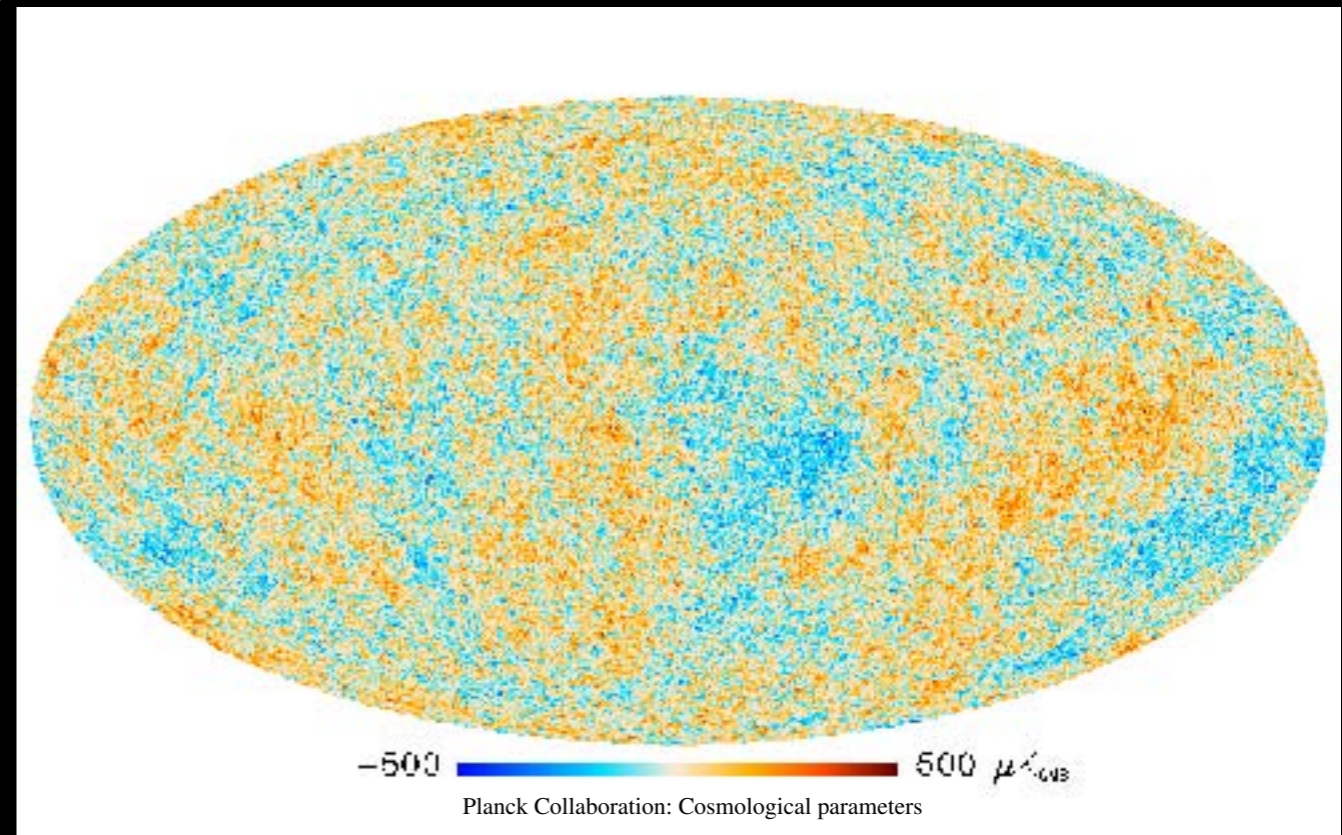


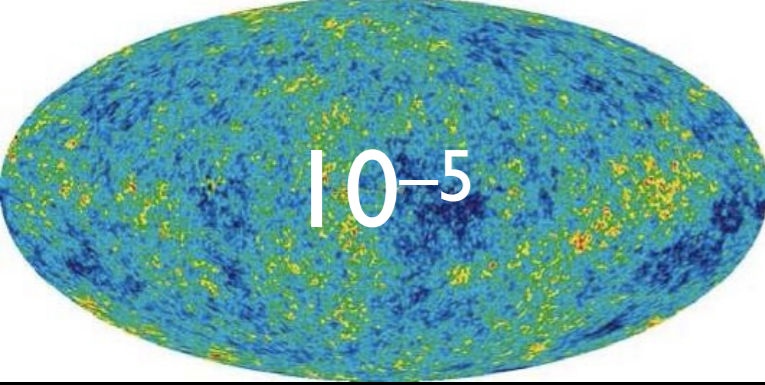
Abell 2218
2.1 B lyrs



cosmological scales

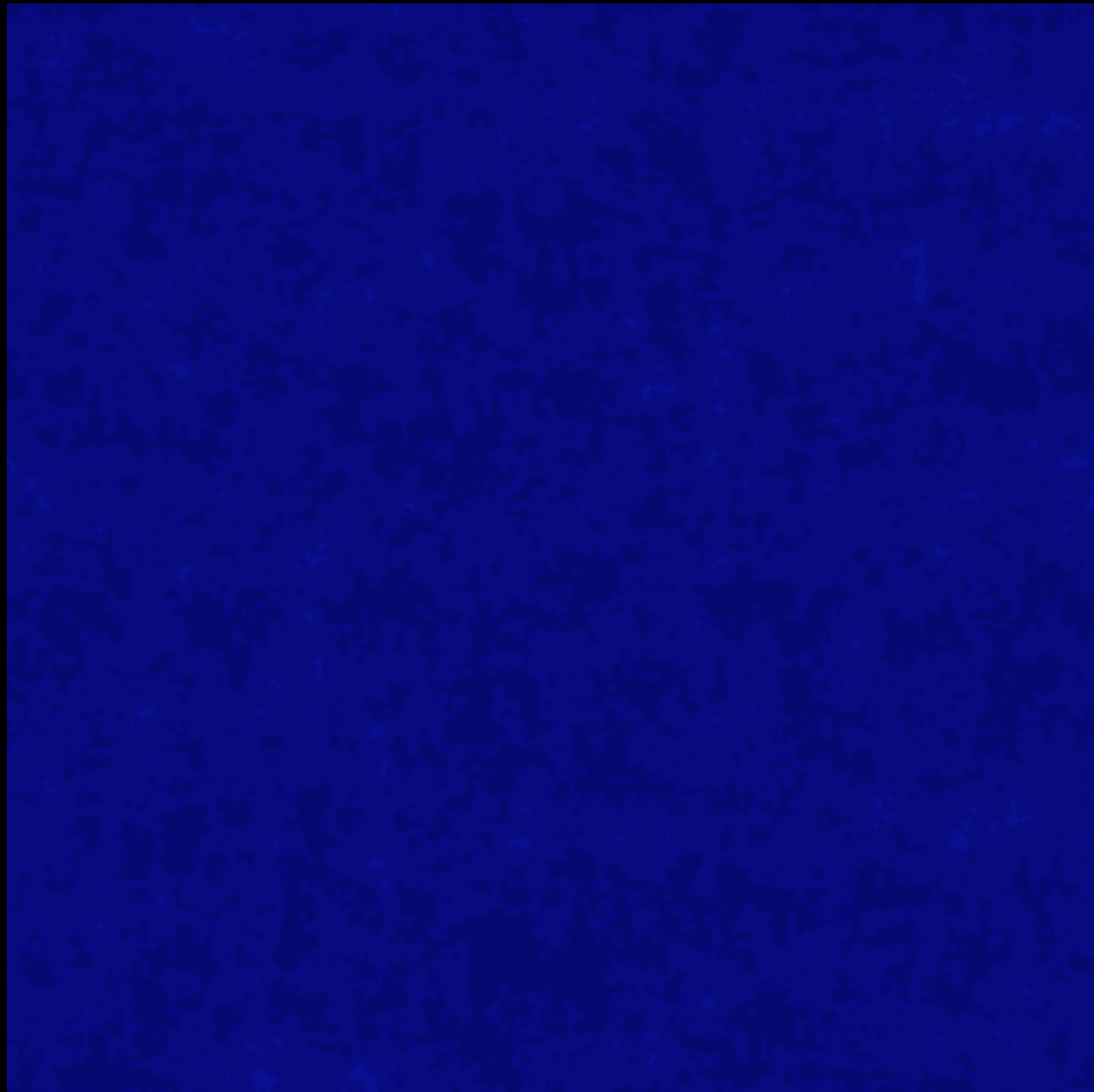
- a random density fluctuations $\sim O(10^{-5})$ more-or-less **scale invariant** $P(k) \propto k^{ns-1}$
- starts acoustic oscillation, amplified by gravitational attraction
- “knows” about everything between $0 < z < 1300$
- $\Omega_{DM}=0.25 \gg \Omega_b=0.05$



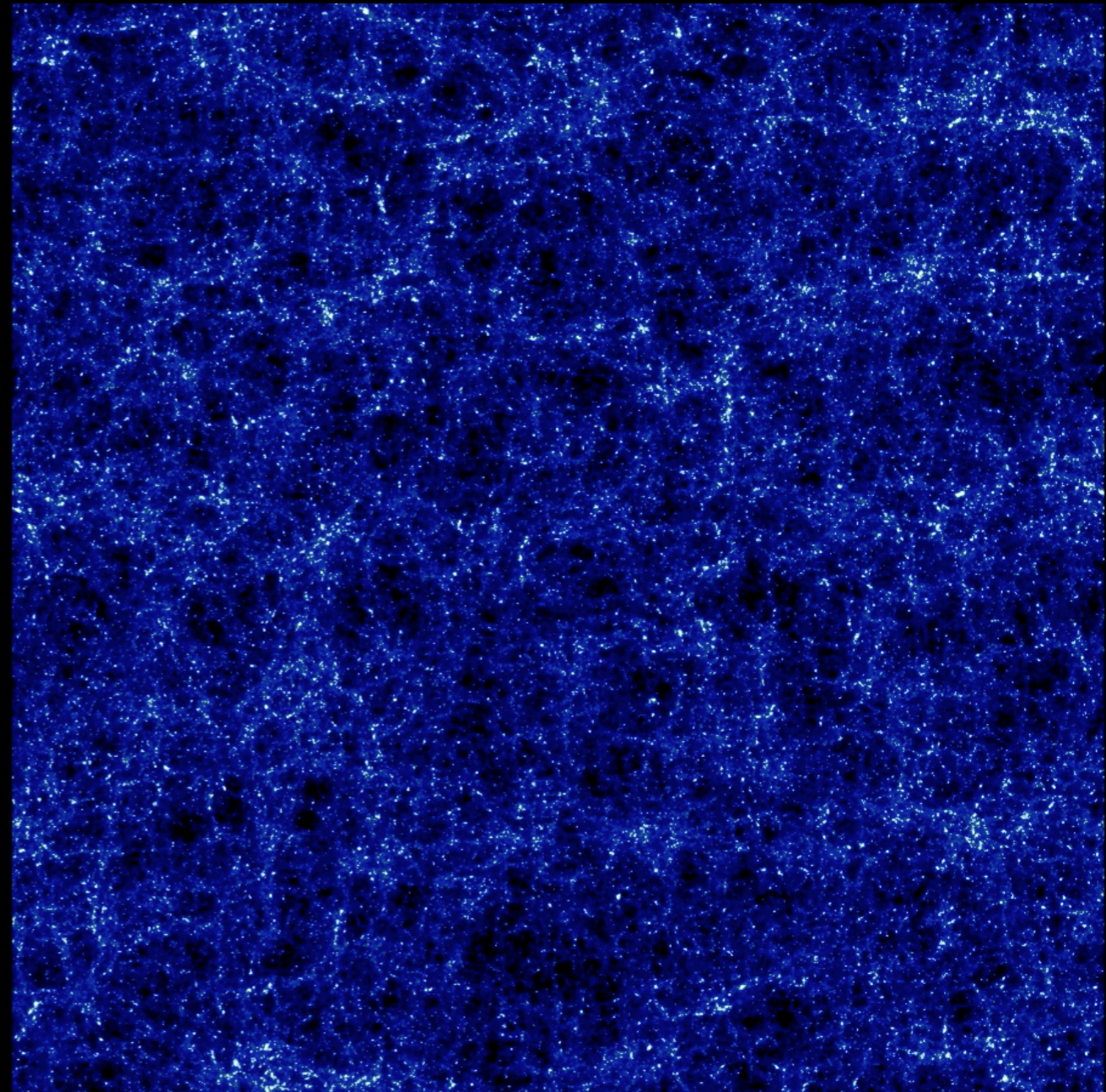


Dark Matter is our Mom

Naoki Yoshida



without dark matter

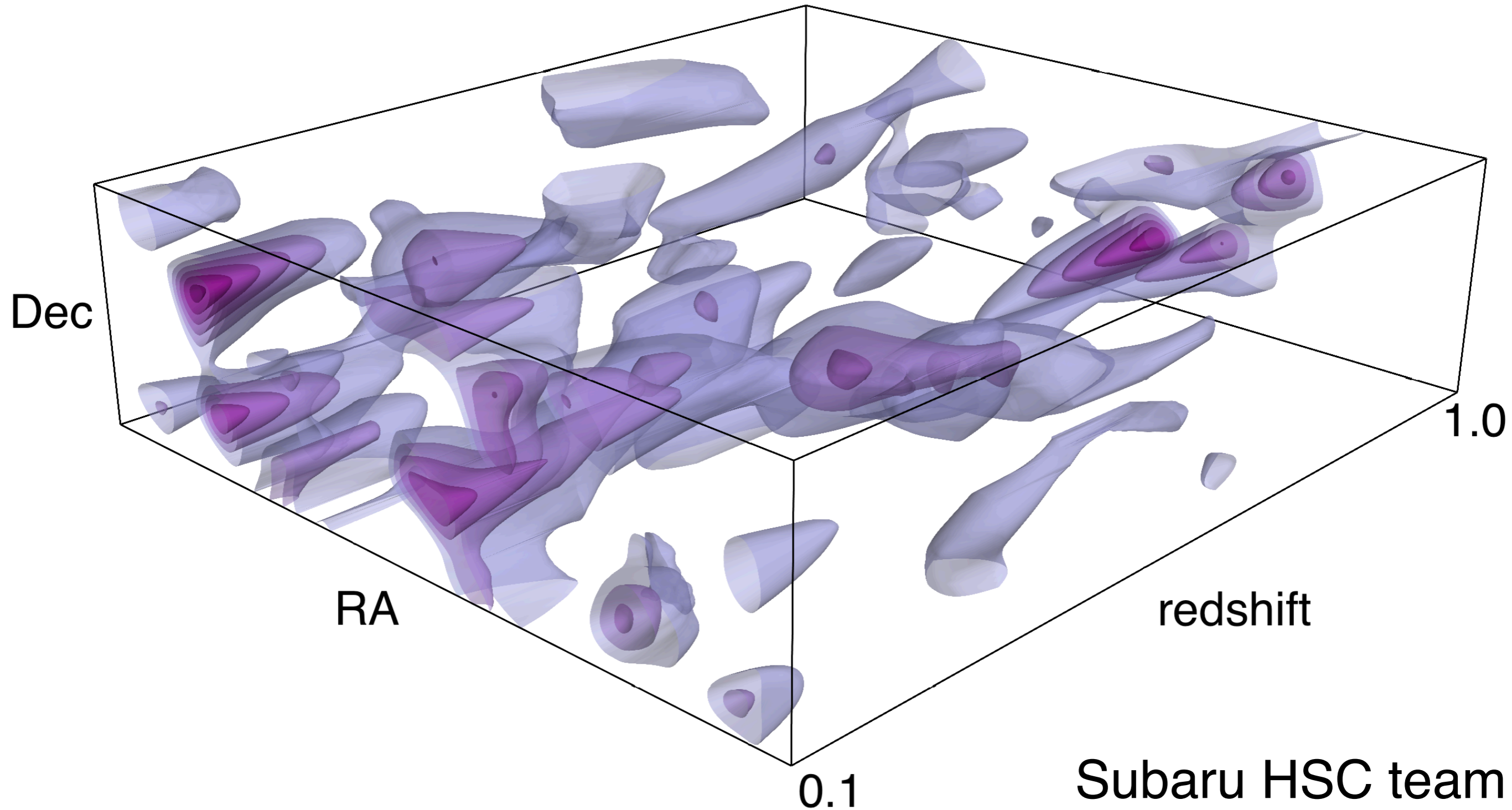


with dark matter

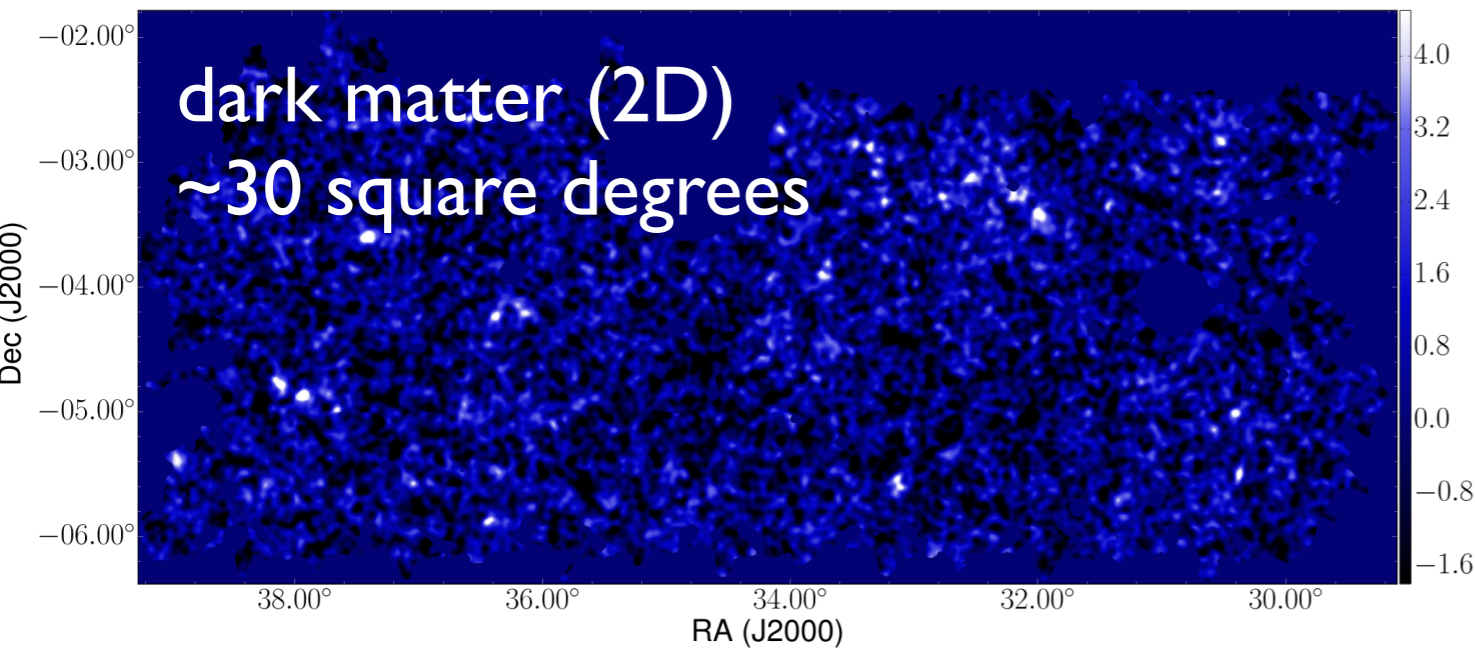
Reenacting the Big Bang with Cal Marching Band



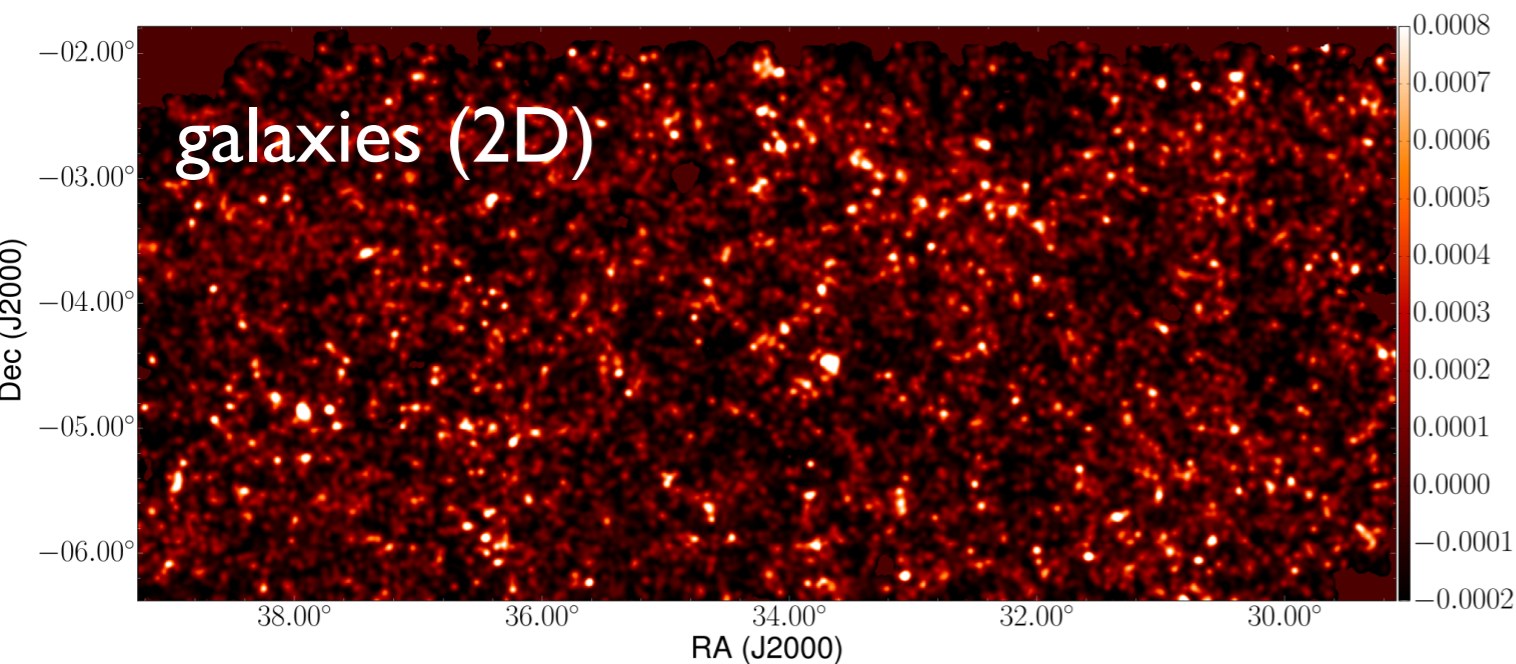
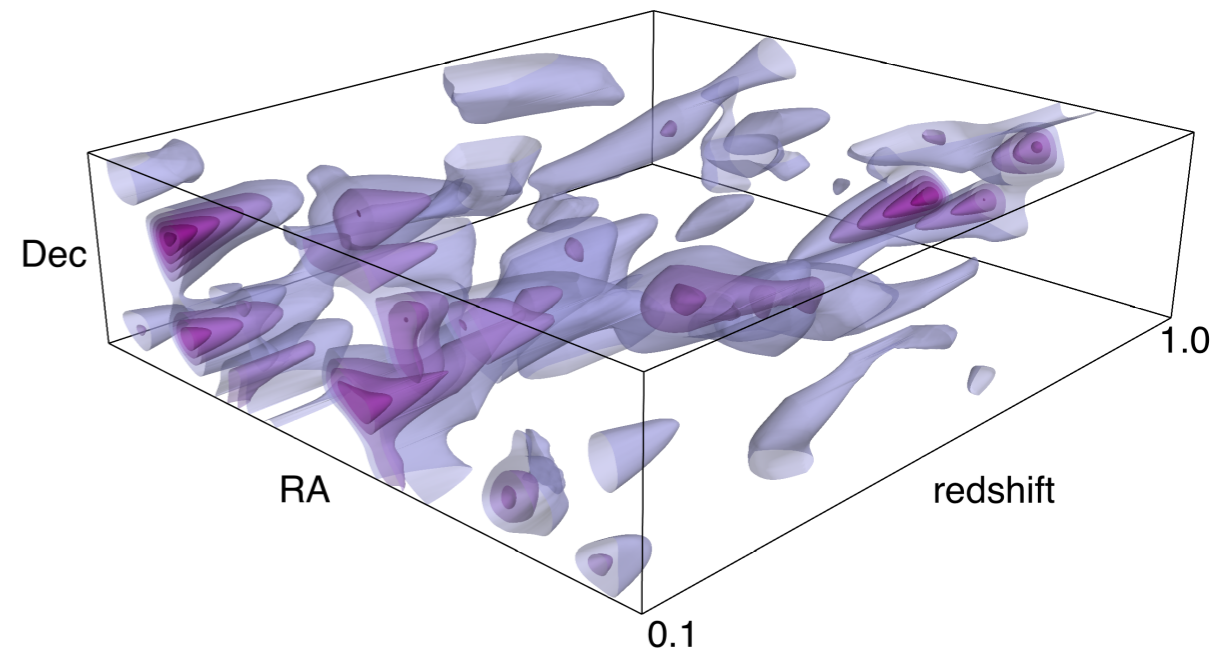
World's largest 3D map of dark matter



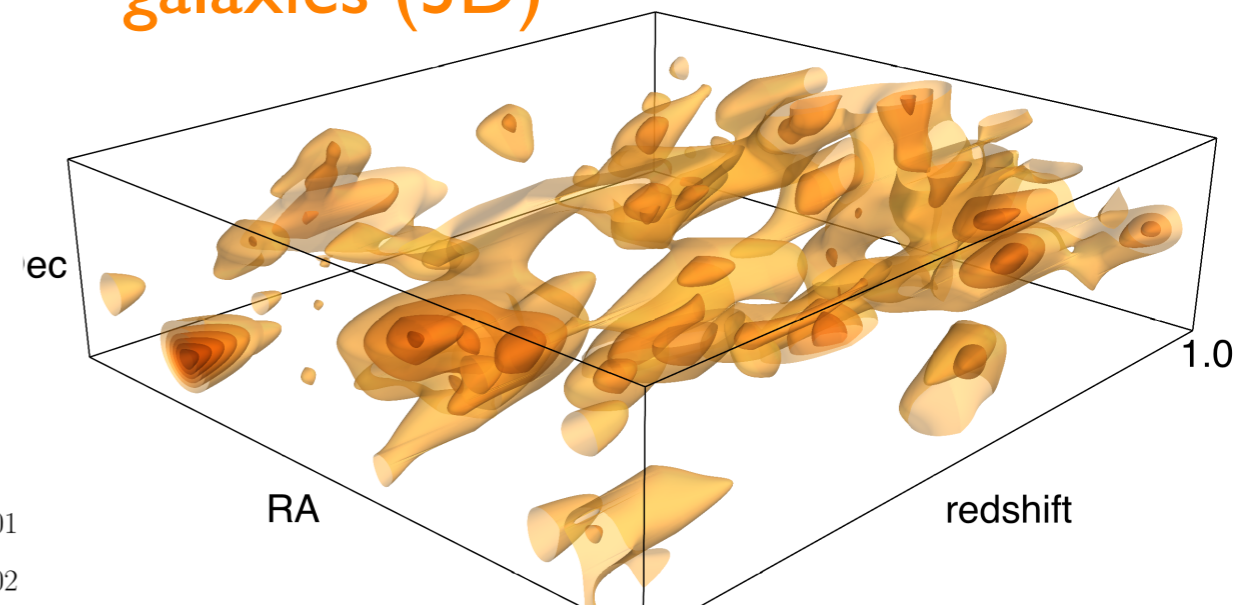
dark matter made us



dark matter (3D)



galaxies (3D)



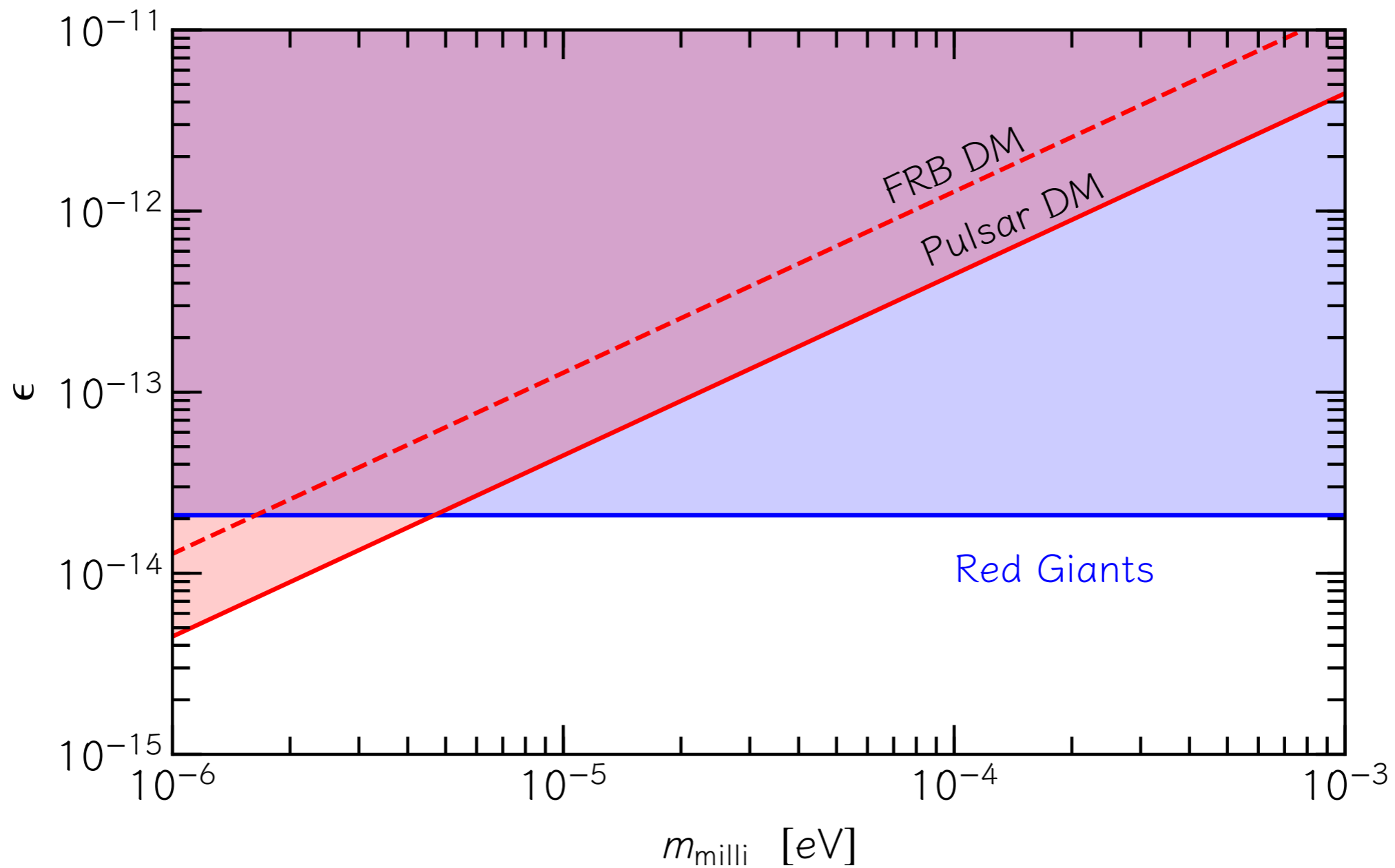
Subaru HSC team

What do we know?

- basic properties of a particle:
 - mass
 - quantum number
 - spin
 - lifetime
 - interaction

Cold and Neutral

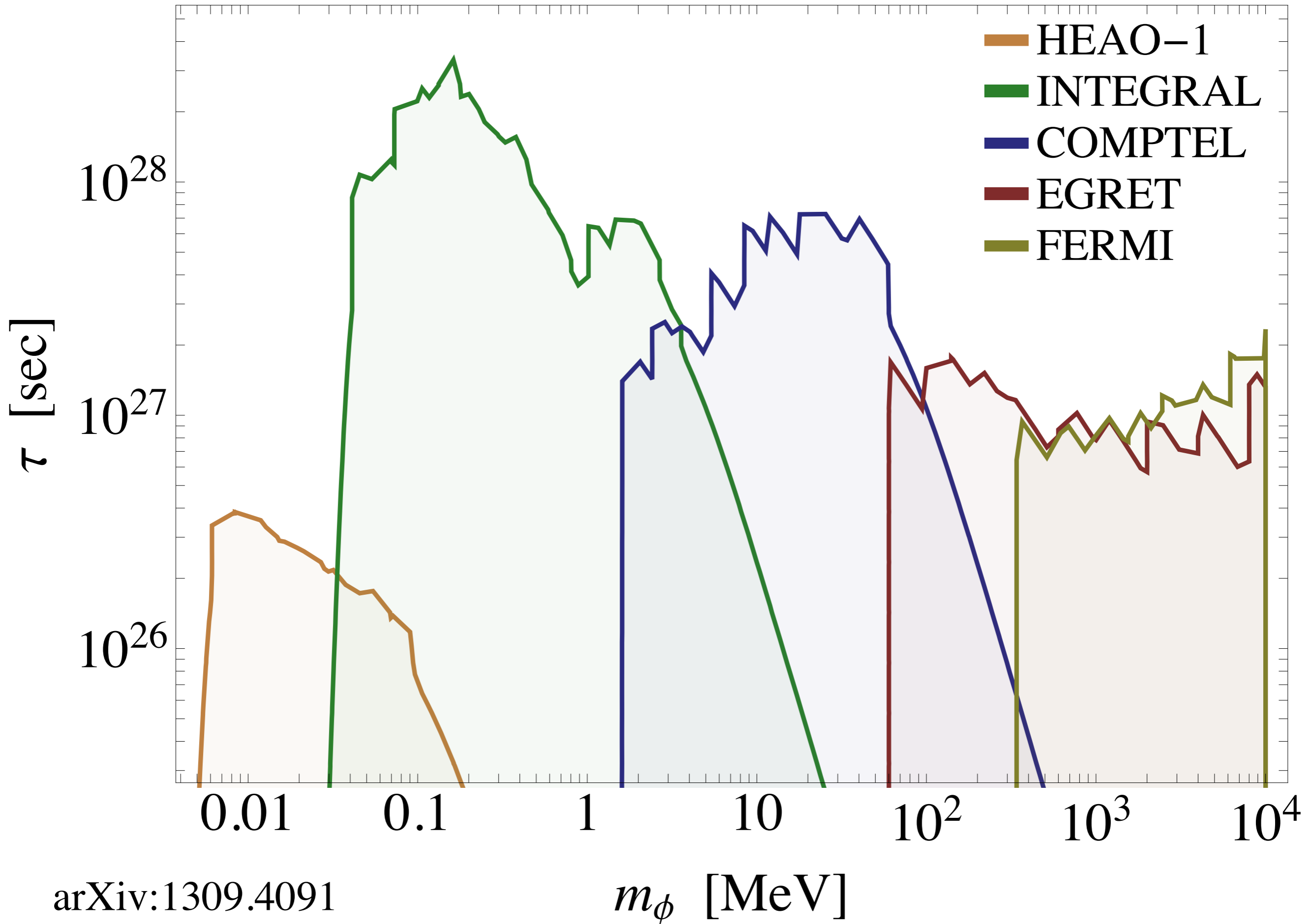
- it must be moving slowly (cold)
- it must be electrically neutral
 - people discuss milli-charged dark matter
- it must be long-lived (at least 13.8 Byrs)
 - stronger limit if decay products visible



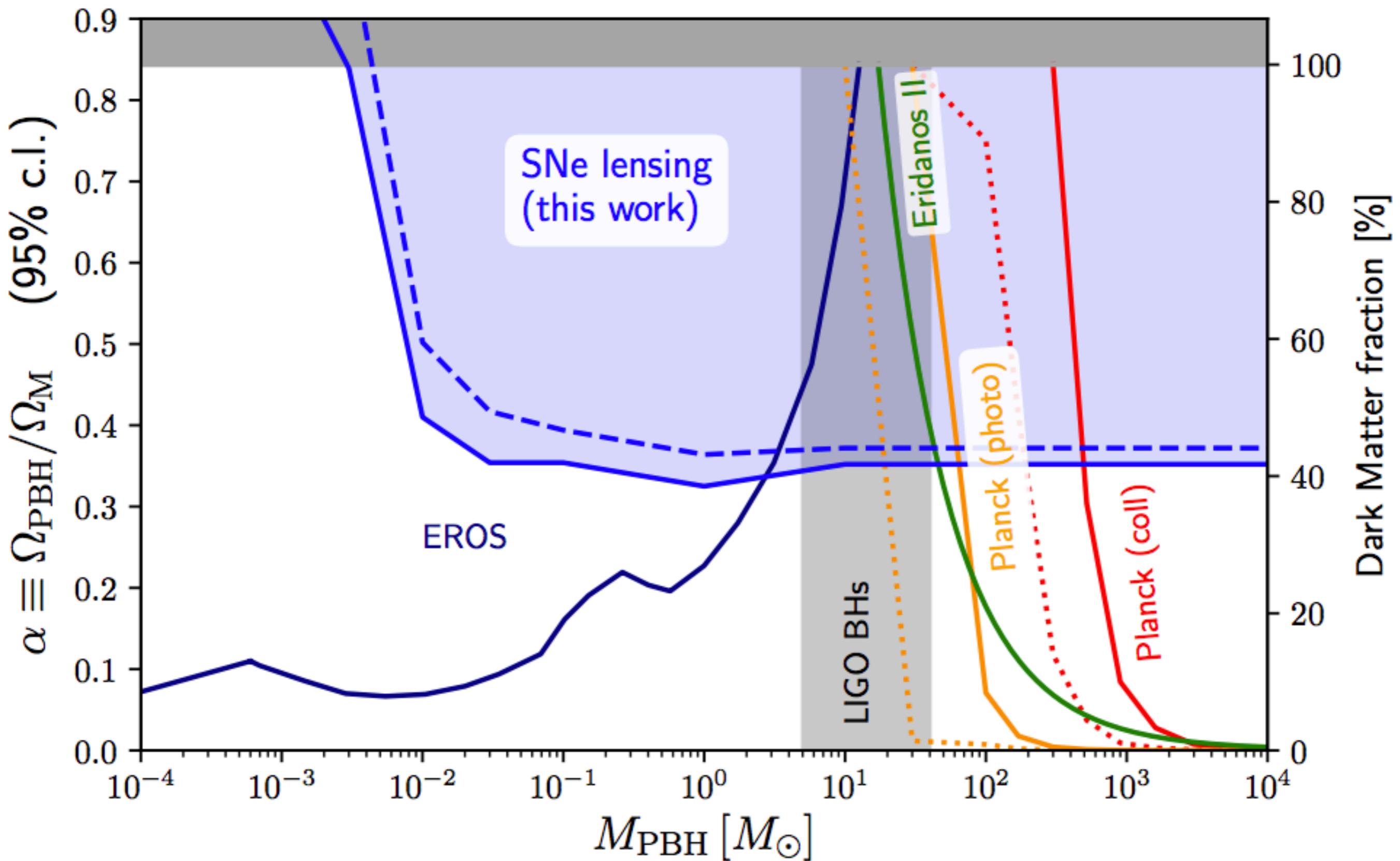
arXiv:1902.02695

FIG. 1. *Constraint on millicharged DMA in the $\epsilon - m_{\text{milli}}$ space from pulsar (solid red line) and FRB 121102 (dashed red line) DM at 95% confidence level. Solid blue line indicates the bound from Red Giants [15]. We assume a homogeneous DMA density $\rho_{\text{dm}} = \rho_{\text{milli}} \approx 0.3 \text{ GeV}/\text{cm}^3$. The bound scales as $\rho_{\text{milli}}^{-1/2}$ for fractional components.*

$$\phi \rightarrow \gamma\gamma$$



Current bounds on MACHOs

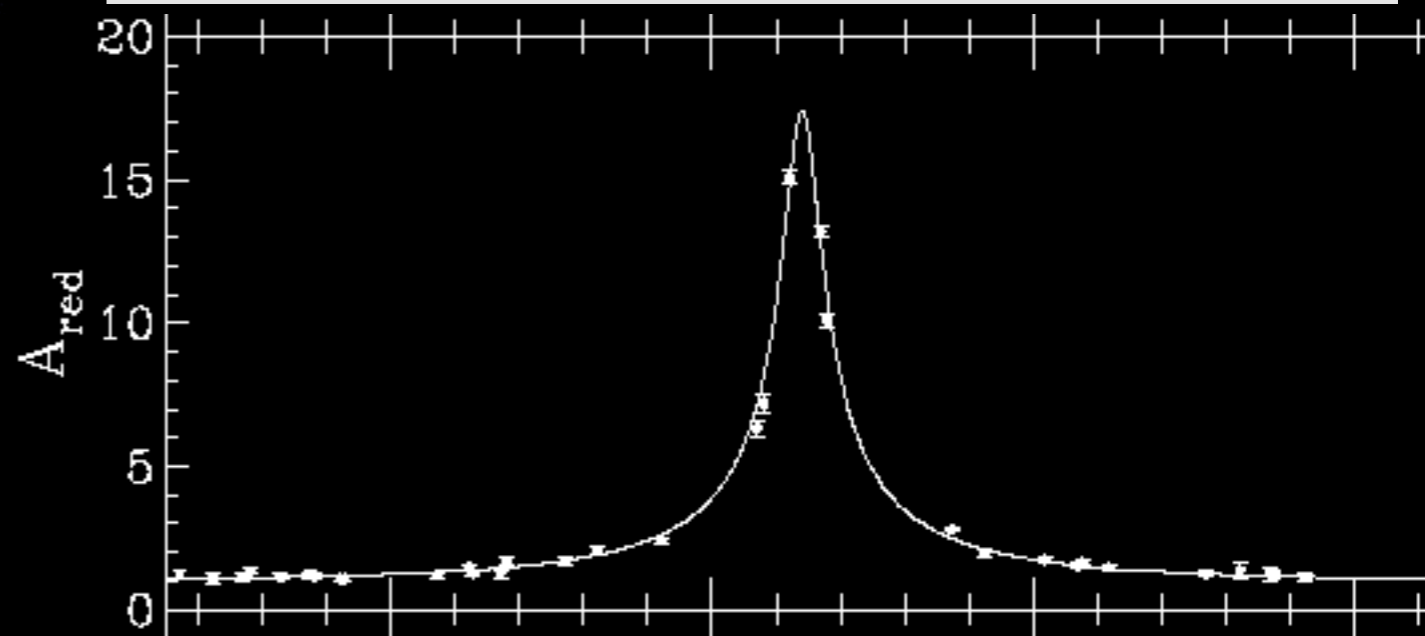
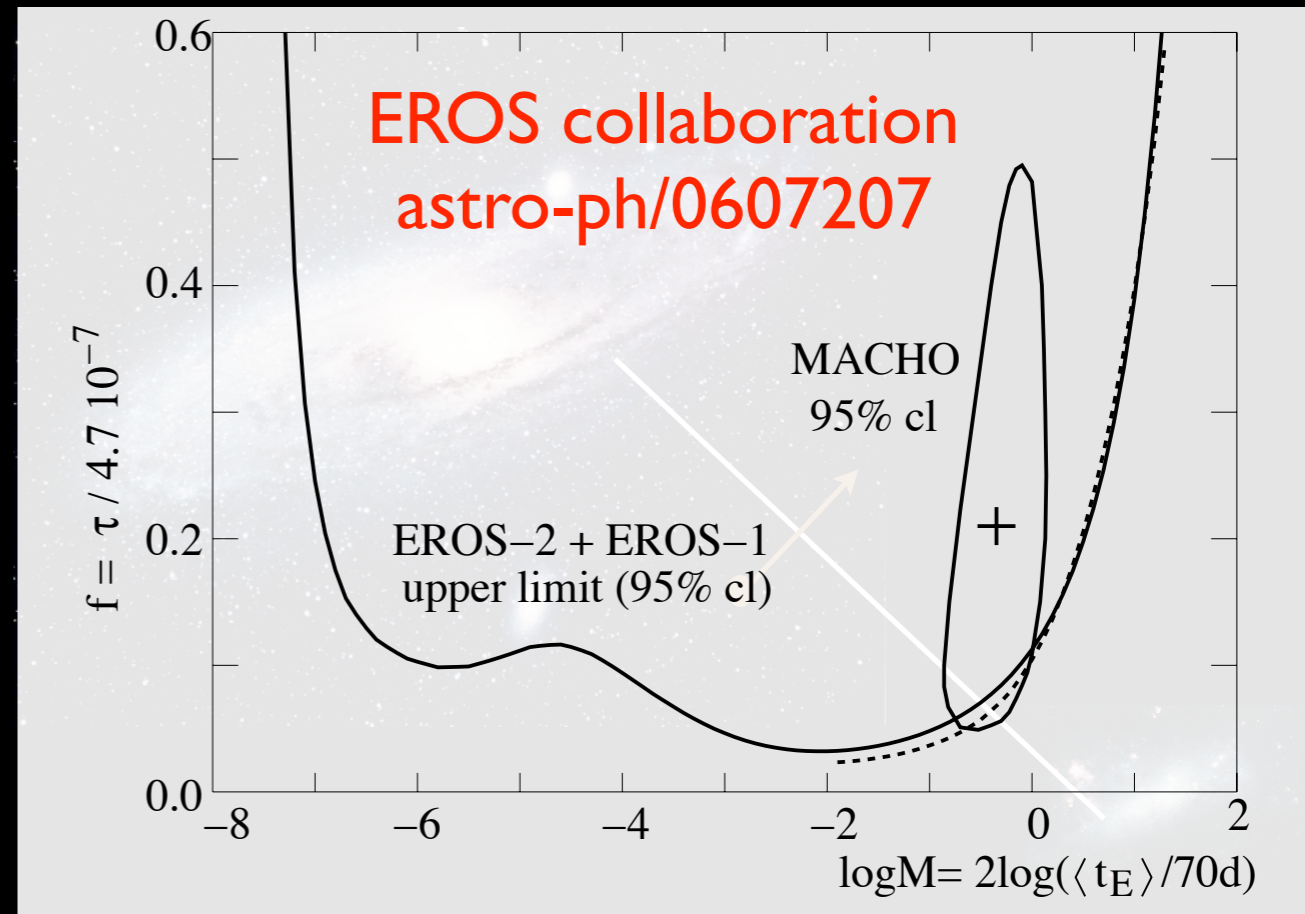


Dim Stars?

Search for **MACHOs**
(Massive Compact Halo Objects)



Large Magellanic Cloud



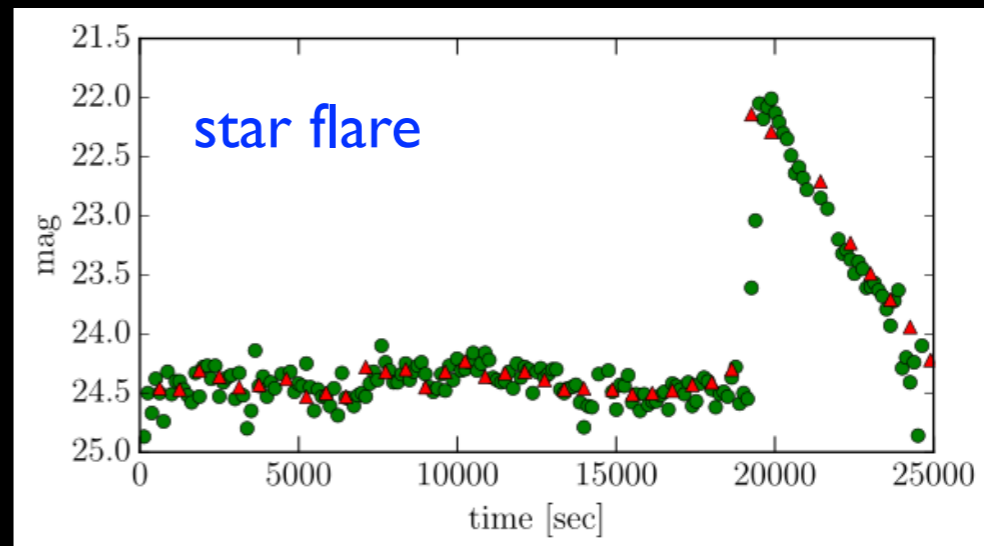
Not enough of them!

Best limit on Black Hole dark matter

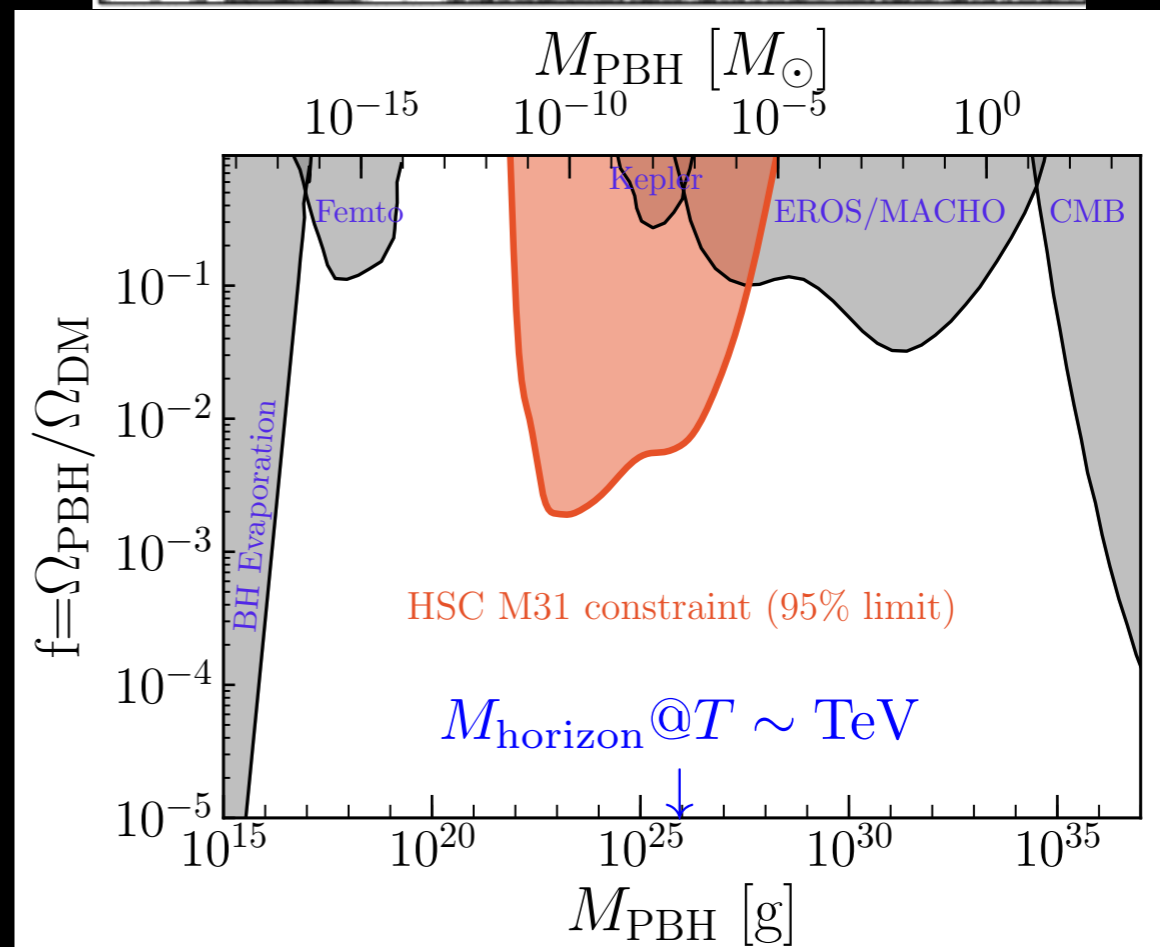
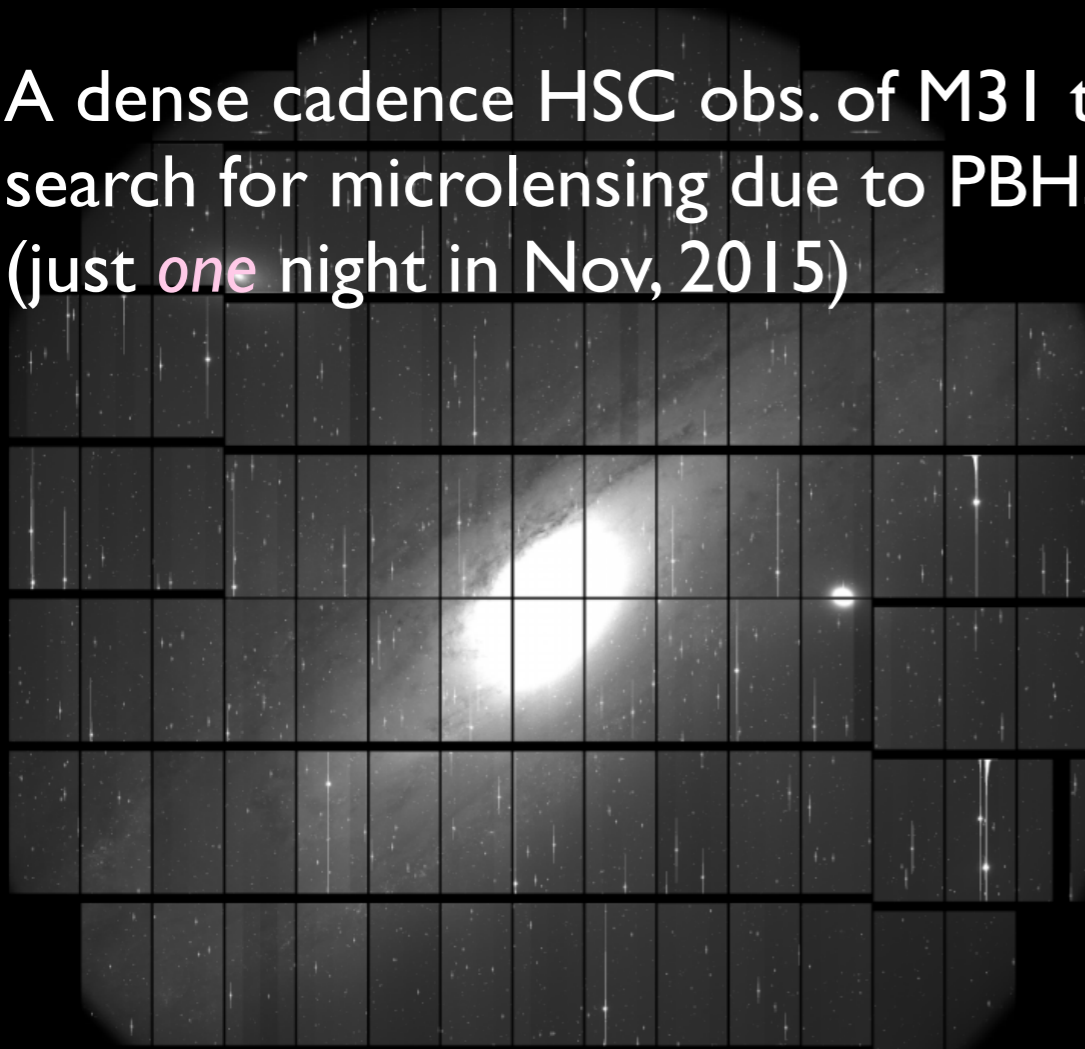
Niikura, Takada et al., *Nature Astronomy*



Found many variable stars



A dense cadence HSC obs. of M31 to search for microlensing due to PBHs (just *one* night in Nov, 2015)



No detection \Rightarrow more stringent upper bound, than 2yr Kepler data (Griest et al.)

Mass Limits

“Uncertainty Principle”

- Clumps to form structure
- imagine $V = G_N \frac{Mm}{r}$
- “Bohr radius”: $r_B = \frac{\hbar^2}{G_N M m^2}$
- too small $m \Rightarrow$ won’t “fit” in a galaxy!
- $m > 10^{-22}$ eV “uncertainty principle” bound
(modified from Hu, Barkana, Gruzinov, astro-ph/0003365)

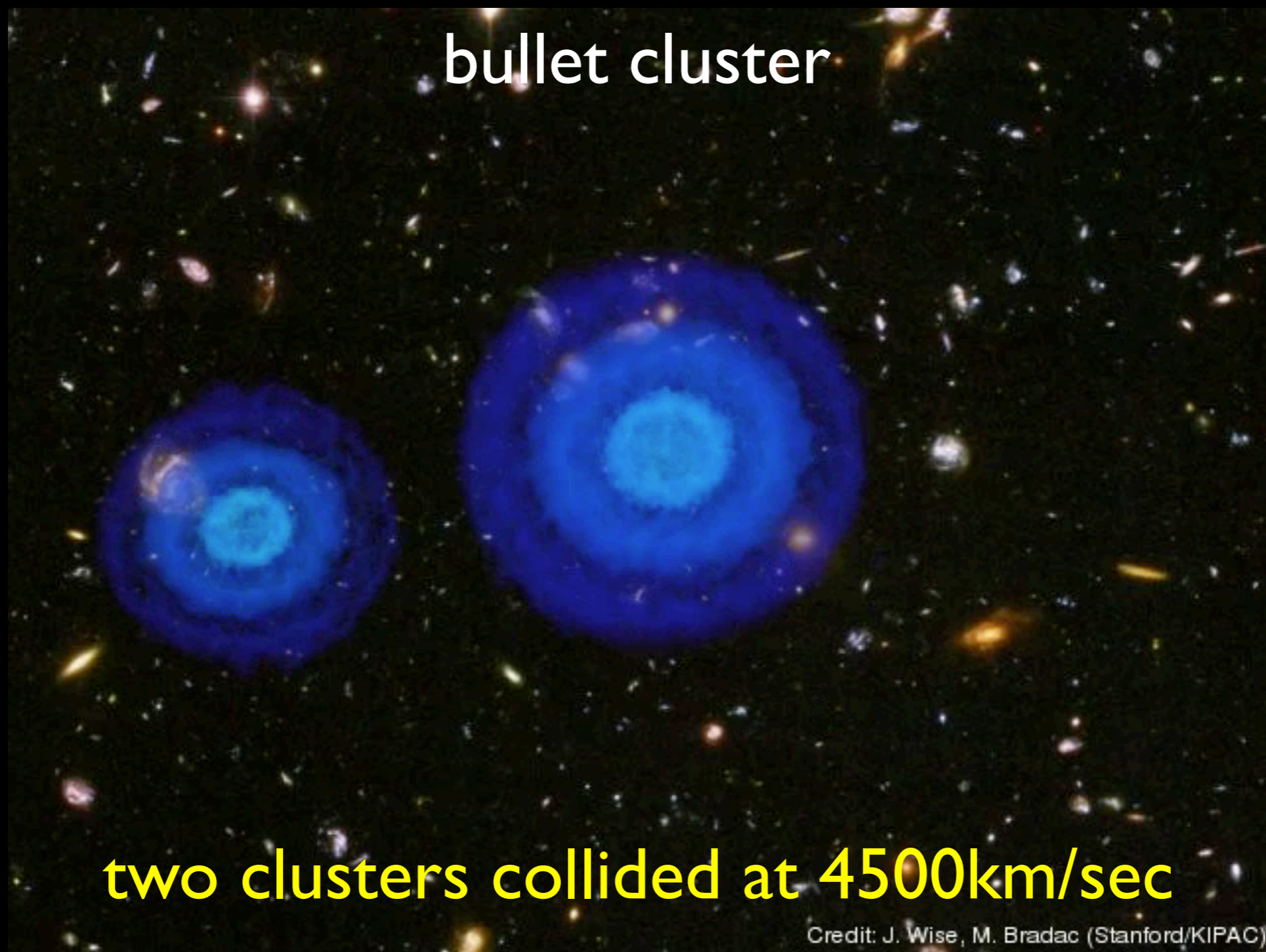
Summary

Mass Limits

- 10^{-31} GeV to 10^{46} GeV
- narrowed it down to within 77 orders of magnitude
- a *big progress* in 70 years since Zwicky



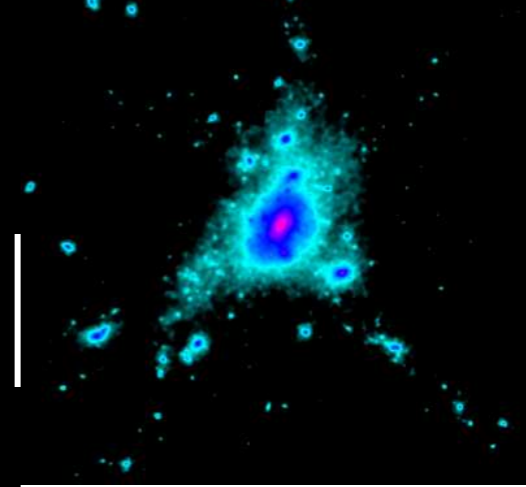
Good not to be here



4B lyrs away

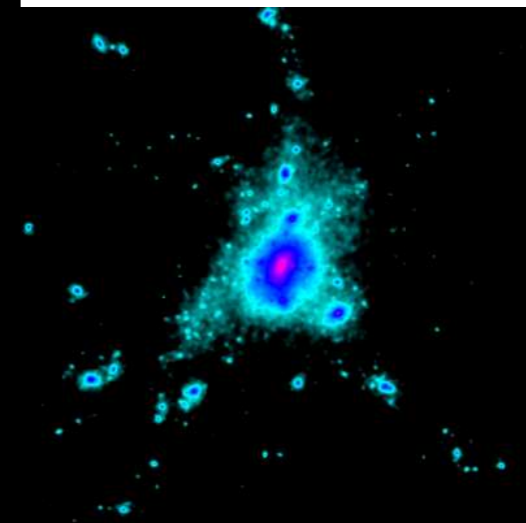
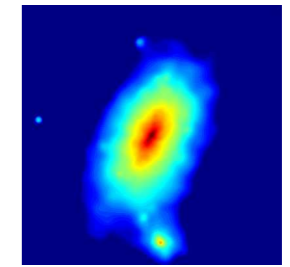
Self-Coup

- if self-coupling too big, will “smooth out” cuspy profile at the galactic center
- some people want it
(Spergel and Steinhardt, astro-ph/9909386)
- need core $< 35 \text{ kpc}/h$ from data
 $\sigma < 1.7 \times 10^{-25} \text{ cm}^2 \text{ (m/GeV)}$
(Yoshida, Springel, White, astro-ph/0006134)
- bullet cluster:
 $\sigma < 1.7 \times 10^{-24} \text{ cm}^2 \text{ (m/GeV)}$
(Markevitch et al, astro-ph/0309303)



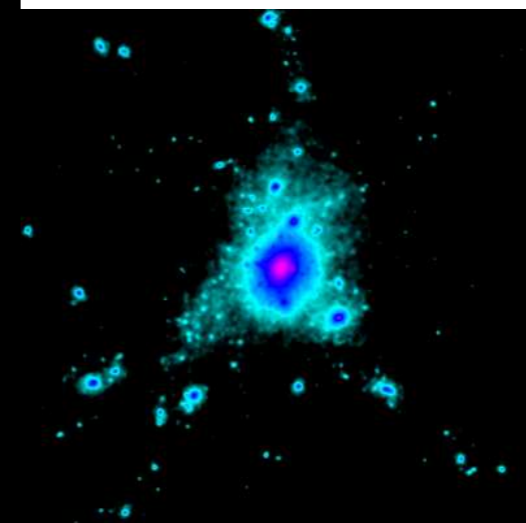
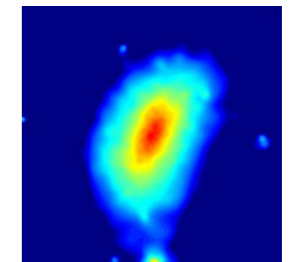
S1

1 : 0.82 : 0.65



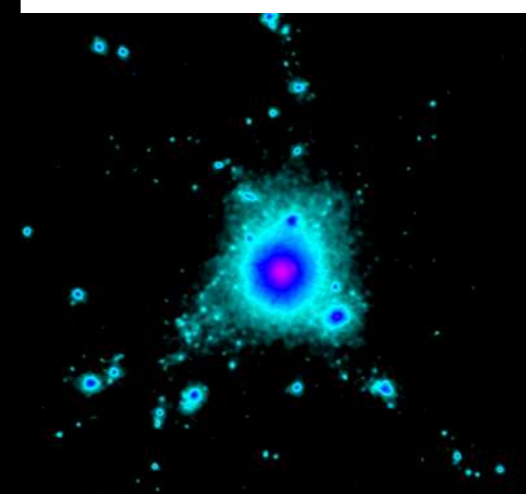
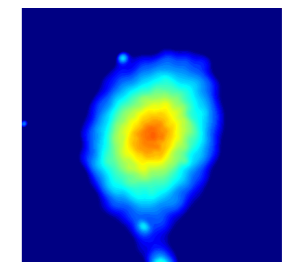
S1Wa

$\sigma^* = 0.1 \text{ cm}^2 \text{g}^{-1}$
 $r_c = 40 h^{-1} \text{ kpc}$
1 : 0.88 : 0.66



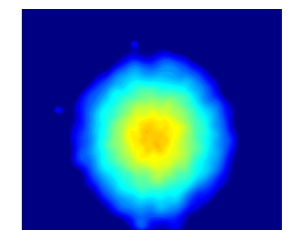
S1Wb

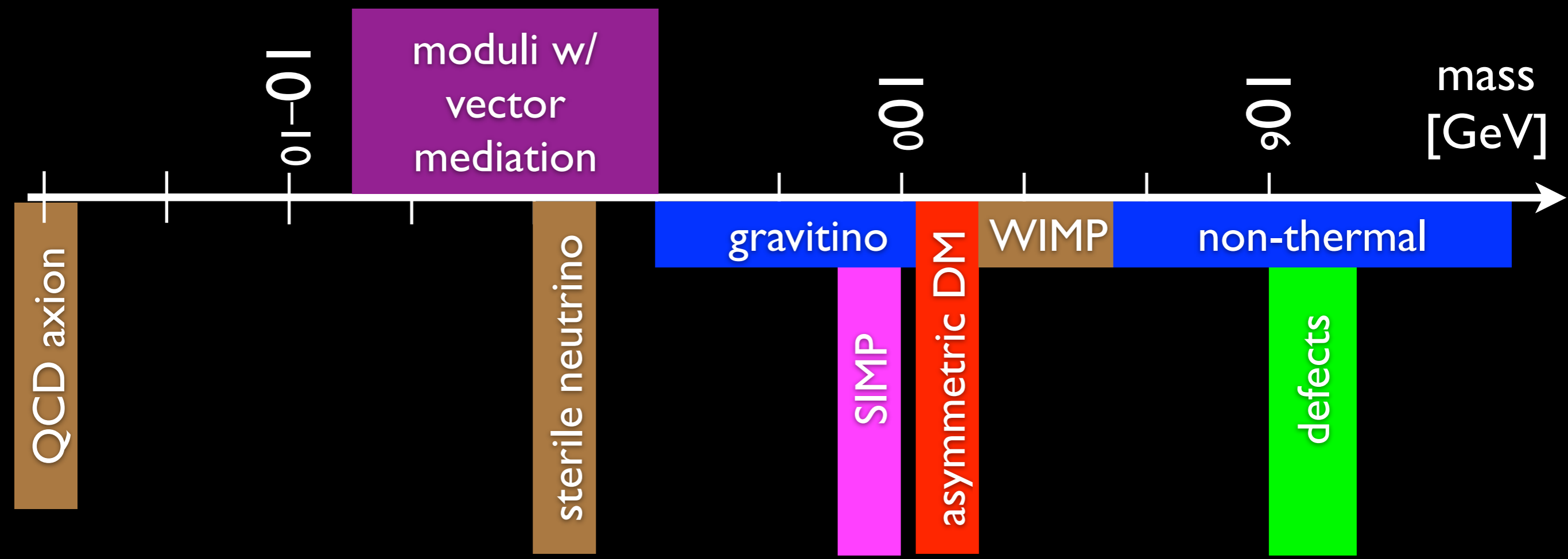
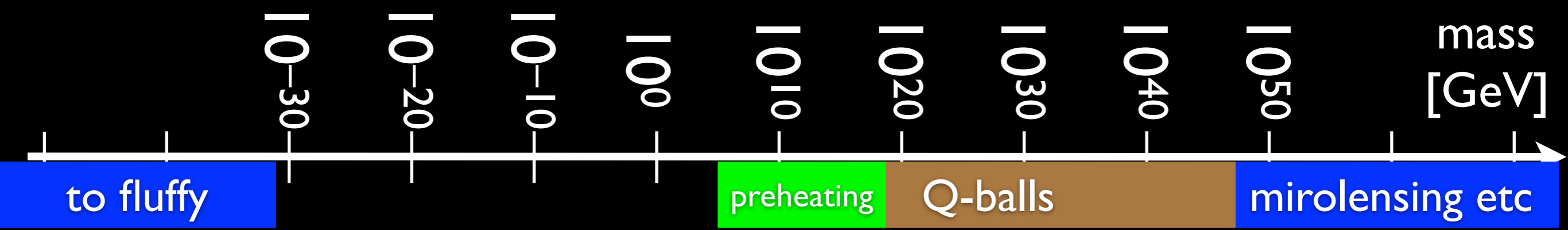
$\sigma^* = 1.0 \text{ cm}^2 \text{g}^{-1}$
 $r_c = 100 h^{-1} \text{ kpc}$
1 : 0.91 : 0.72



S1Wc

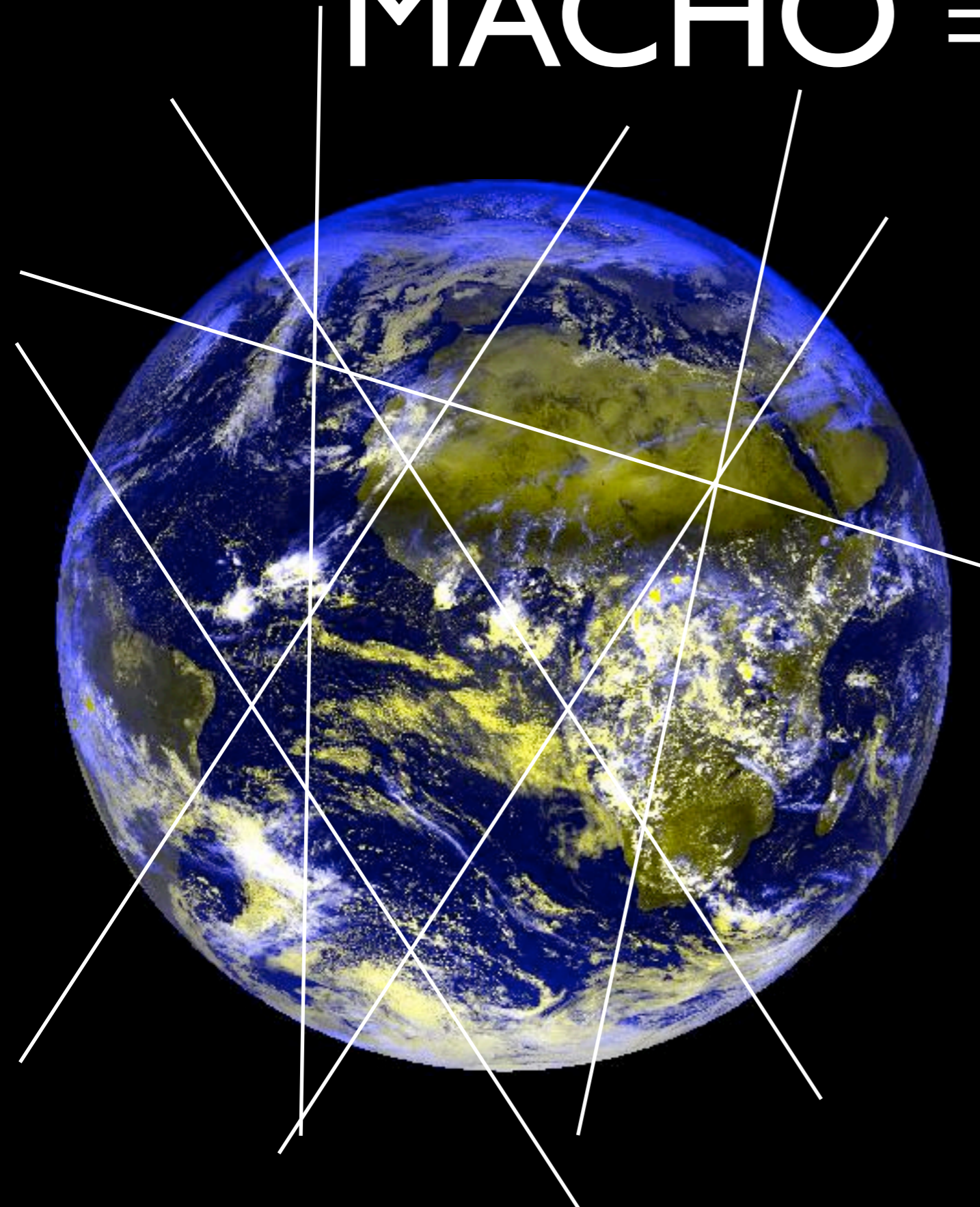
$\sigma^* = 10.0 \text{ cm}^2 \text{g}^{-1}$
 $r_c = 160 h^{-1} \text{ kpc}$
1 : 0.98 : 0.89





Can't do justice to many many ideas in the literature!

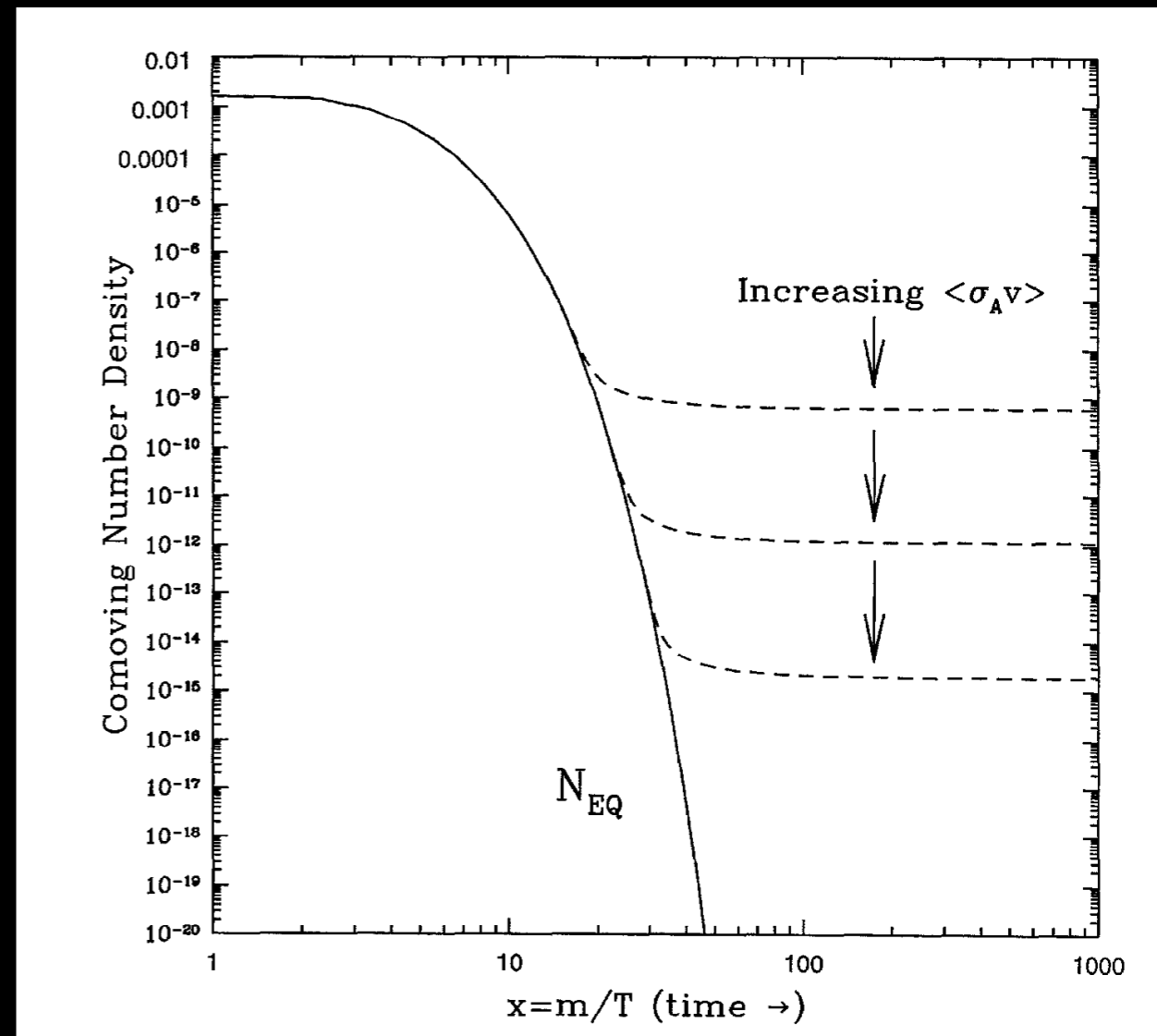
MACHO \Rightarrow WIMP



- It is probably **WIMP** (Weakly Interacting Massive Particle)
- Stable heavy particle produced in early Universe, **left-over from near-complete annihilation**
- Will focus on WIMPs for the rest of the lecture

thermal relic

- thermal equilibrium when $kT > m_\chi c^2$
- Once $kT < m_\chi c^2$, no more χ created
- if stable, only way to lose them is annihilation
- but universe expands and χ get dilute
- at some point they can't find each other
- their number in comoving volume "frozen"



Freeze-out

- WIMP freezes out when the annihilation rate drops below the expansion rate
- Yield $Y=n/s$ constant under expansion
- stronger annihilation \Rightarrow less abundance

$$H \approx g_*^{1/2} \frac{T^2}{M_{Pl}}$$

$$\Gamma_{\text{ann}} \approx \langle \sigma_{\text{ann}} v \rangle n$$

$$H(T_f) = \Gamma_{\text{ann}}$$

$$n \approx g_*^{1/2} \frac{T_f^2}{M_{Pl} \langle \sigma_{\text{ann}} v \rangle}$$

$$s \approx g_* T^3$$

$$Y = \frac{n}{s} \approx g_*^{-1/2} \frac{1}{M_{Pl} T_f \langle \sigma_{\text{ann}} v \rangle}$$

$$\Omega_\chi = \frac{m_\chi Y s_0}{\rho_c}$$

$$\approx g_*^{-1/2} \frac{x_f}{M_{Pl}^3 \langle \sigma_{\text{ann}} v \rangle} \frac{s_0}{H_0^2}$$

Order of magnitude

- “Known” $\Omega_\chi=0.23$ determines the WIMP annihilation cross section
- simple estimate of the annihilation cross section
- within the range at LHC!!!

$$\Omega_\chi \approx g_*^{-1/2} \frac{x_f}{M_{Pl}^3 \langle \sigma_{\text{ann}} v \rangle} \frac{s_0}{H_0^2}$$

$$\langle \sigma_{\text{ann}} v \rangle \approx \frac{1.12 \times 10^{-10} \text{GeV}^{-2} x_f}{g_*^{1/2} \Omega_\chi h^2}$$

$$\sim 10^{-9} \text{GeV}^{-2}$$

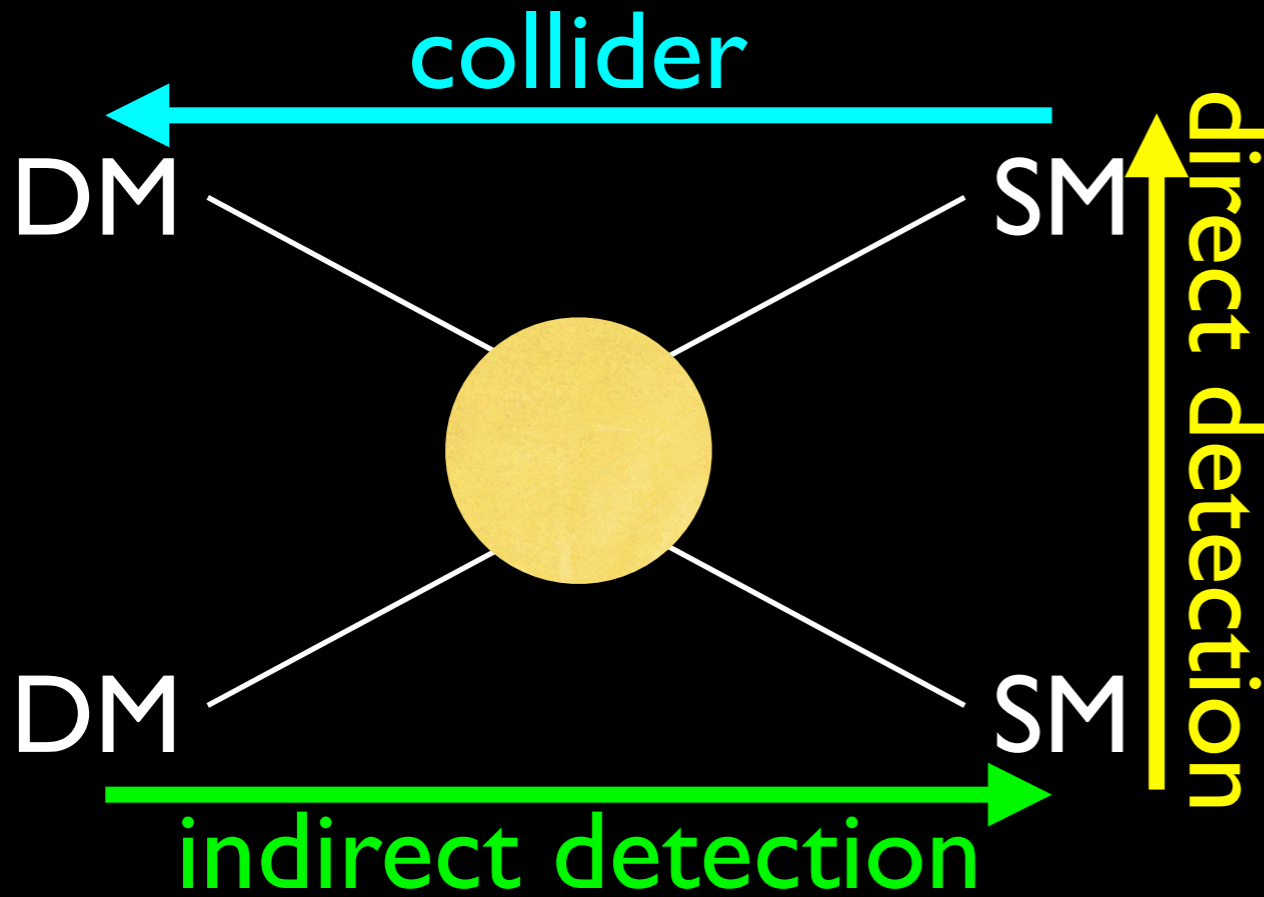
$$\langle \sigma_{\text{ann}} v \rangle \approx \frac{\pi \alpha^2}{m_\chi^2}$$

$$m_\chi \approx 300 \text{ GeV}$$



$$\frac{n_{DM}}{s} = 4.4 \times 10^{-10} \frac{GeV}{m_{DM}}$$

WIMP Miracle

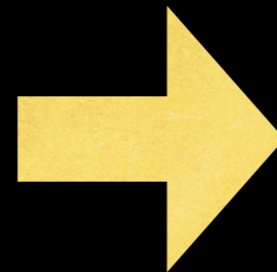


$$\langle \sigma_{2 \rightarrow 2\nu} \rangle \approx \frac{\alpha^2}{m^2}$$

$$\alpha \approx 10^{-2}$$

$$m \approx 300 \text{ GeV}$$

“weak” coupling
“weak” mass scale

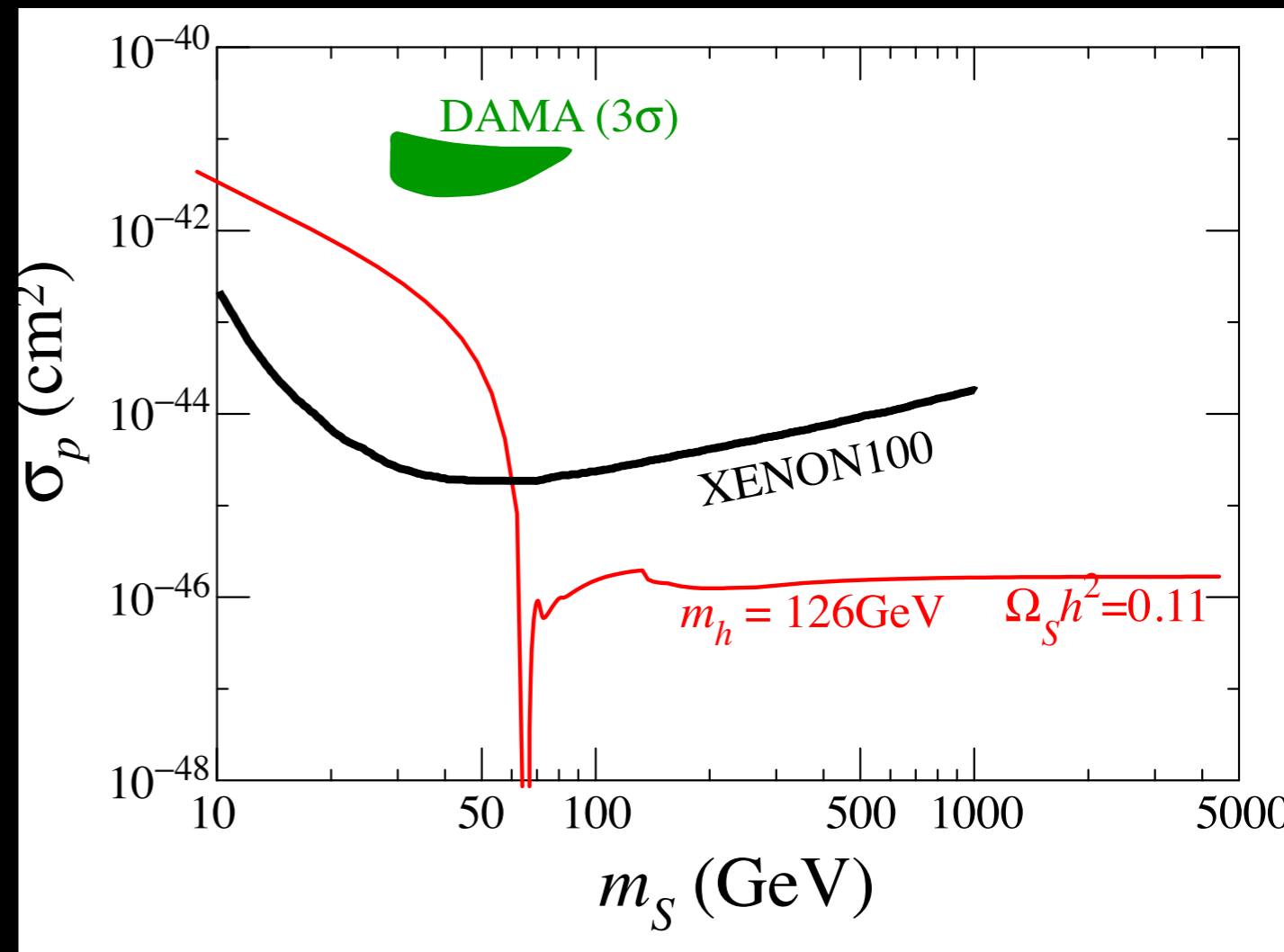


correct abundance

We want new particles for naturalness anyway
Miracle²

Littlest Dark Matter

- dark matter clearly a new degree of freedom
- The smallest dof you can add to the SM is a real Klein-Gordon field S :
dof=1
- assign odd Z_2 parity to S , everything else even



$$L_S = \frac{1}{2} \partial_\mu S \partial^\mu S - \frac{1}{2} m_S^2 S^2 - \frac{k}{2} |H|^2 S^2 - \frac{h}{4!} S^4.$$

Electron mass is natural by doubling #particles

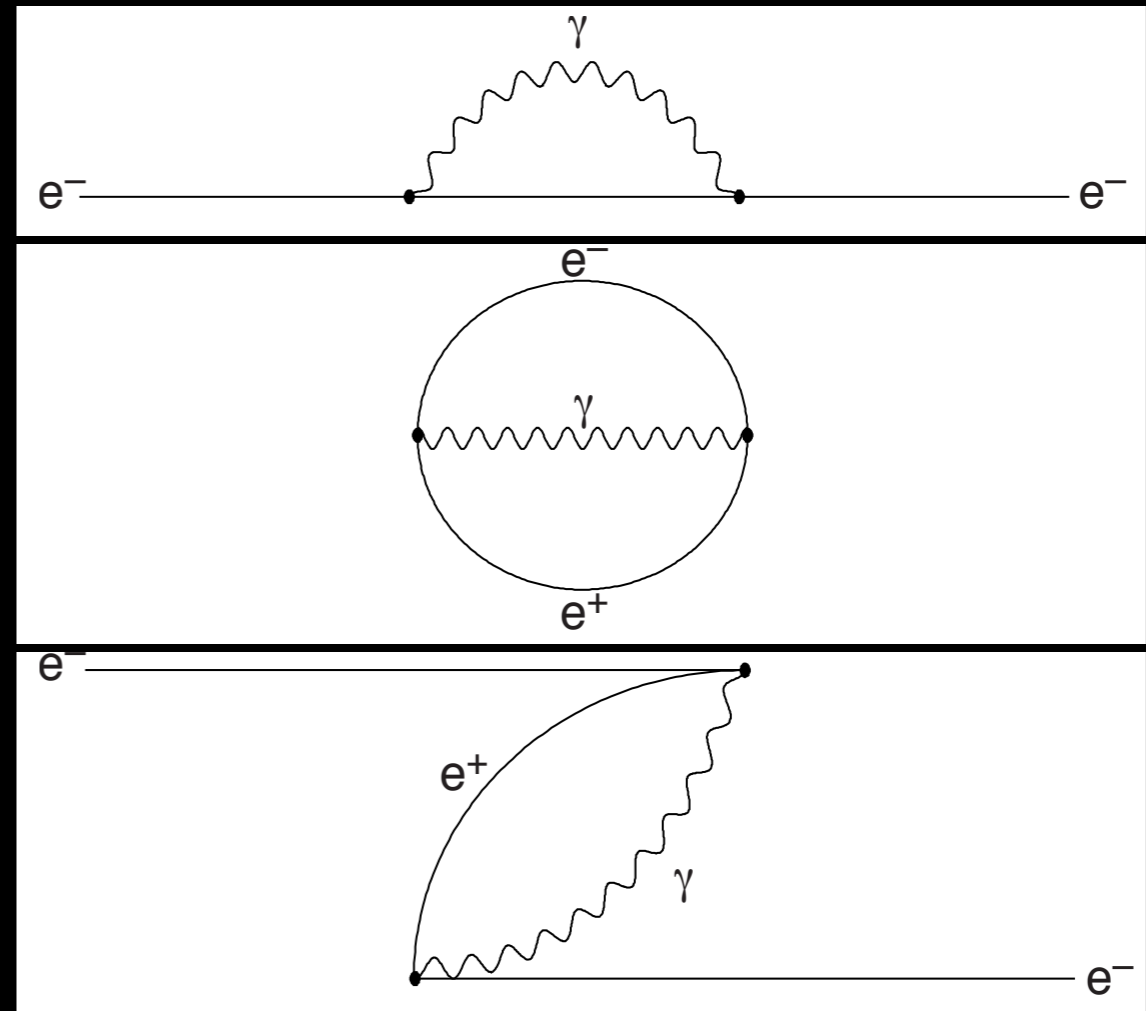
- Electron creates a force to repel itself

$$\Delta m_e c^2 \sim \frac{e^2}{r_e} \sim \text{GeV} \frac{10^{-17} \text{cm}}{r_e}$$

- quantum mechanics and anti-matter

⇒ only 10% of mass even

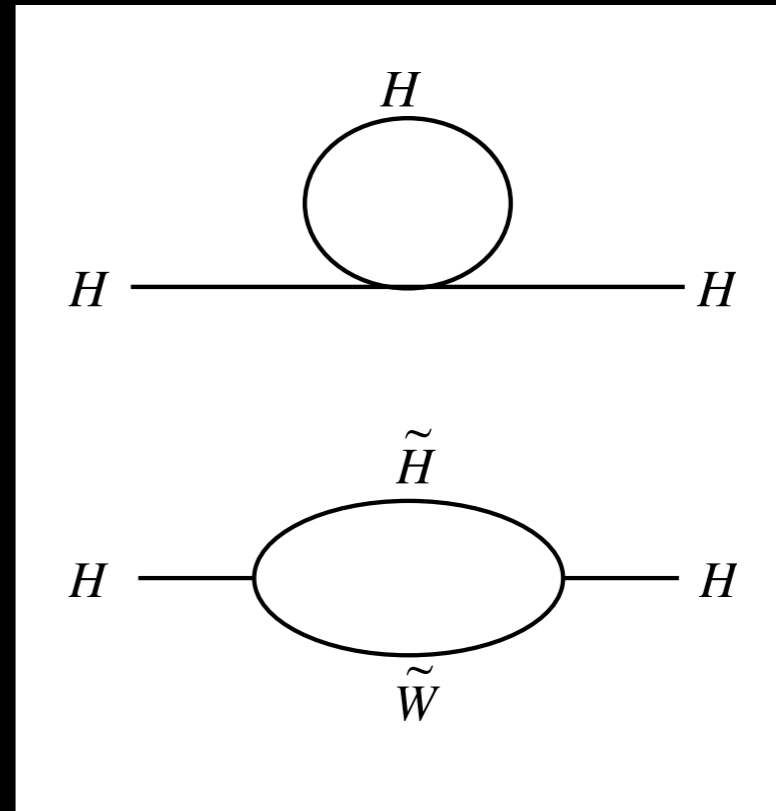
for Planck-size $r_e \sim 10^{-33} \text{cm}$



$$\Delta m_e \sim m_e \frac{\alpha}{4\pi} \log(m_e r_e)$$

Higgs mass is natural by doubling #particles?

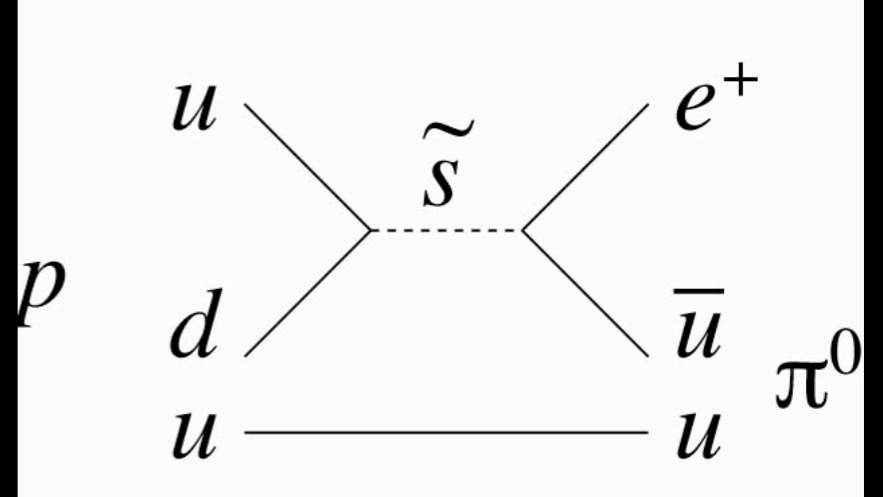
- Higgs also repels itself
- Double #particles again
⇒ superpartners
- only log sensitivity to UV
- Standard Model made
consistent up to higher
energies



$$\Delta m_H^2 \sim \frac{\alpha}{4\pi} m_{SUSY}^2 \log(m_H r_H)$$

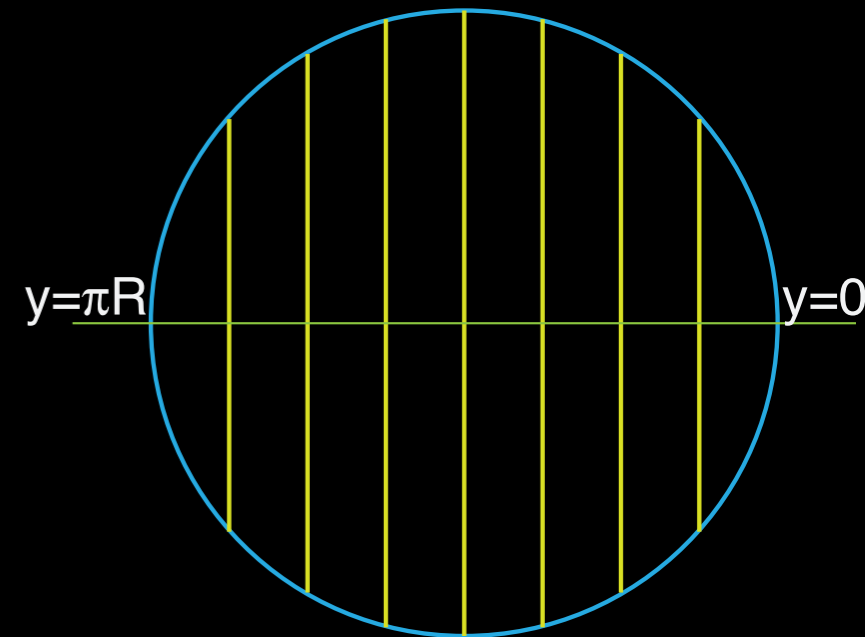
➔ I still take it seriously

R-parity

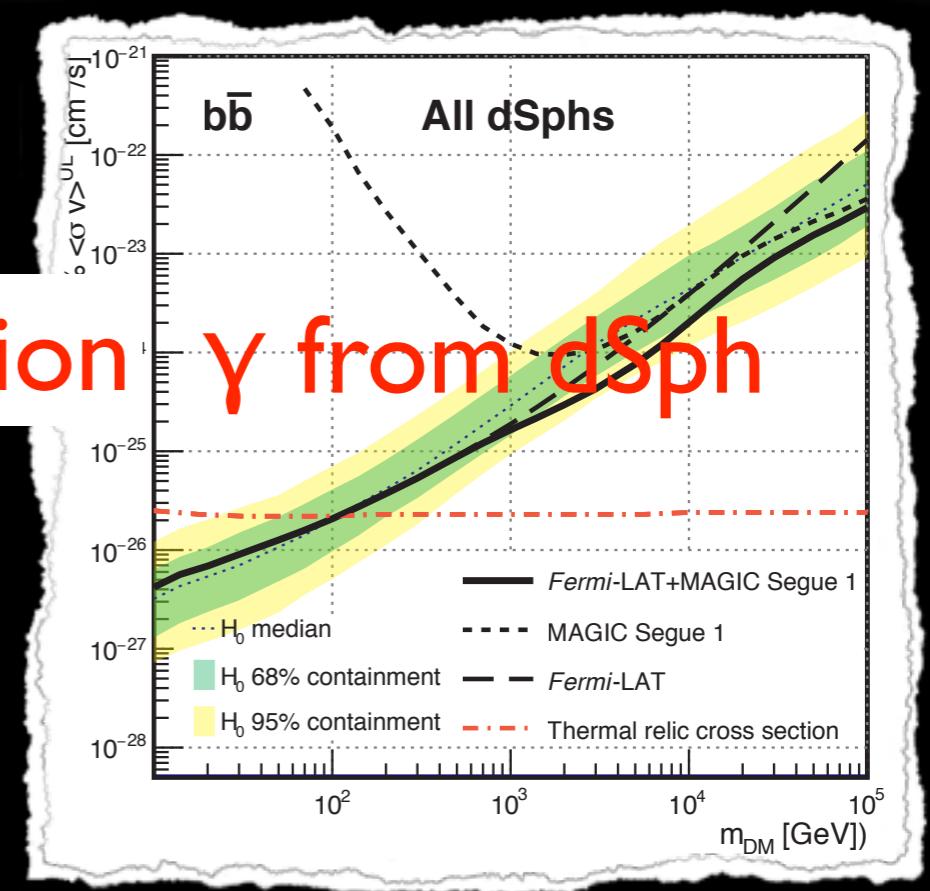
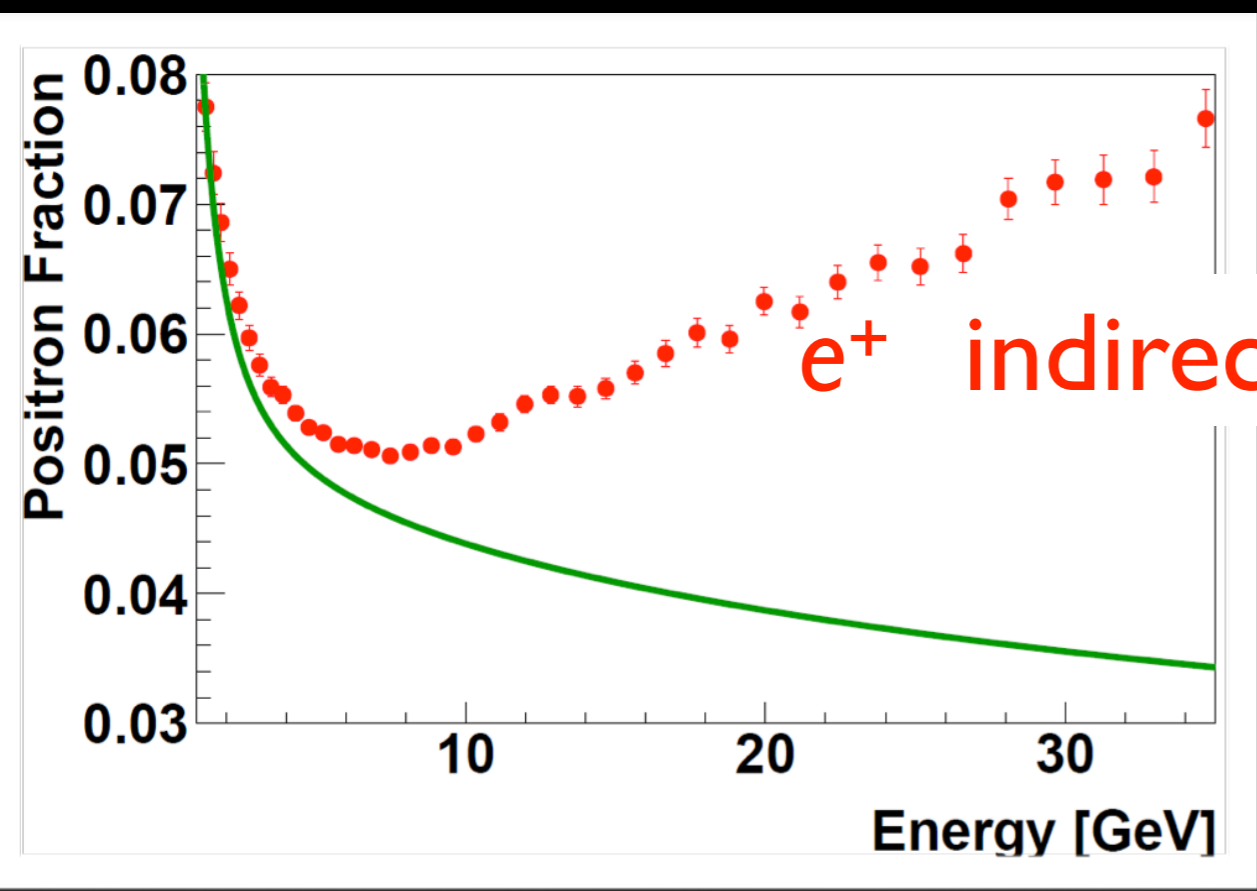
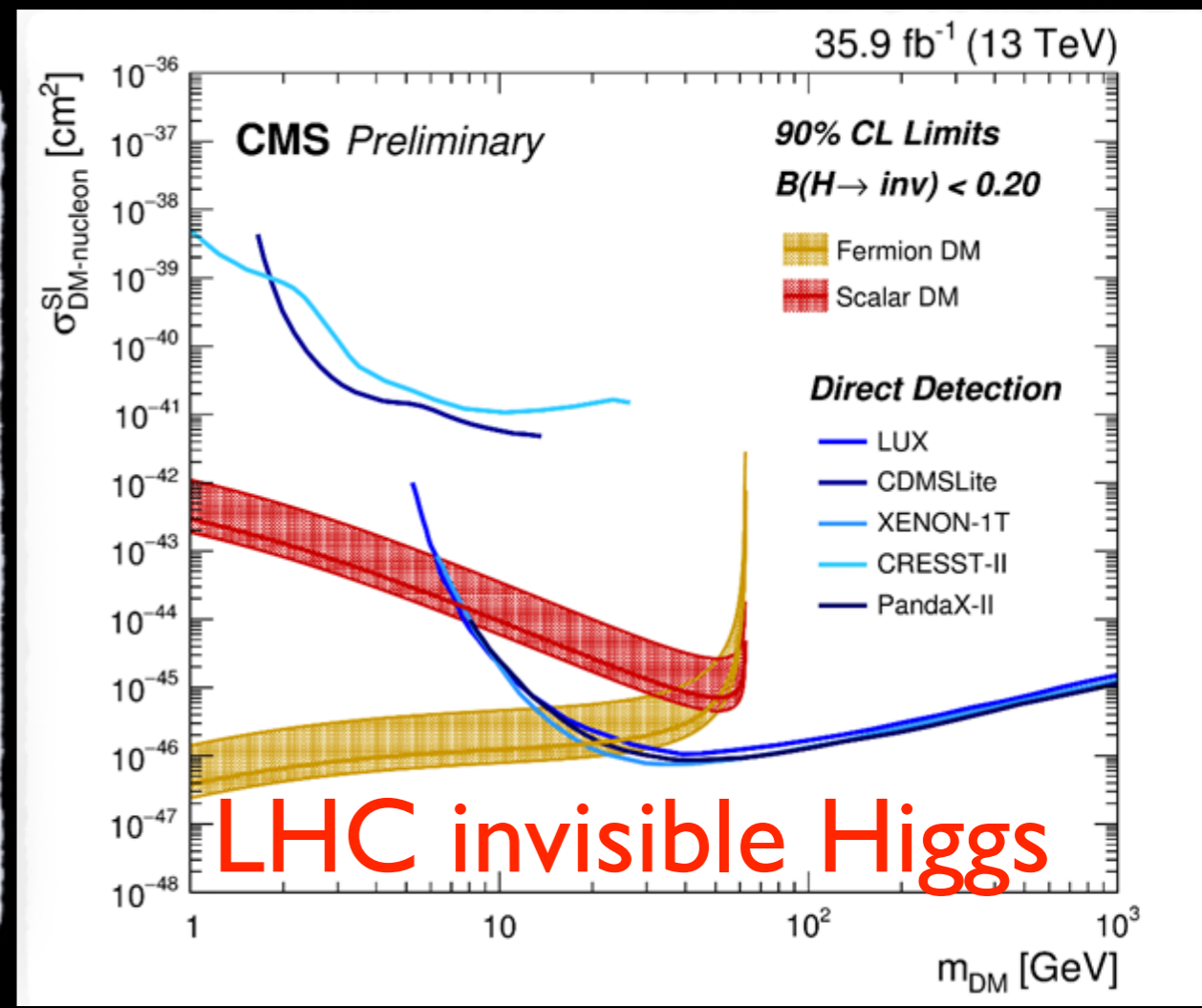
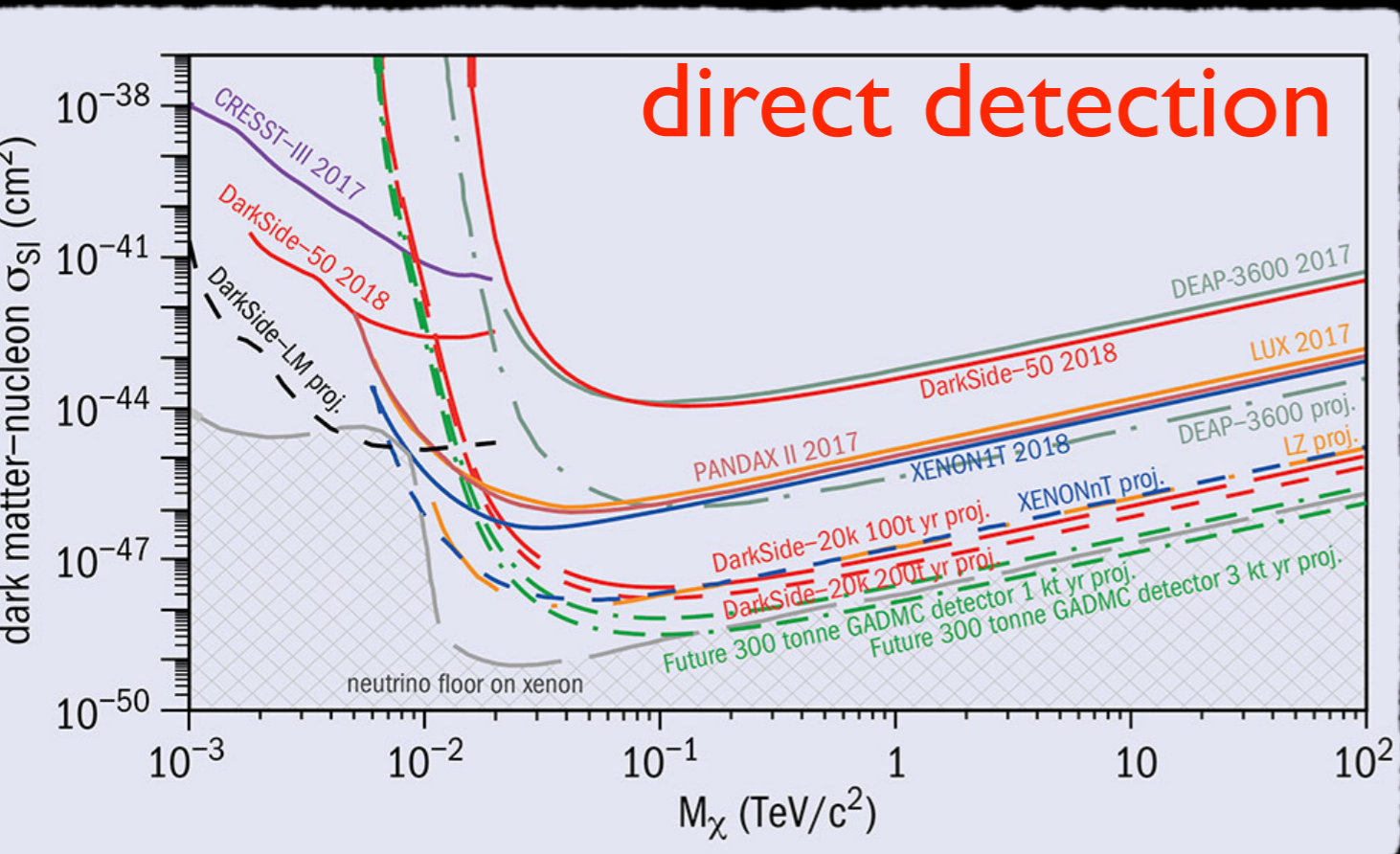


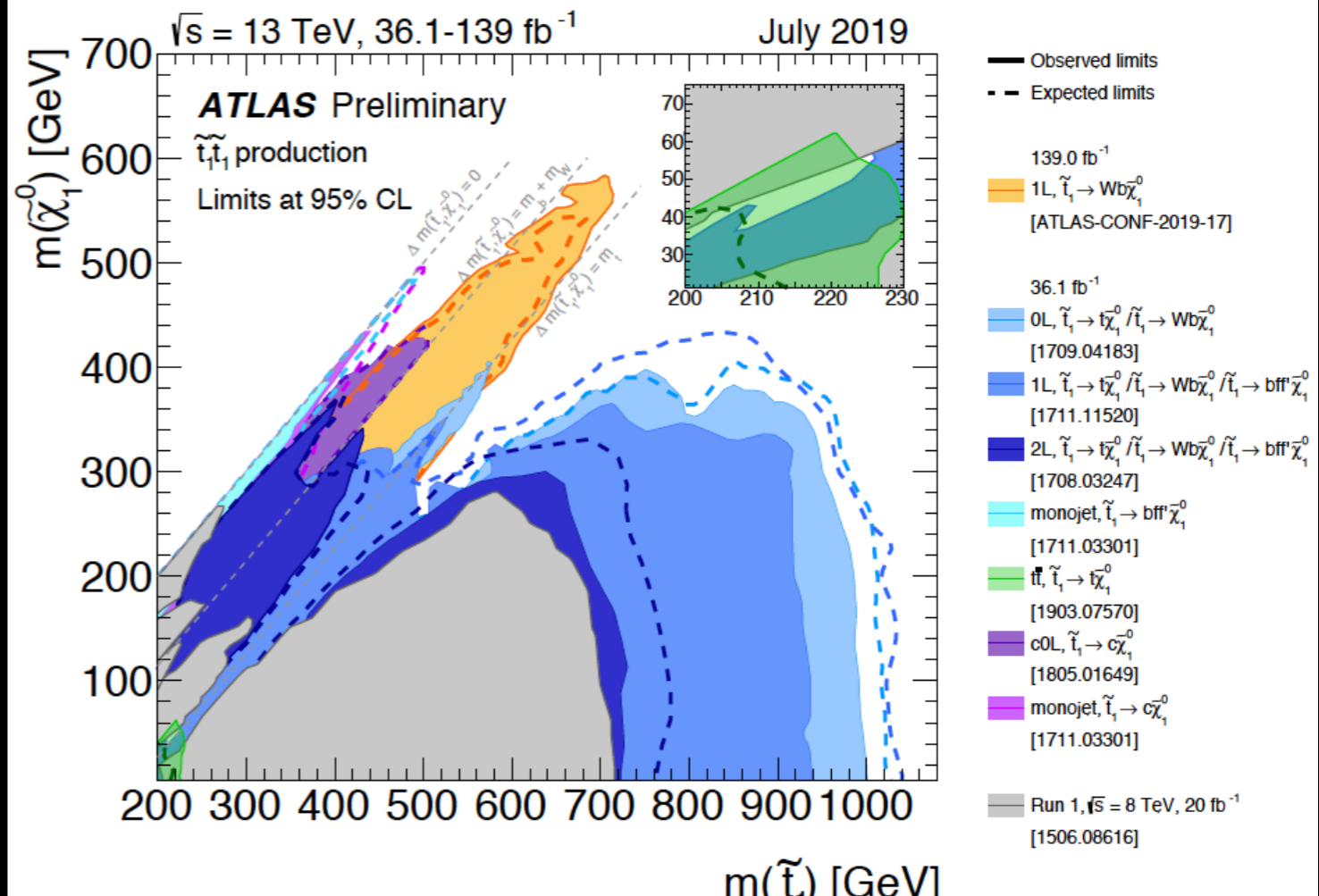
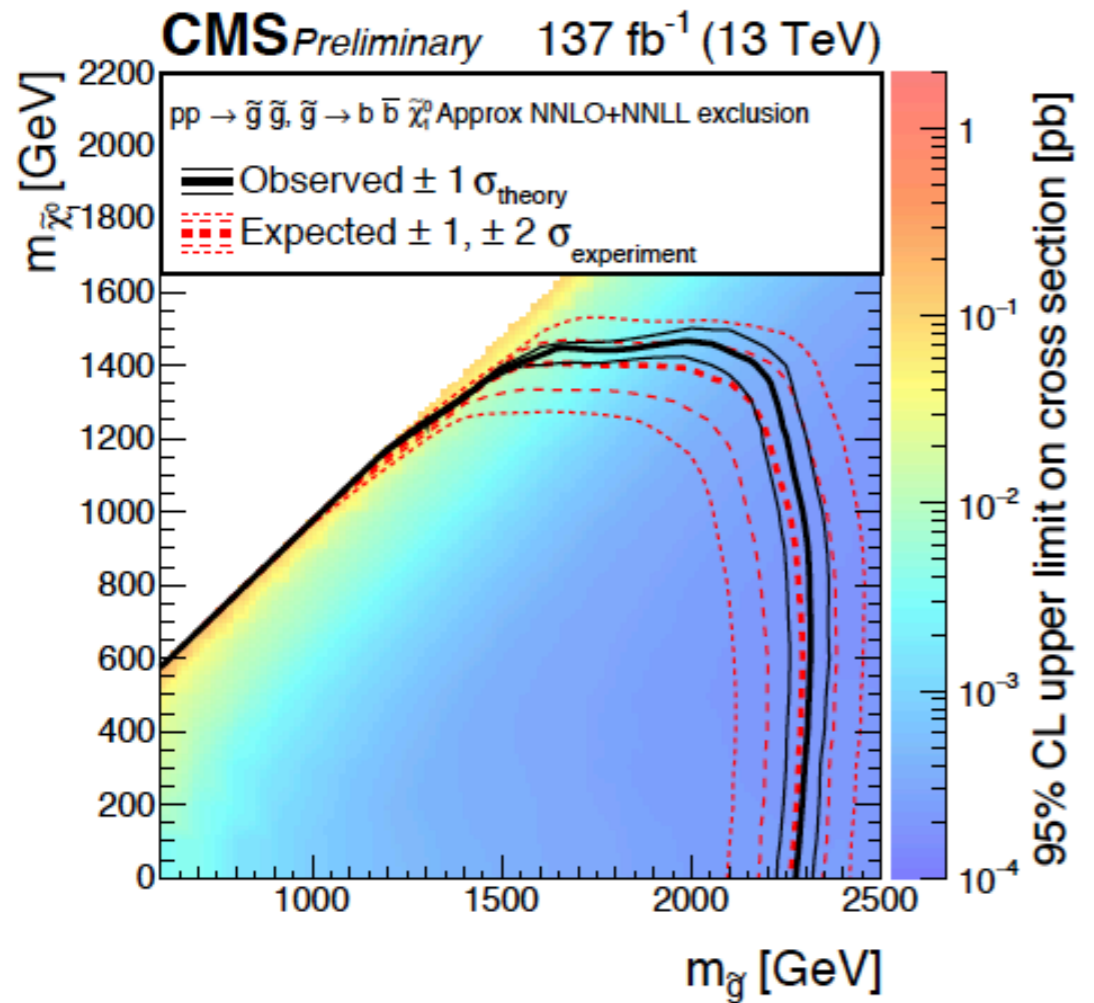
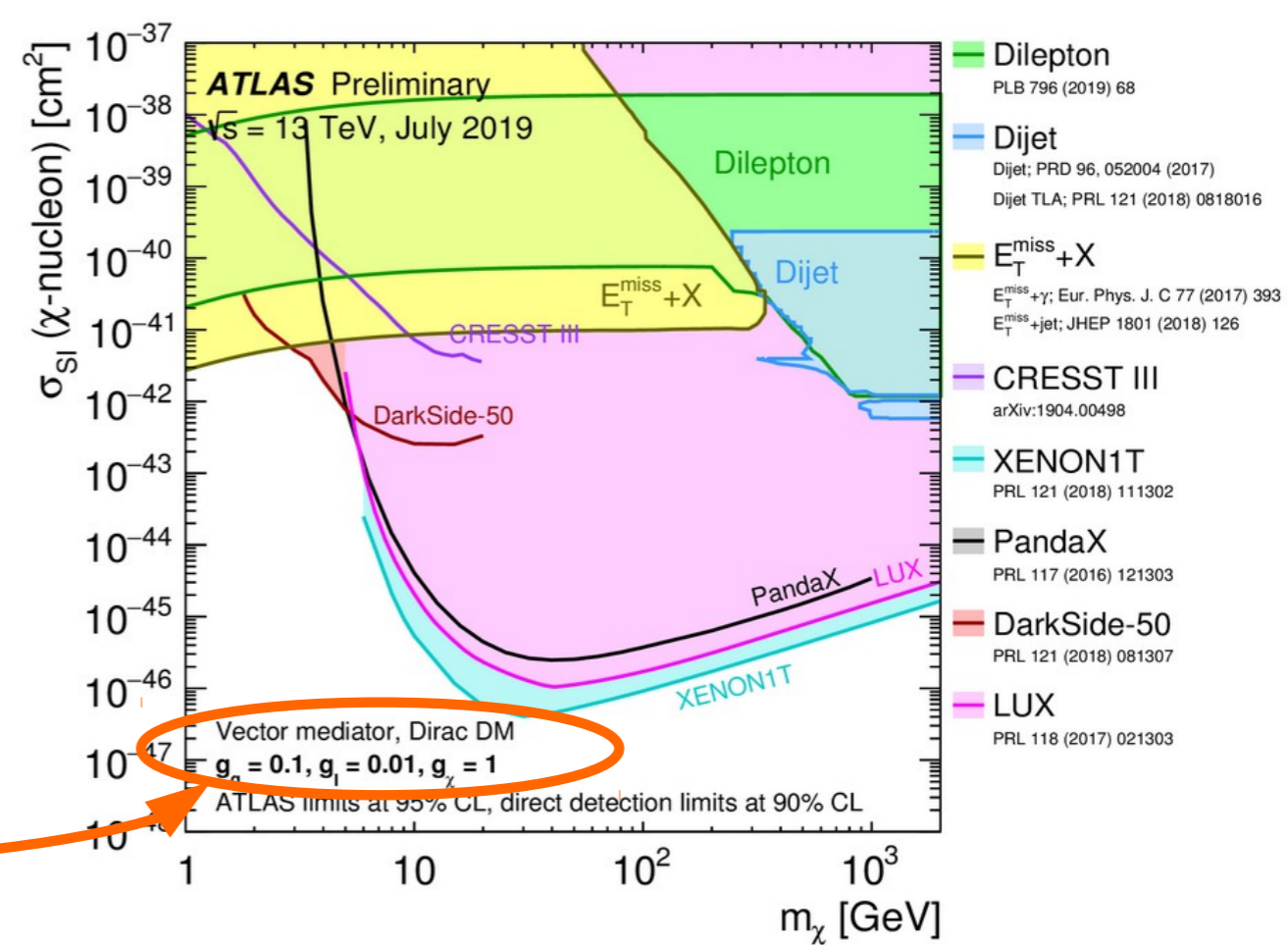
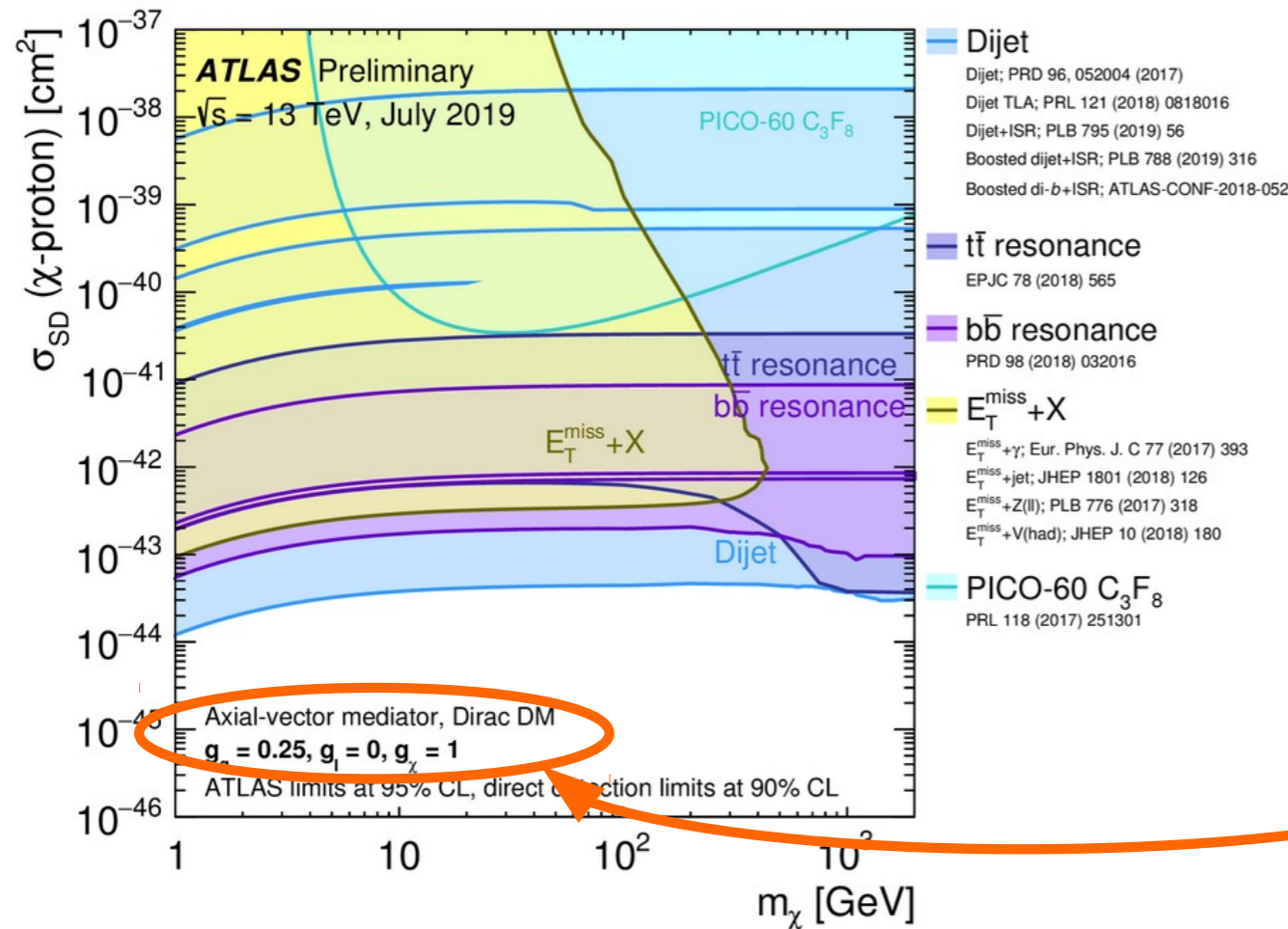
- B, L -conservation not automatic
- $W = udd + QdL + LLe + LH_u$
- If they exist with $O(1)$ couplings:
- $\tau_p \sim m_{sq}^4 / m_p^5 \sim 10^{-12}$ sec!
- Product of two couplings $< 10^{-26}$
- Impose R -parity = $(-1)^{3B+L+2s}$
- Forbids B and L number violation
- R -parity is non-anomalous; may be gauged
- Stable Lightest Supersymmetric Particle
⇒ Cold Dark Matter
- SUSY particles always pair-produced and decay into the LSP: missing energy signal

UED



- one extra dimension (S^1/Z_2)
 - mod out by parity in 5D
- Lightest state with odd parity is stable
- typically KK state of $U(1)Y$ gauge boson





Galactic center

Daylan et al, arXiv:1402.6703

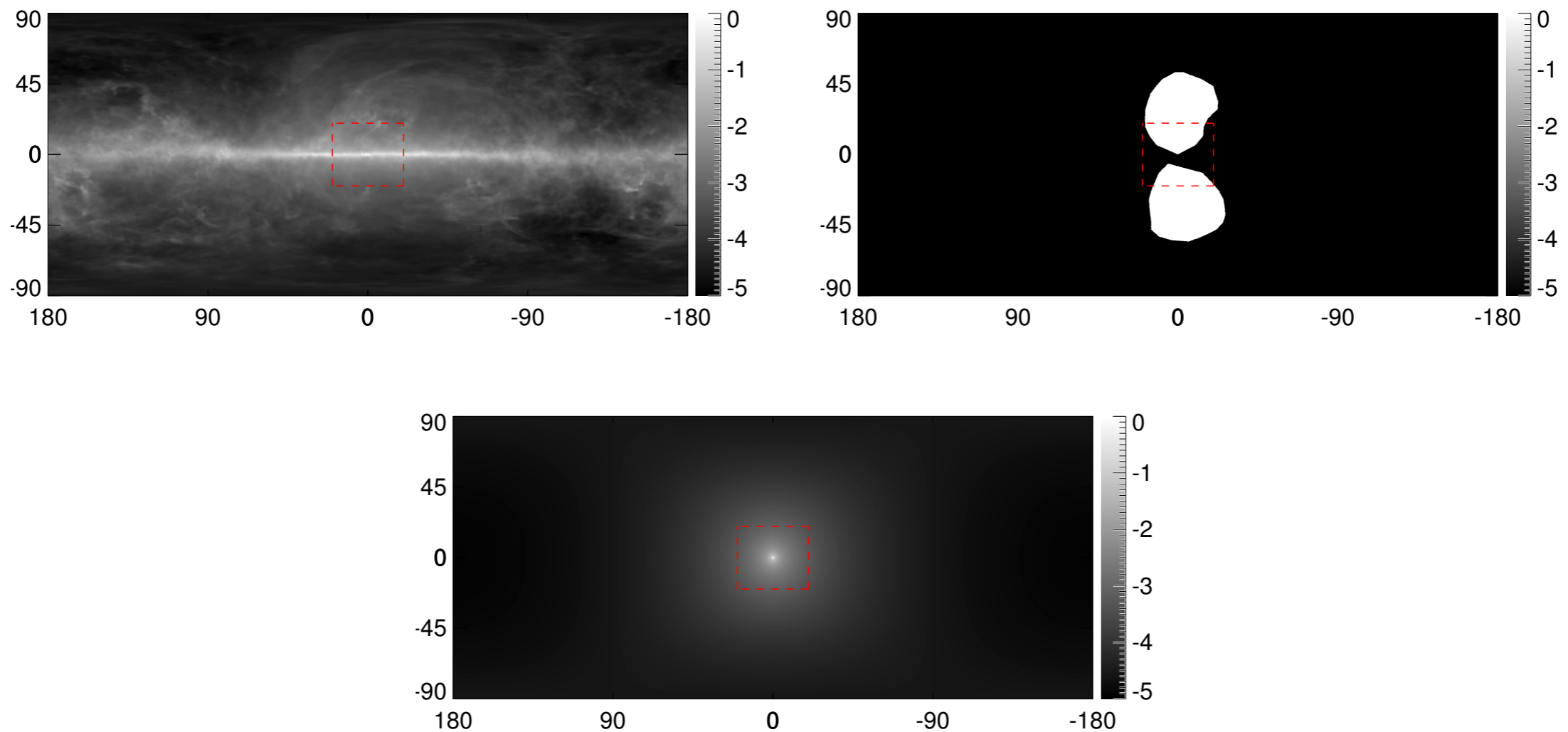
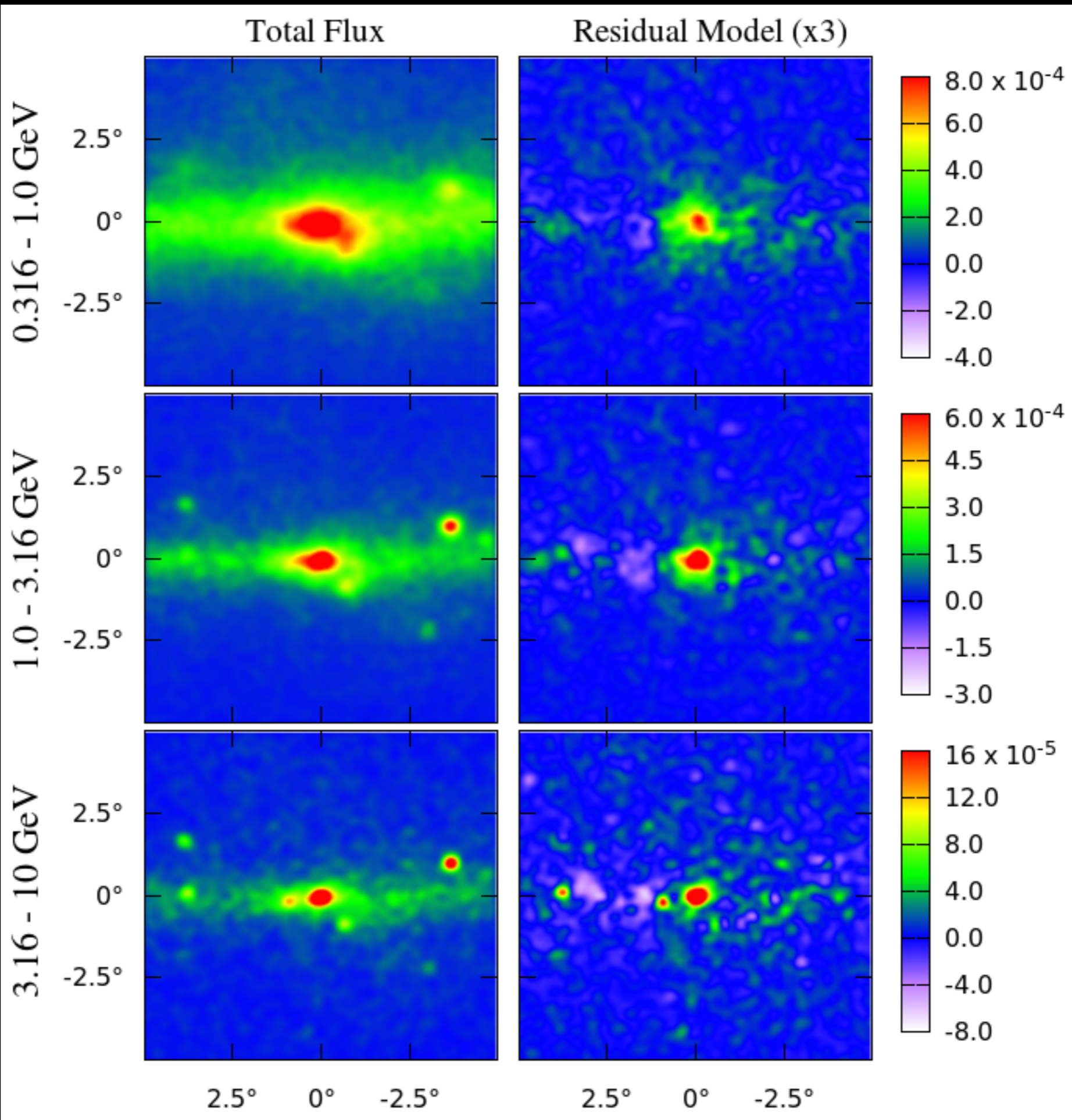


FIG. 4: The spatial templates (in galactic coordinates) for the Galactic diffuse model (upper left), the *Fermi* bubbles (upper right), and dark matter annihilation products (lower), as used in our Inner Galaxy analysis. The scale is logarithmic (base 10), normalized to the brightest point in each map. The diffuse model template is shown as evaluated at 1 GeV, and the dark matter template corresponds to a generalized NFW profile with an inner slope of $\gamma = 1.18$. Red dashed lines indicate the boundaries of our standard Region of Interest (we also mask bright point sources and the region of the Galactic plane with $|b| < 1^\circ$).

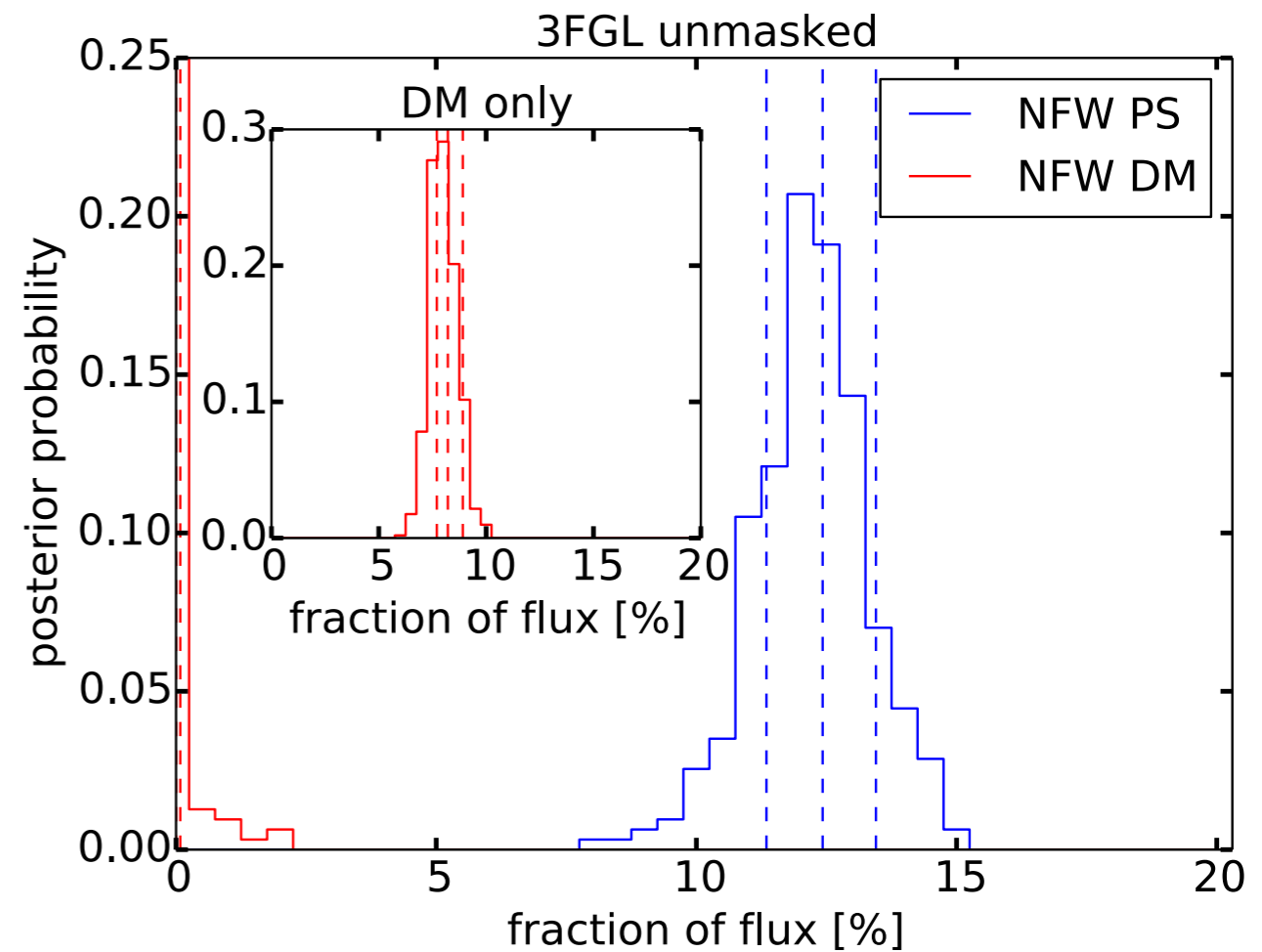
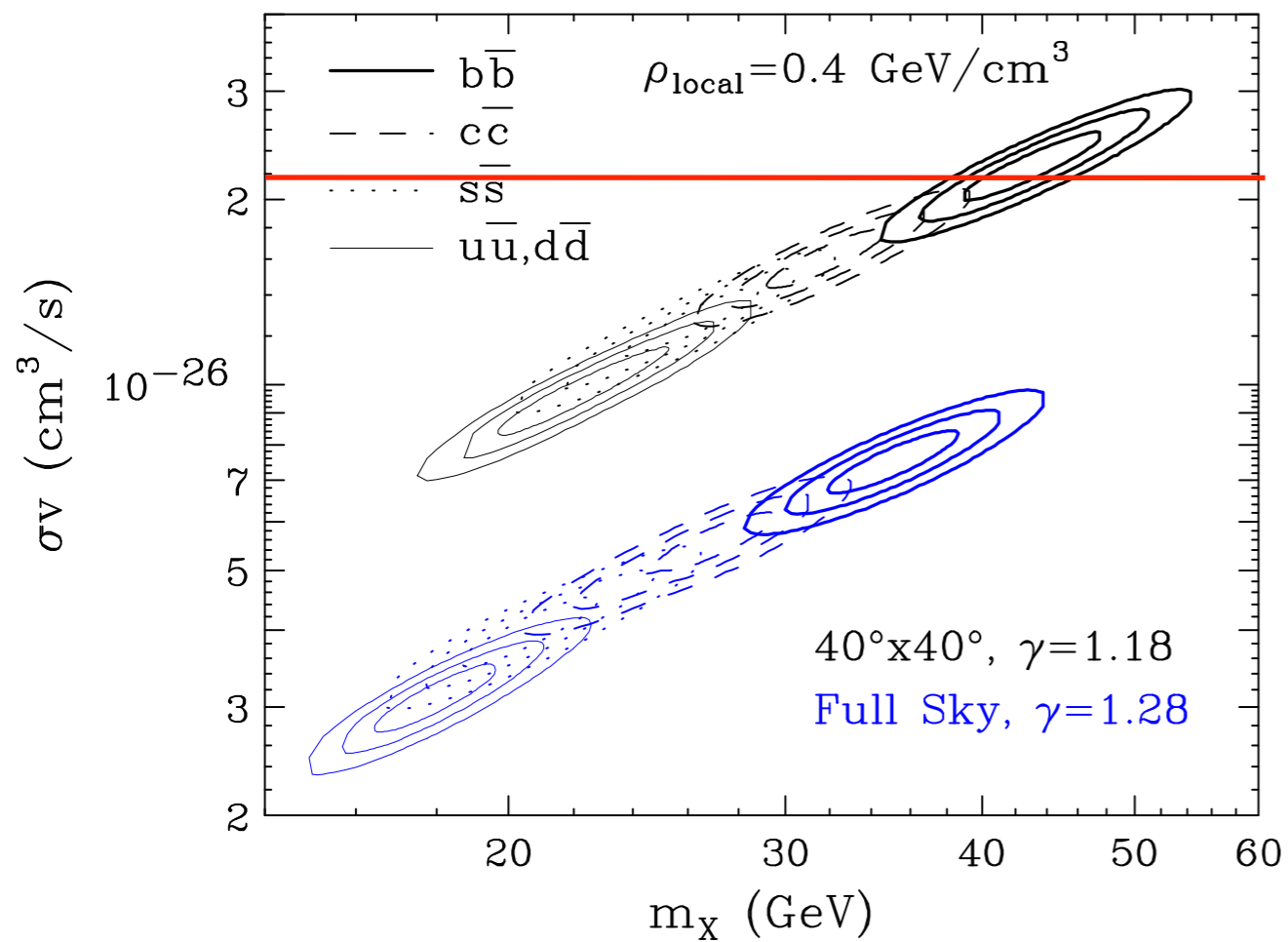


dark matter annihilation?

Daylan et al, arXiv:1402.6703

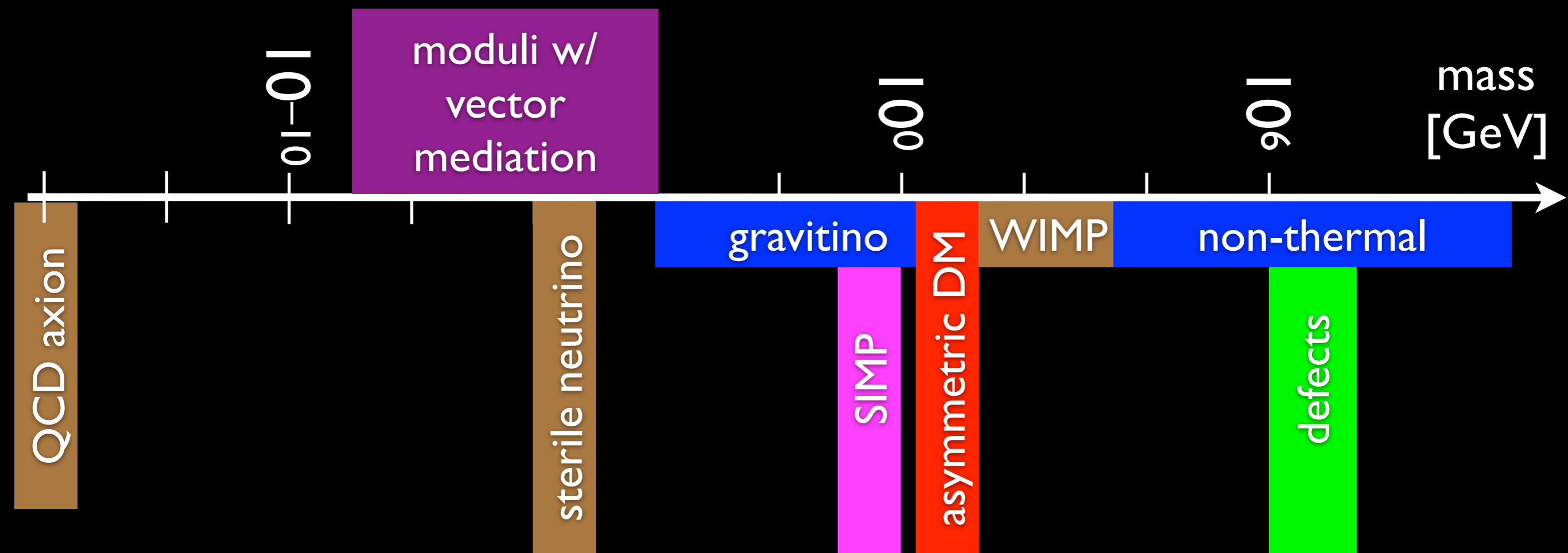
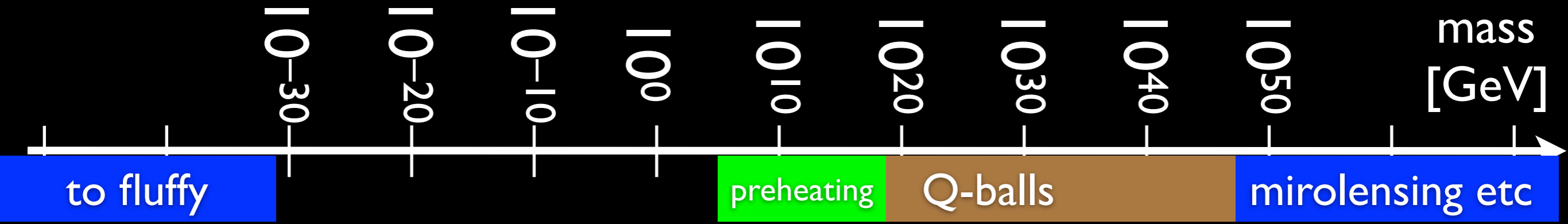
or unresolved point sources?

S. Lett et al, arXiv:1506.05124v1

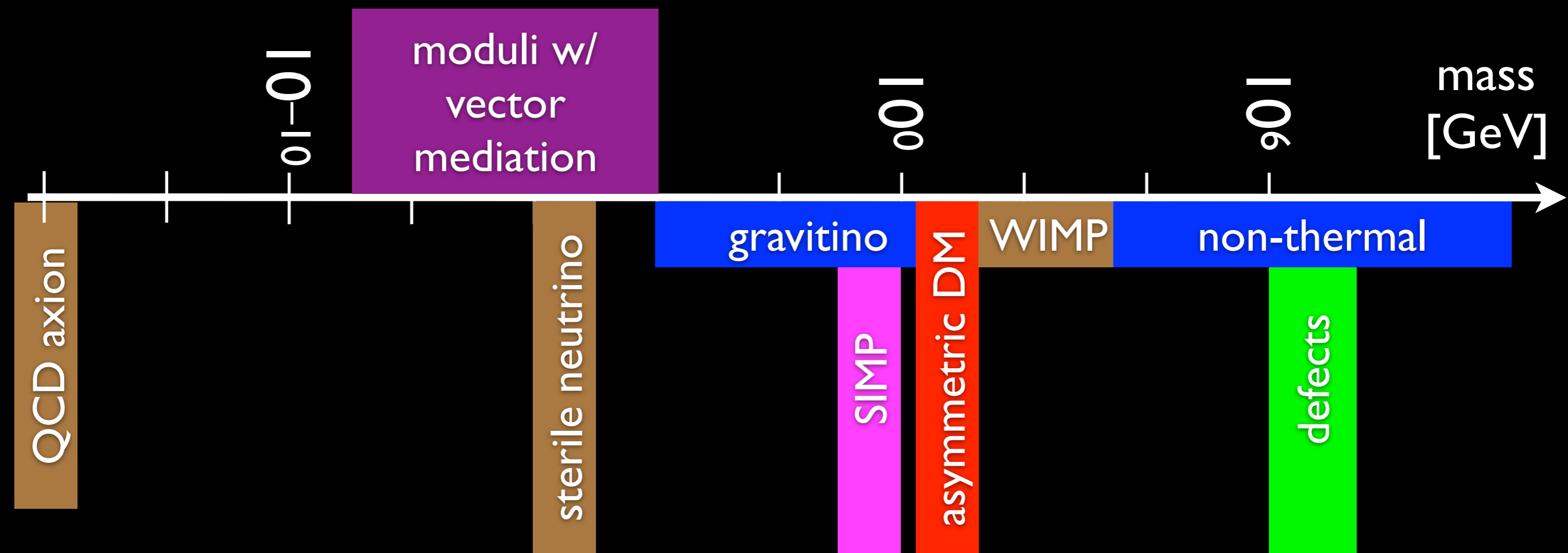
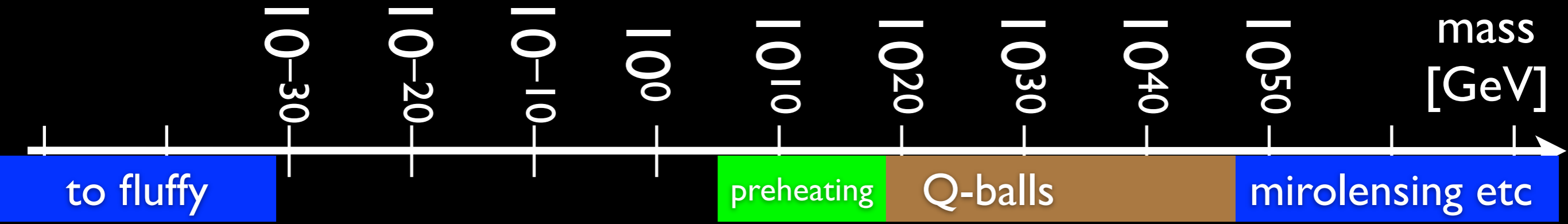


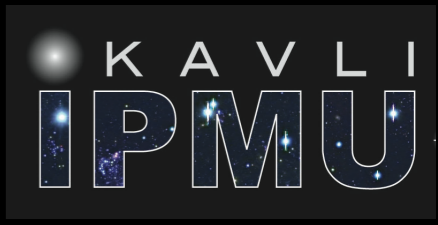
new sociology

- WIMP should be explored at least down to the **neutrino floor**
 - heavier? e.g., wino @ 3TeV \Rightarrow CTA
- dark matter definitely exists
 - hierarchy problem may be optional?
- need to explain dark matter on its own
- perhaps we should decouple these two
- do we really need big ideas like SUSY?
- perhaps not necessarily heavier but rather **lighter and weaker coupling?**



boson ←





After Inflation

1,000,000,001

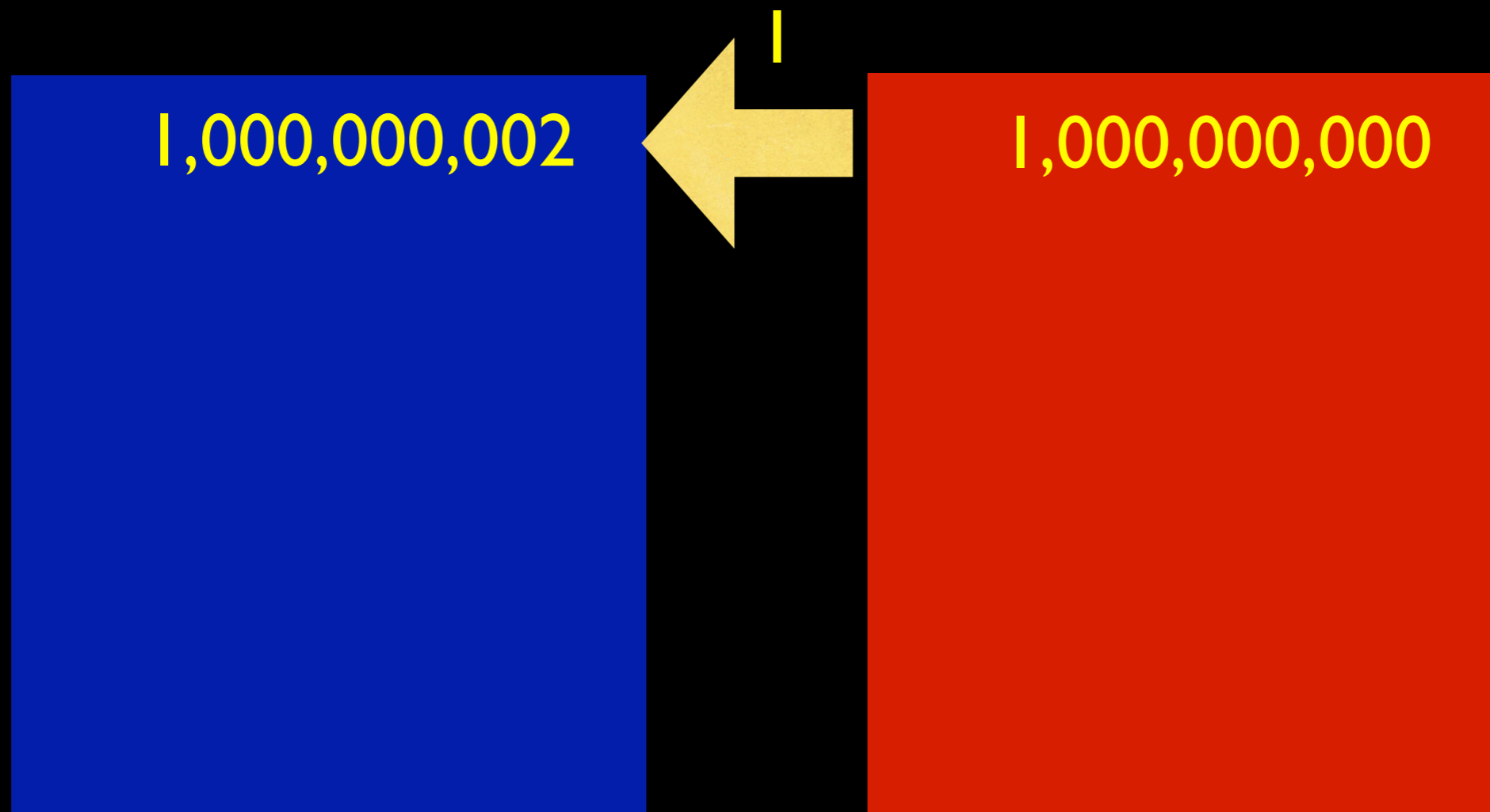
1,000,000,001

matter

anti-matter



fraction of second later



matter

anti-matter

turned a billionth of anti-matter to matter



Universe Now

$$m_{\text{DM}} = \frac{n_b}{n_{\text{DM}}} \frac{\Omega_{\text{DM}}}{\Omega_b} m_p \approx 6 \text{ GeV} \times \frac{\eta_b}{\eta_{\text{DM}}}$$

2
•
us

- motivation for 1–10 GeV dark matter
- challenge: get rid of symmetric component
- signal depends on portal; new medium

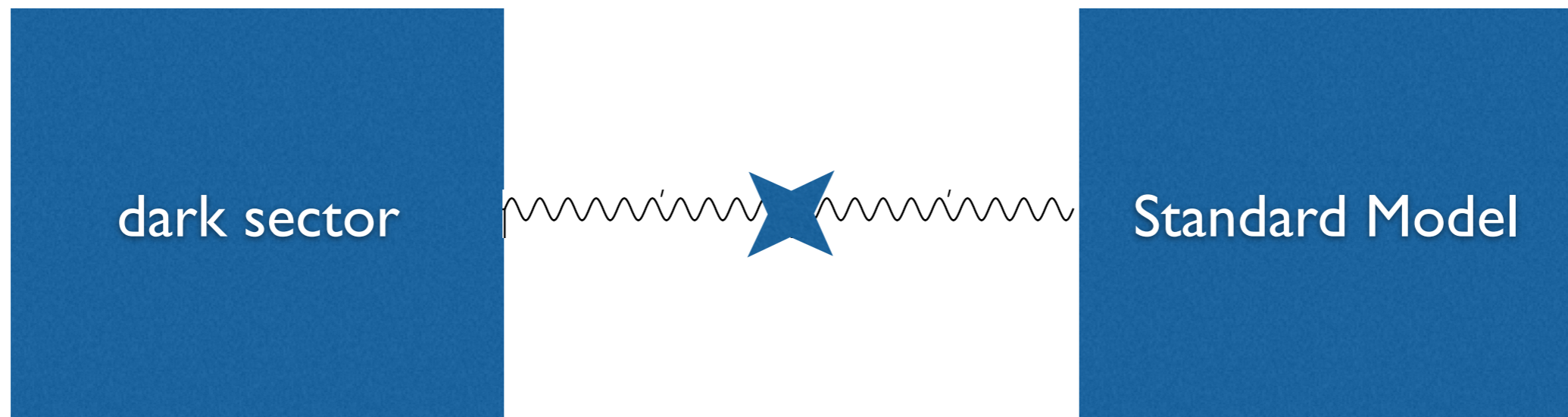
Gelmini, Hall, Lin (1987)

Kaplan, Luty, Zurek, 0901.4117

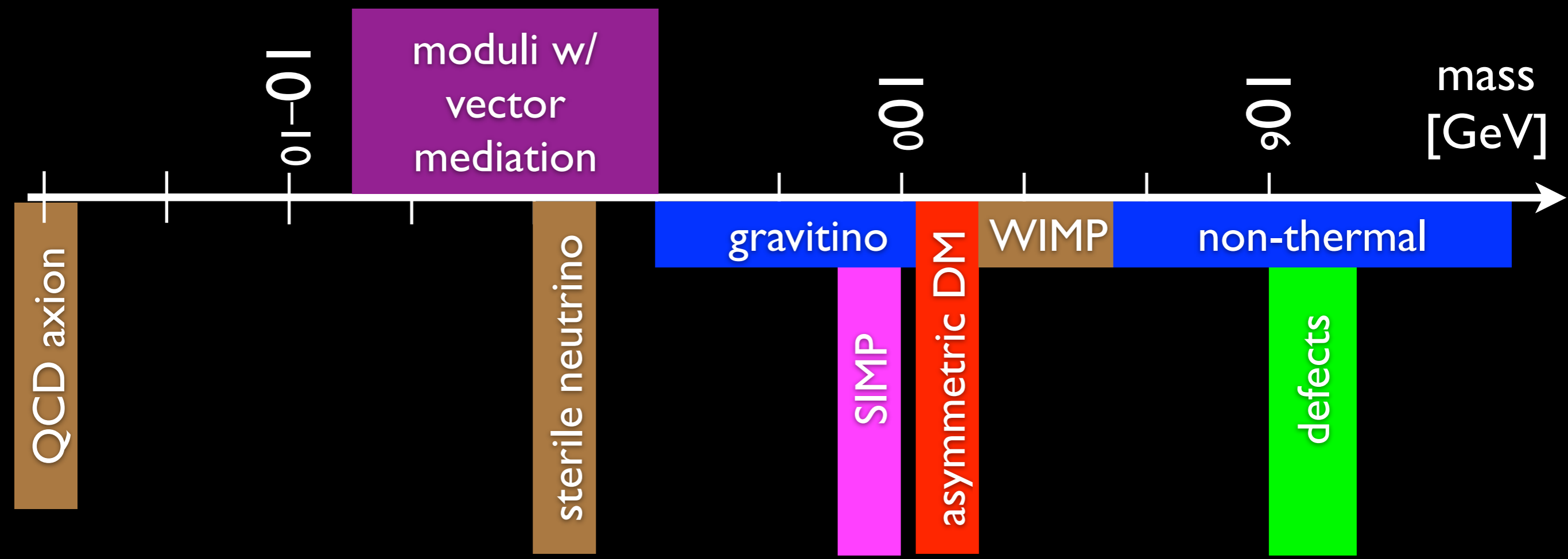
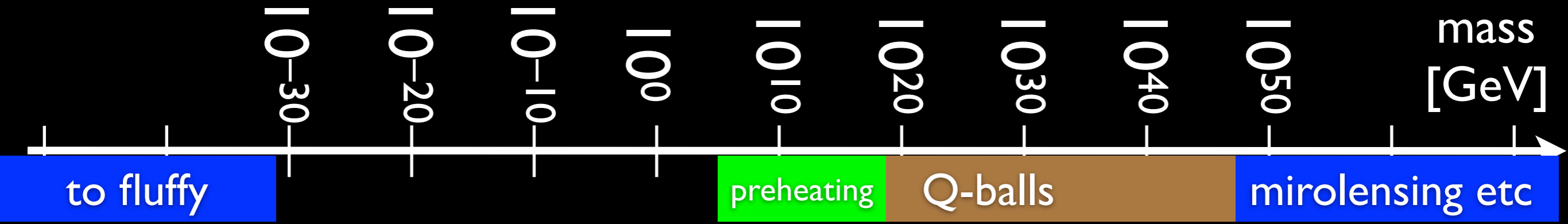
dark matter *dark anti-matter*

This must be how *we* survived the Big Bang!
they

portals



- vector portal $\frac{\epsilon_\gamma}{2c_W} B_{\mu\nu} F_D^{\mu\nu}$ \rightarrow collider, beam dump
- scalar portal $\mu S H^\dagger H, S^2 H^\dagger H$ \rightarrow $H \rightarrow$ invisible, couplings
- neutrino portal $\bar{L} N H$ \rightarrow neutrino exp, dump



neutrino mass too light for dark matter

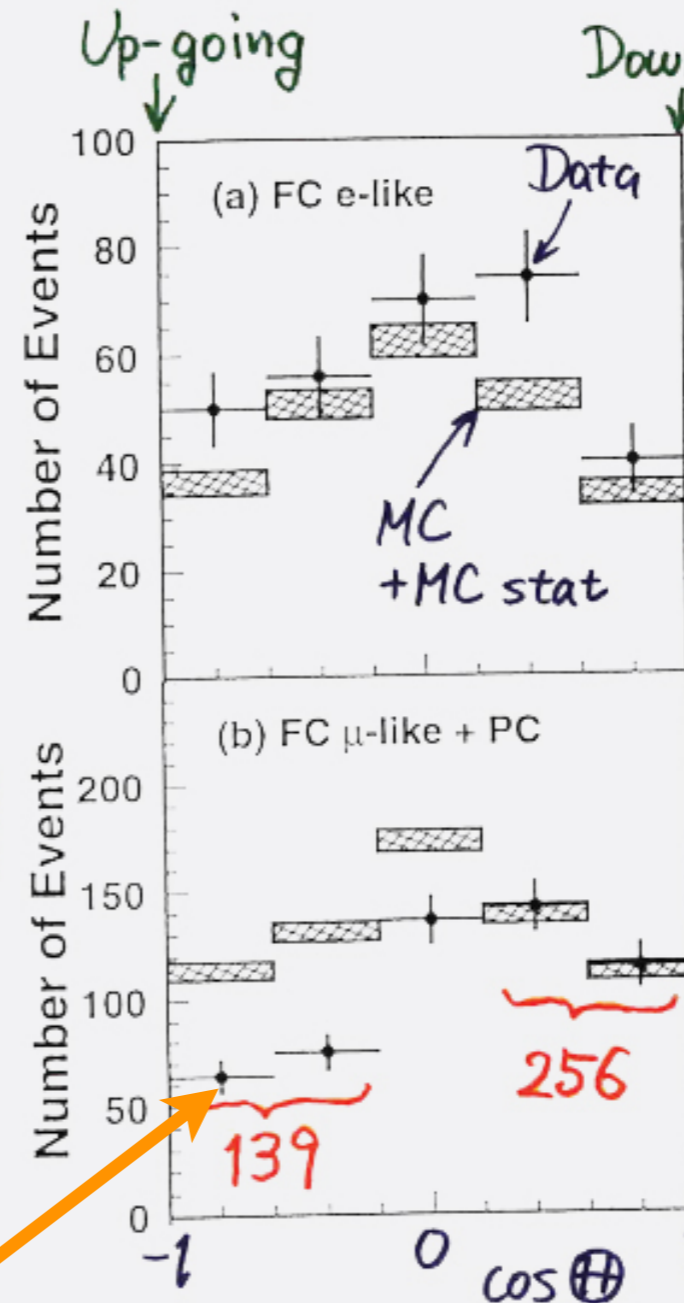


1998

a half of
expected

Zenith angle dependence (Multi-GeV)

(e)



(mu)

$\chi^2(\text{shape}) = 2.8/4 \text{ dof}$

$\frac{\text{Up}}{\text{Down}} = 0.93^{+0.13}_{-0.12}$

$\chi^2(\text{shape}) = 30/4 \text{ dof}$

$\frac{\text{Up}}{\text{Down}} = 0.54^{+0.06}_{-0.05}$

(6.2σ!!)

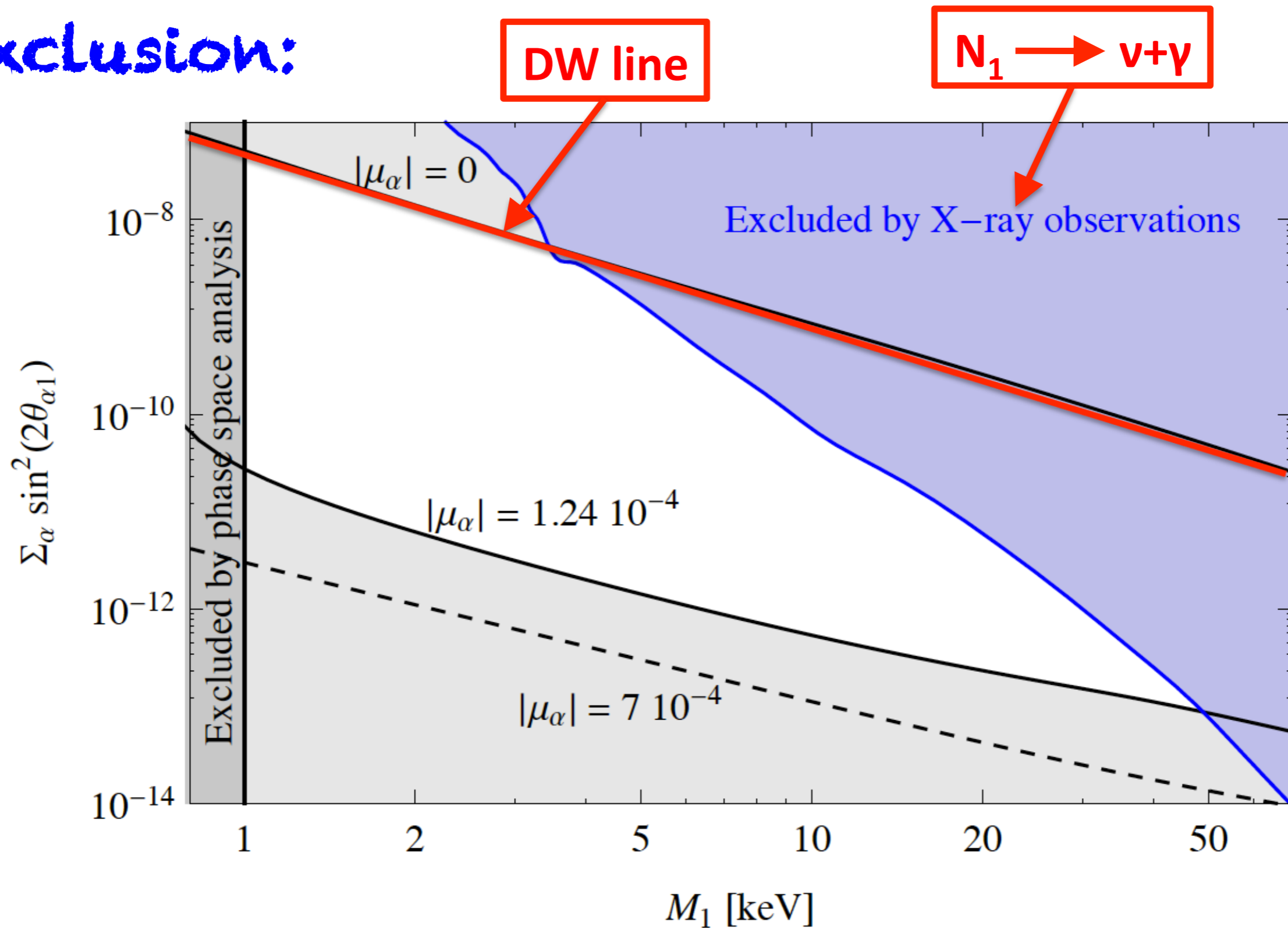
* Up/Down syst. error for μ -like

Prediction (flux calculation $\lesssim 1\%$
1km rock above SK 1.5%) 1.8%

Data (Energy calib. for $\uparrow\downarrow$ 0.7%
Non ν Background < 2%) 2.1%

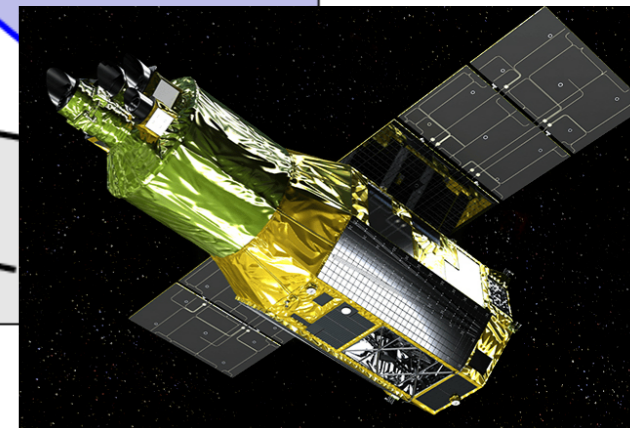
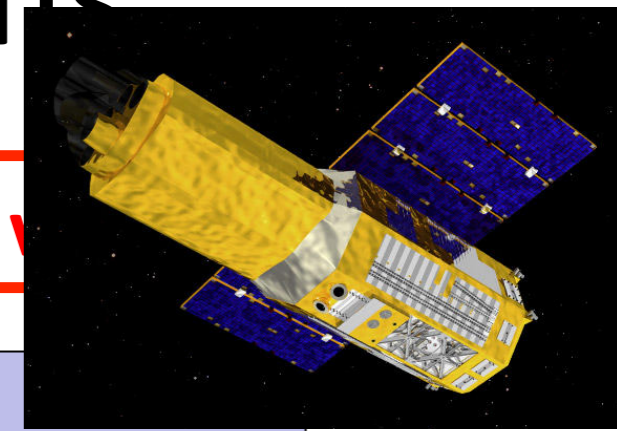
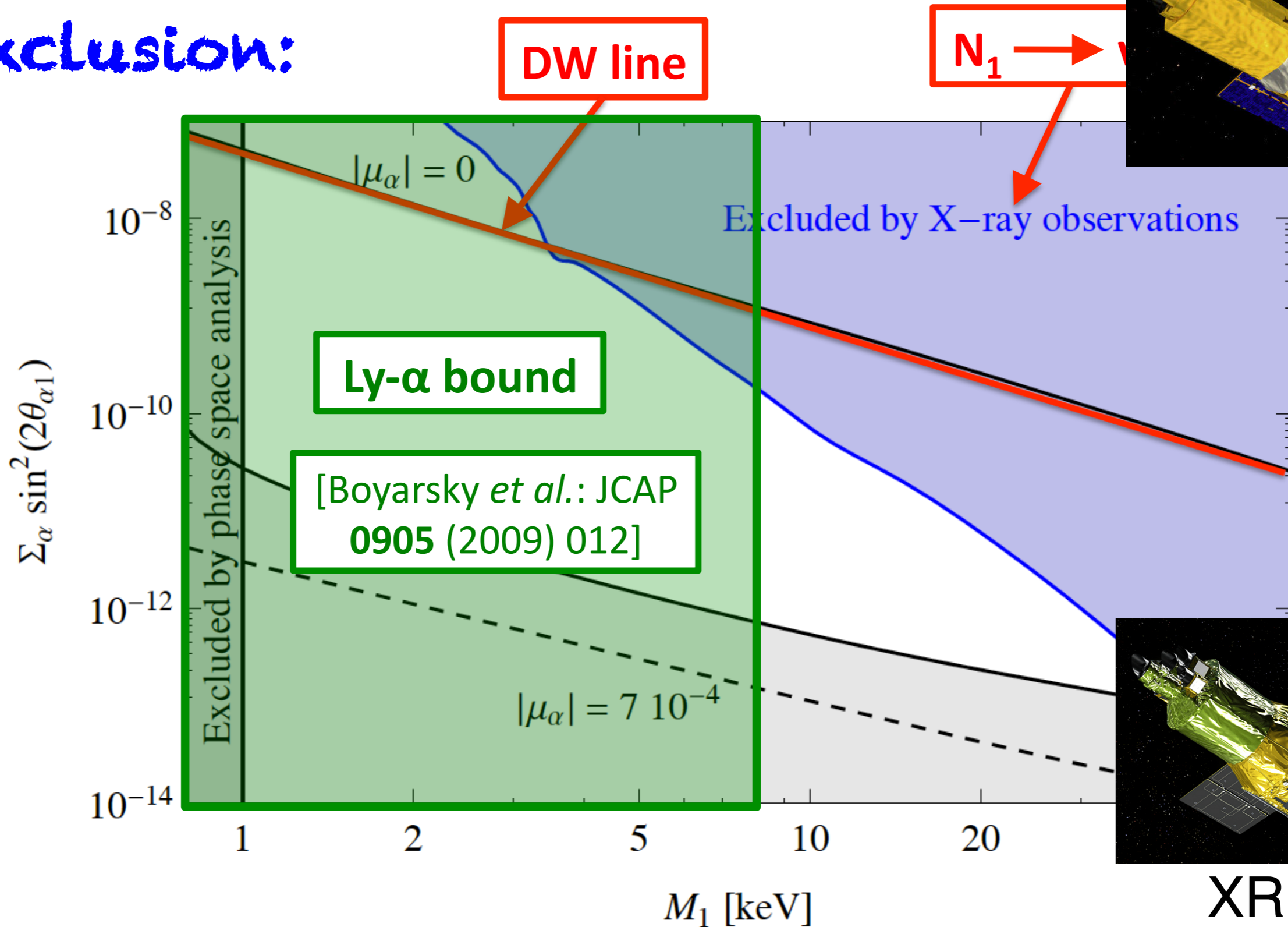
2. Production Mechanisms

Exclusion:

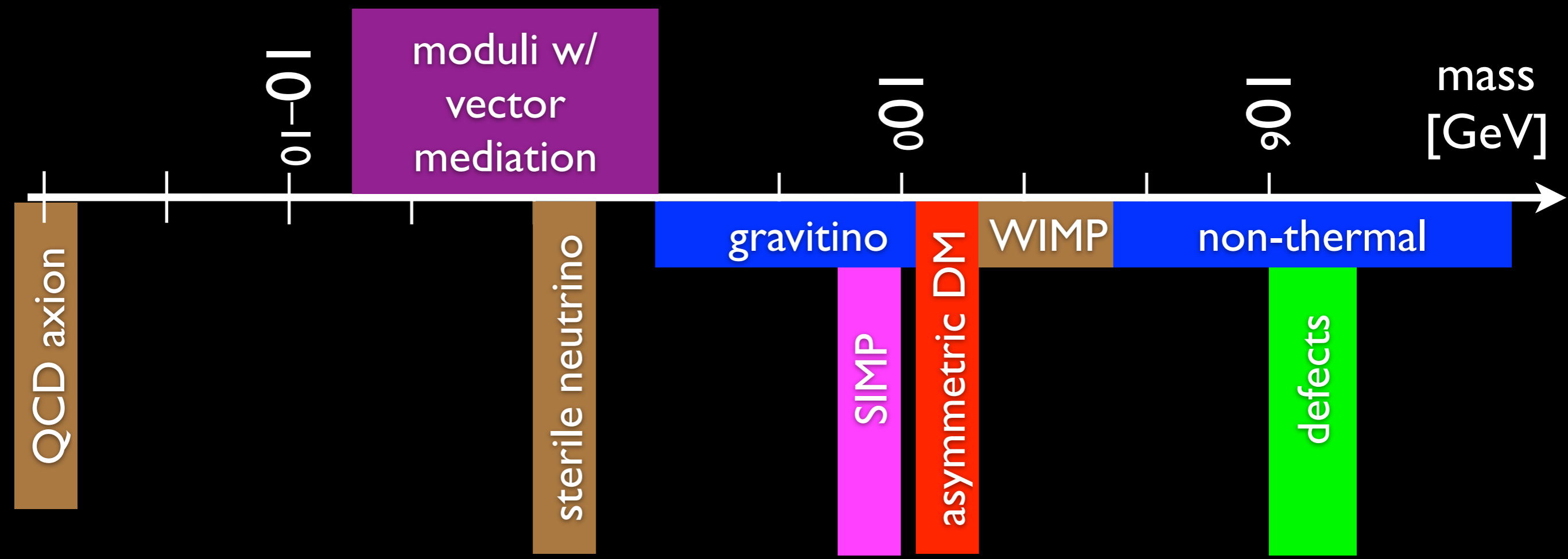
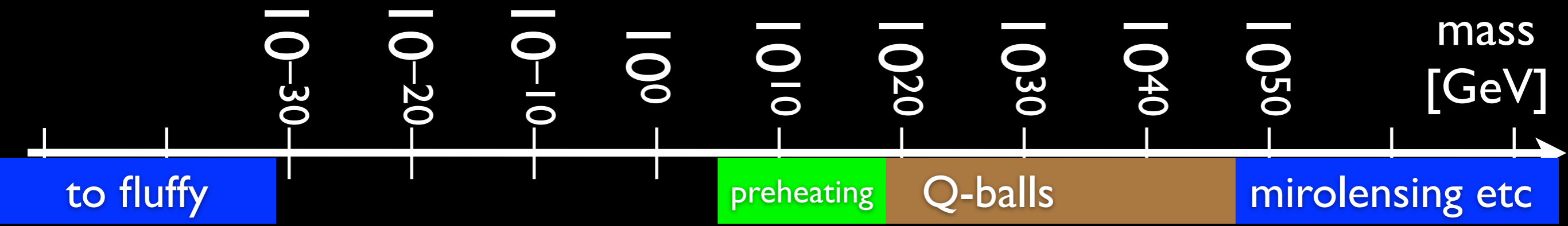


2. Production Mechanisms Suzaku

Exclusion:



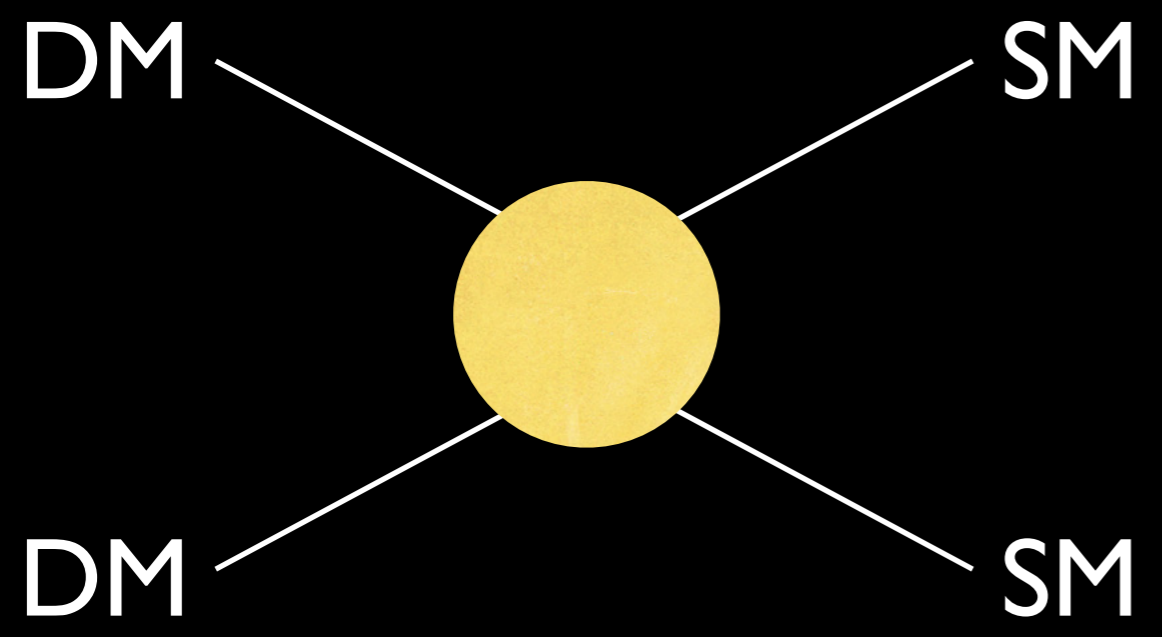
XRISM





$$\frac{n_{\text{DM}}}{s} = 4.4 \times 10^{-10} \frac{\text{GeV}}{m_{\text{DM}}}$$

Miracles

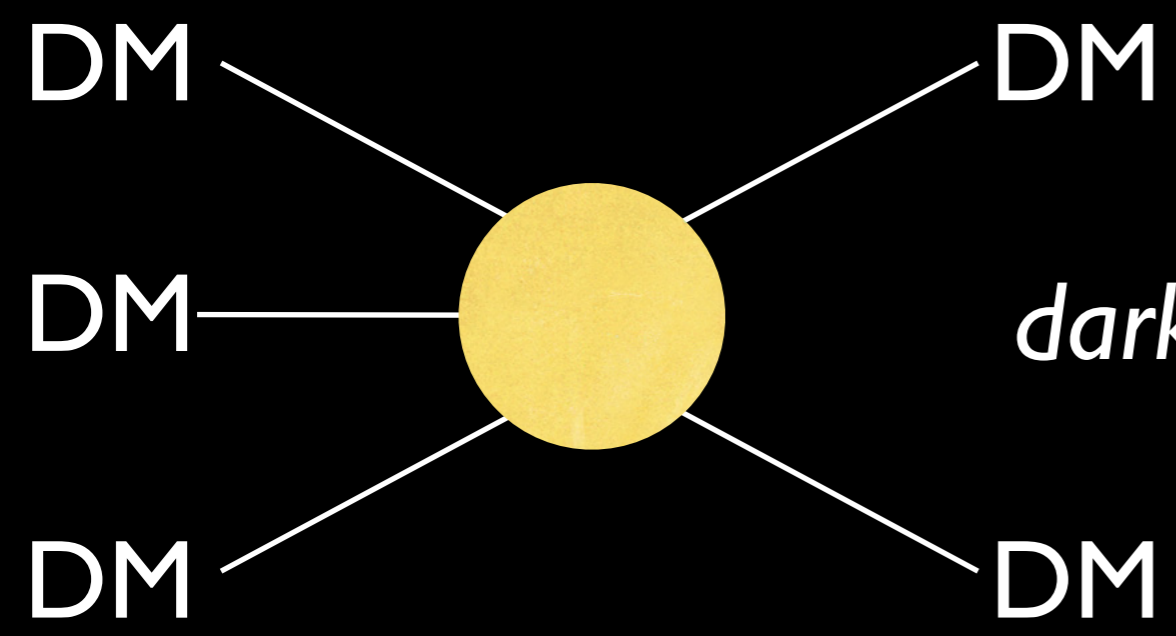


$$\langle \sigma_{2 \rightarrow 2\nu} \rangle \approx \frac{\alpha^2}{m^2}$$

$$\alpha \approx 10^{-2}$$

$$m \approx 300 \text{ GeV}$$

WIMP miracle!



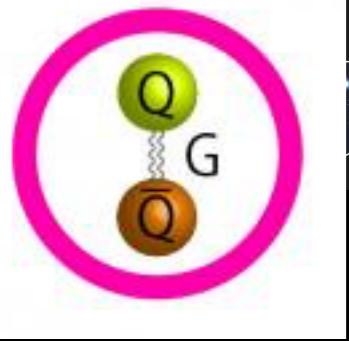
dark pions

$$\langle \sigma_{3 \rightarrow 2\nu^2} \rangle \approx \frac{\alpha^3}{m^5}$$

$$\alpha \approx 4\pi$$

$$m \approx 300 \text{ MeV}$$

SIMP miracle!



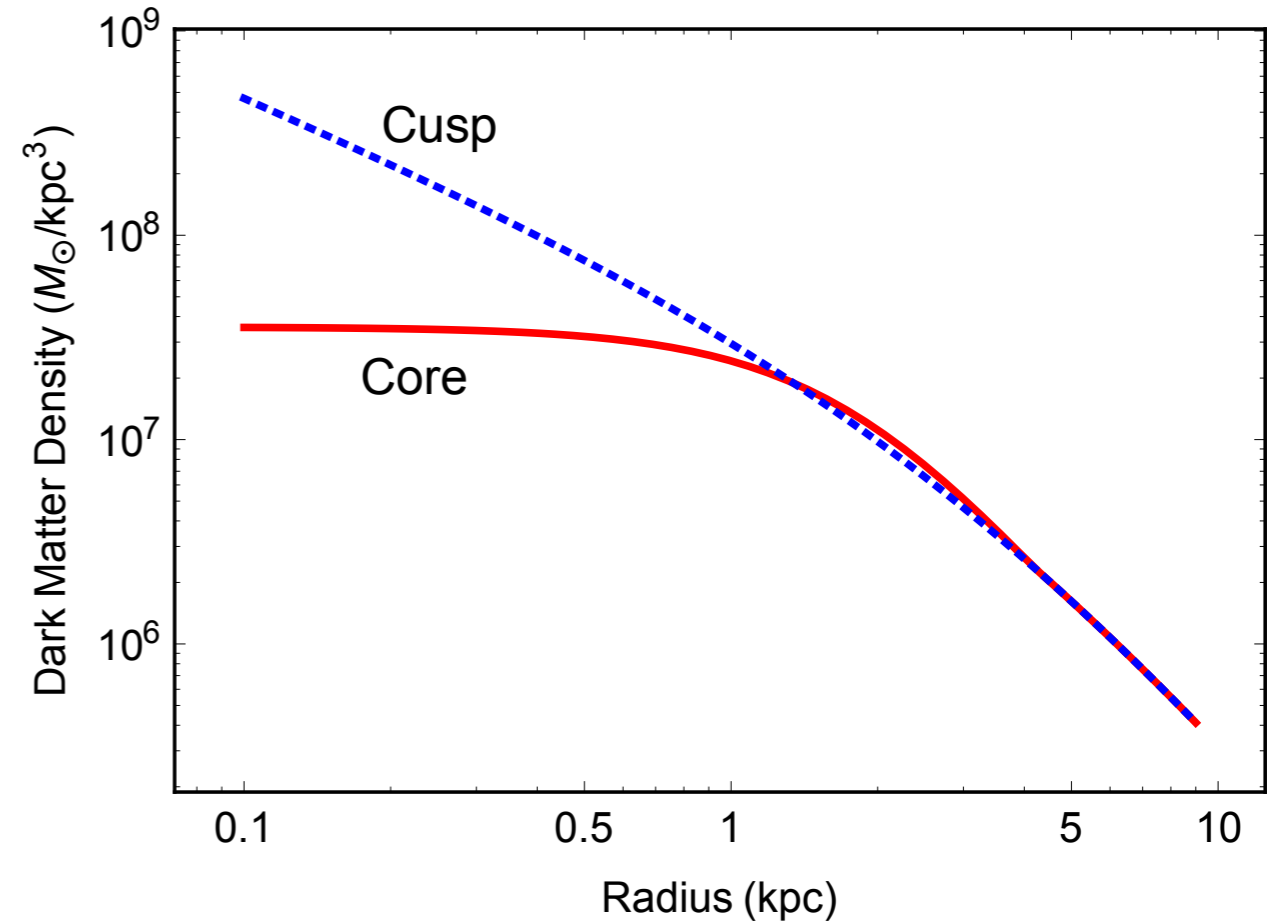
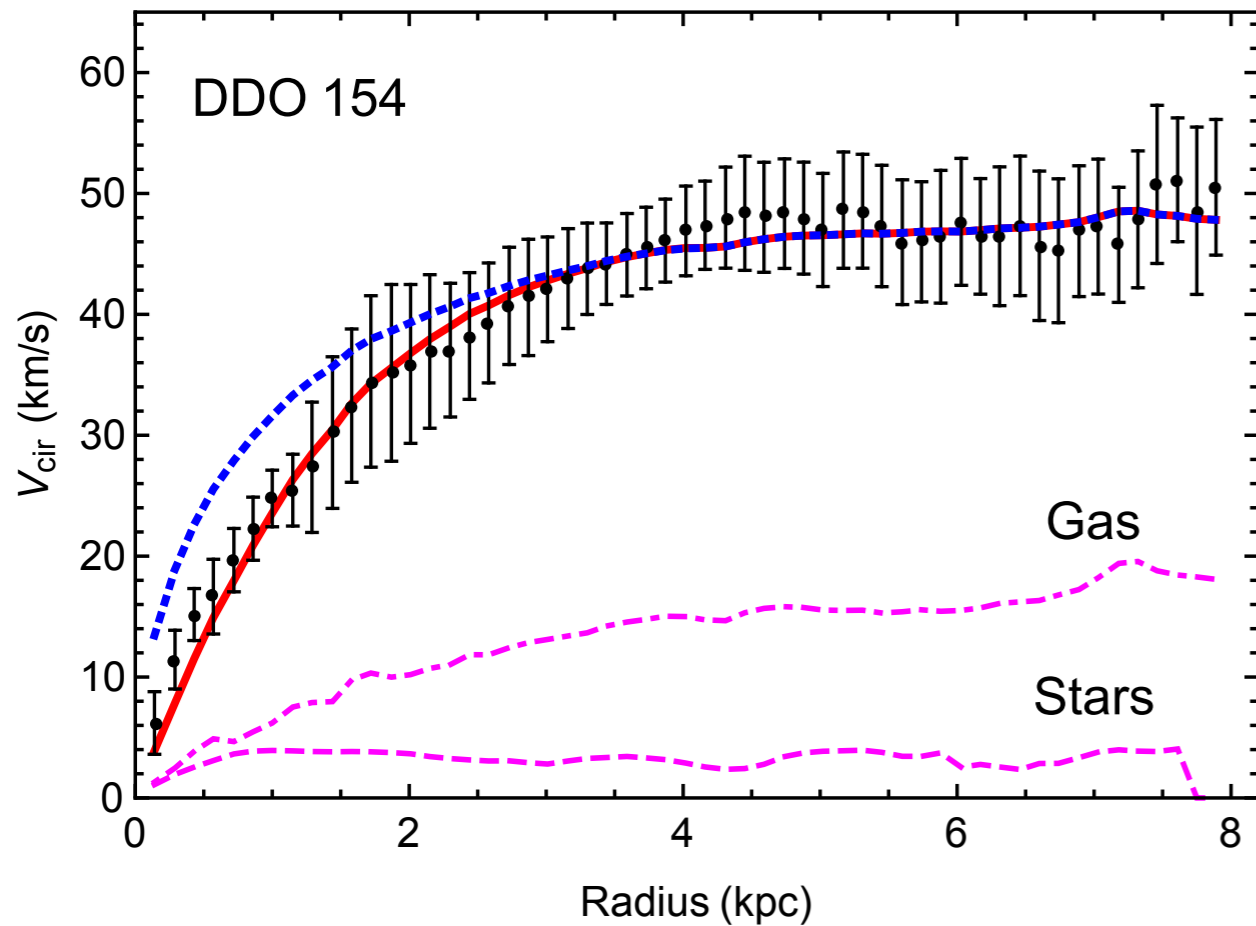
SIMPLe

- Most gauge theories, $SU(N_c)$, $SO(N_c)$, $Sp(N_c)$ lead to Wess-Zumino term if $N_f \geq 2, 3$
- $\mathcal{L}_{WZ} = \epsilon_{abcde} \epsilon^{\mu\nu\rho\sigma} \pi^a \partial_\mu \pi^b \partial_\nu \pi^c \partial_\rho \pi^d \partial_\sigma \pi^e$
- 3to2 interaction automatically there
- strongly-coupled theory
- rich with resonances

DDO 154 dwarf galaxy



DDO 154 dwarf galaxy



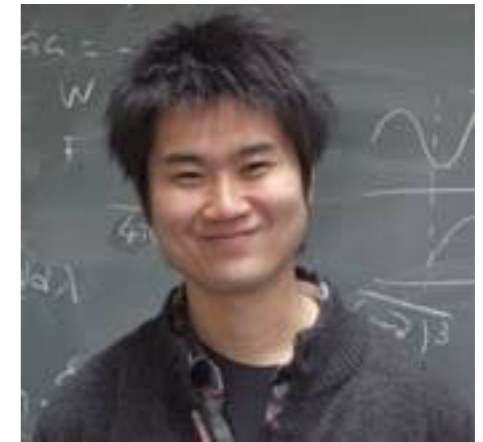
can be explained if dark matter scatters against itself
Need $\sigma/m \sim 1 \text{ b} / \text{GeV}$

only astrophysical information beyond gravity

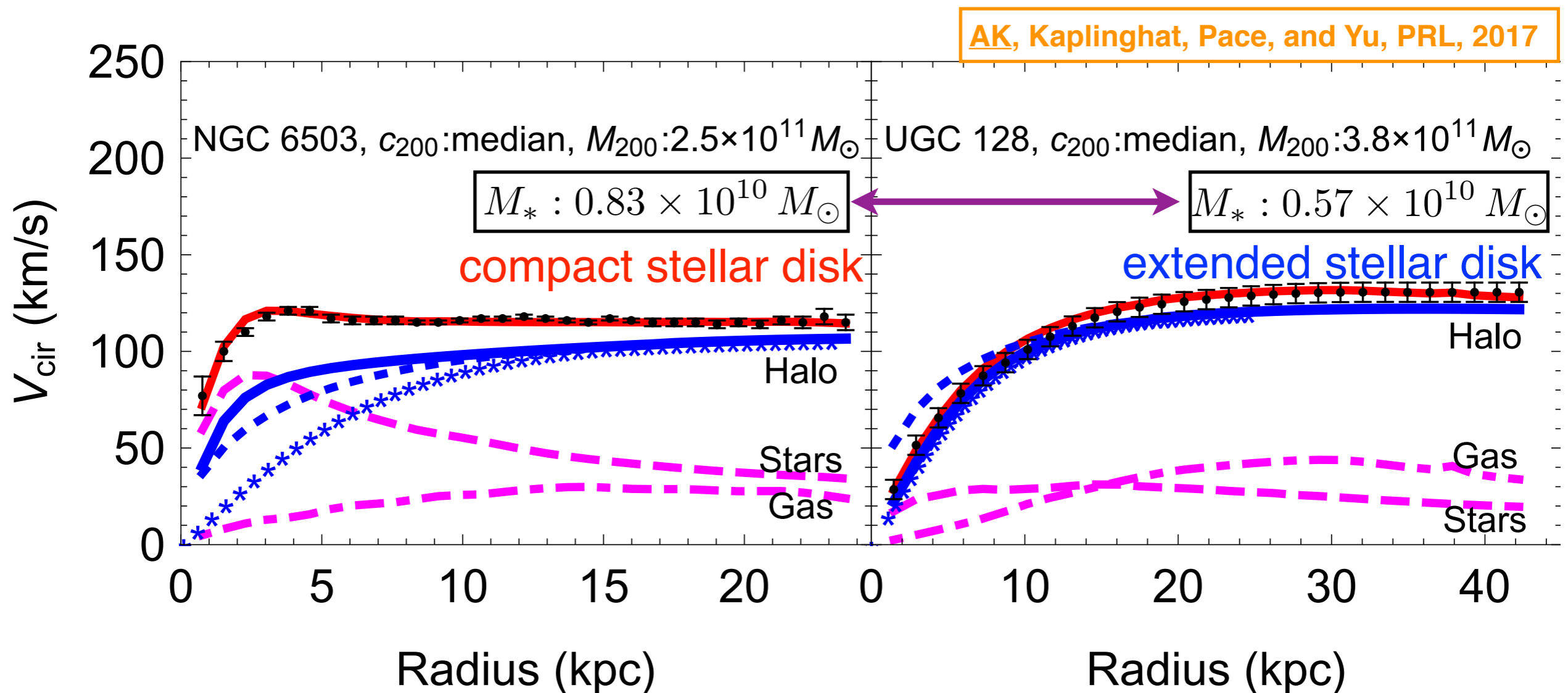
Diversity in stellar distribution

Similar outer circular velocity and stellar mass, but different stellar distribution

- compact \rightarrow redistribute SIDM significantly
- extended \rightarrow unchange SIDM distribution



Ayuki Kamada

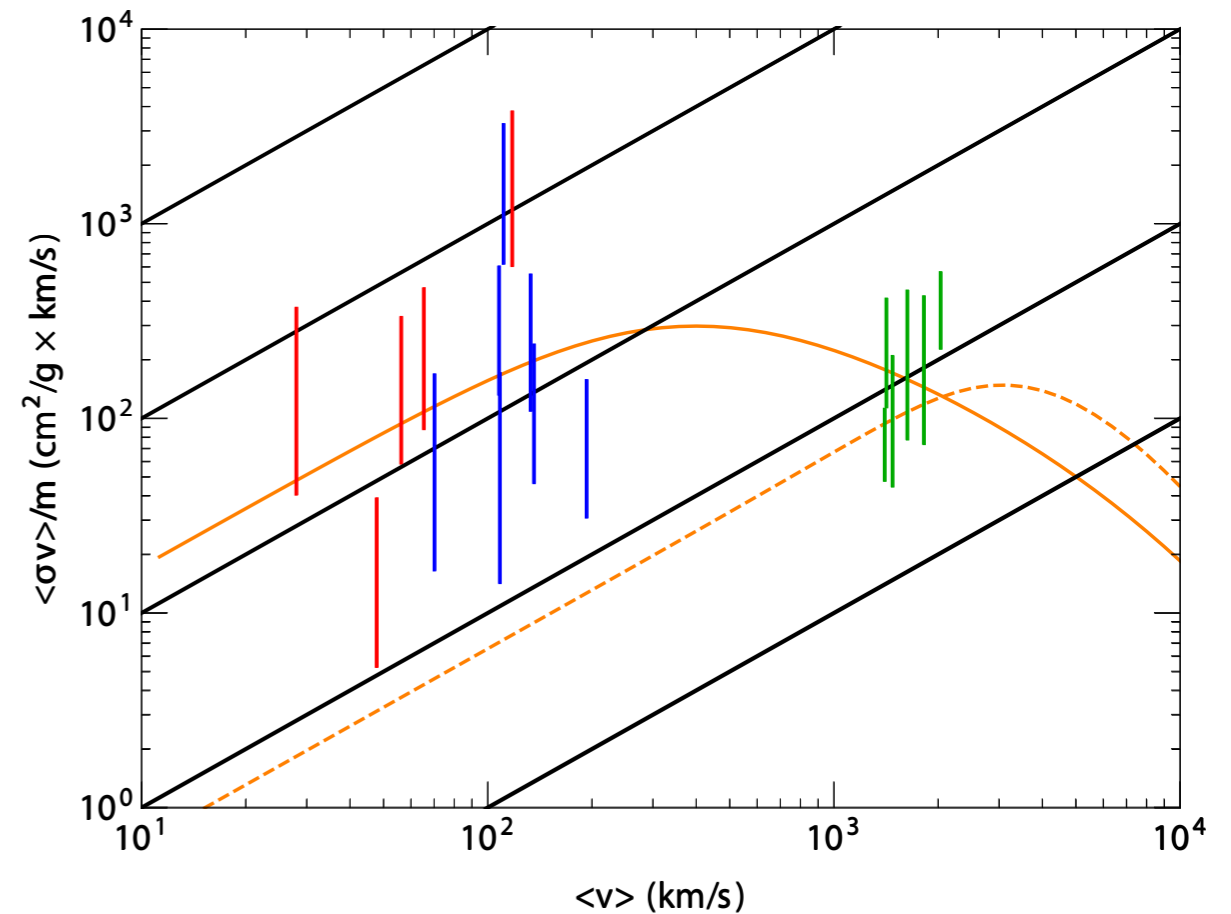


velocity dependence?

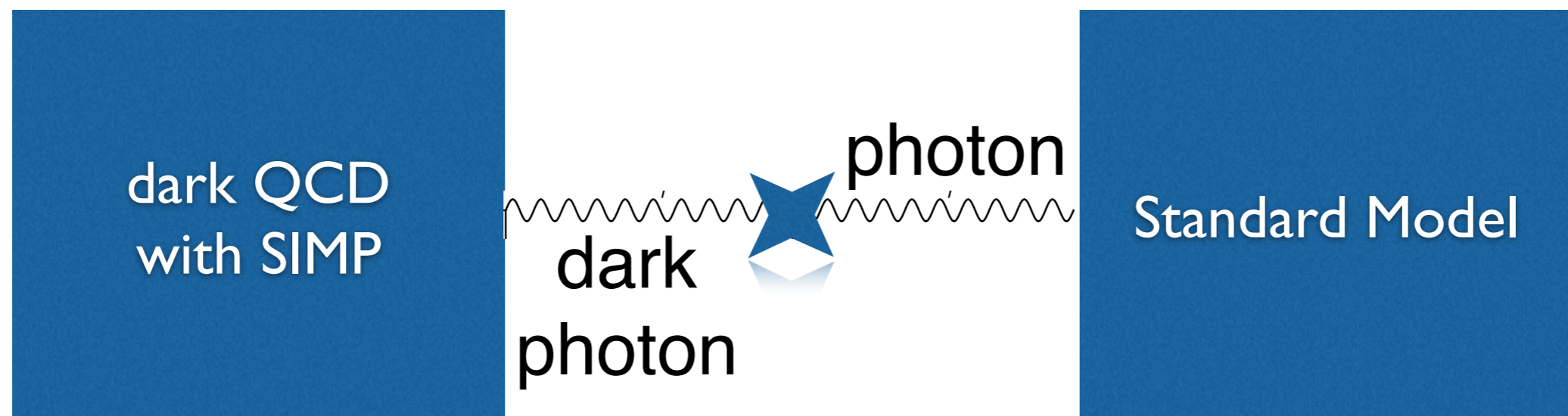
- cluster data prefer smaller σ ?
- near-threshold resonance can “fit” the data
- *i.e.*, $\pi\pi \rightarrow \sigma \rightarrow \pi\pi$
 - (Xiaoyong Chu, Camilo Garcia-Cely, HM)
 - useful description by Effective Range Theory (Hans Bethe 1949)

$$\mathcal{L} = m_R g RDM^2 .$$

n	a	b	γ_0	v_R (km/s)	m_R (GeV)	χ^2 /d.o.f.
0	24	32	$10^{-4.3}$	1829	26	2.1

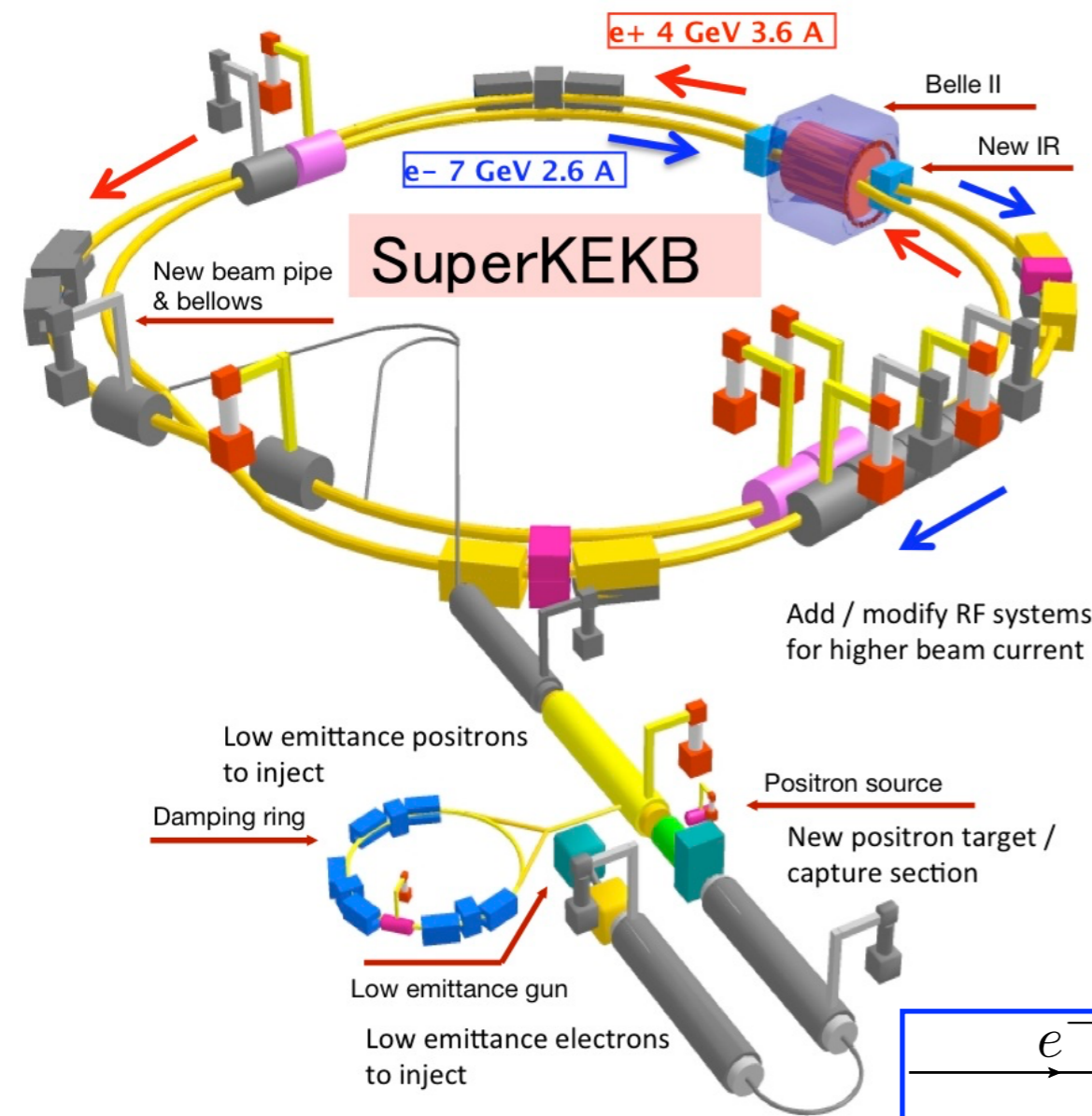


vector portal

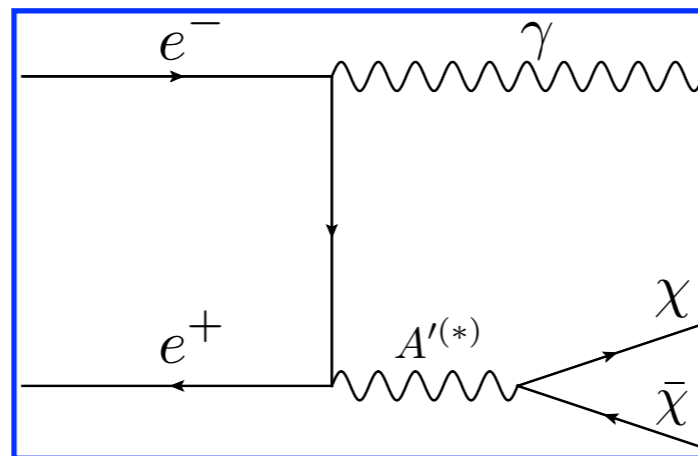
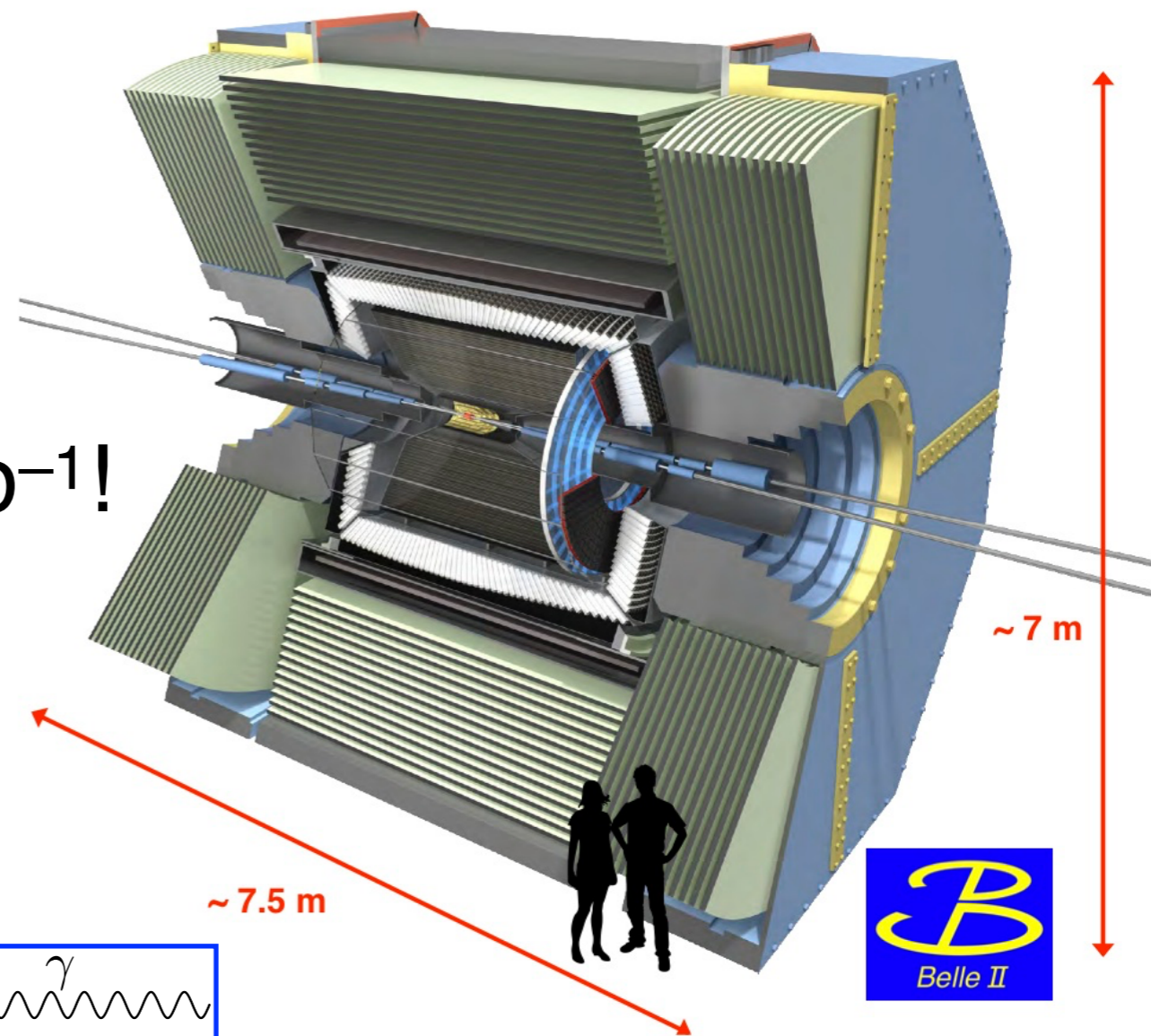


$$\frac{\epsilon_\gamma}{2c_W} B_{\mu\nu} F_D^{\mu\nu}$$

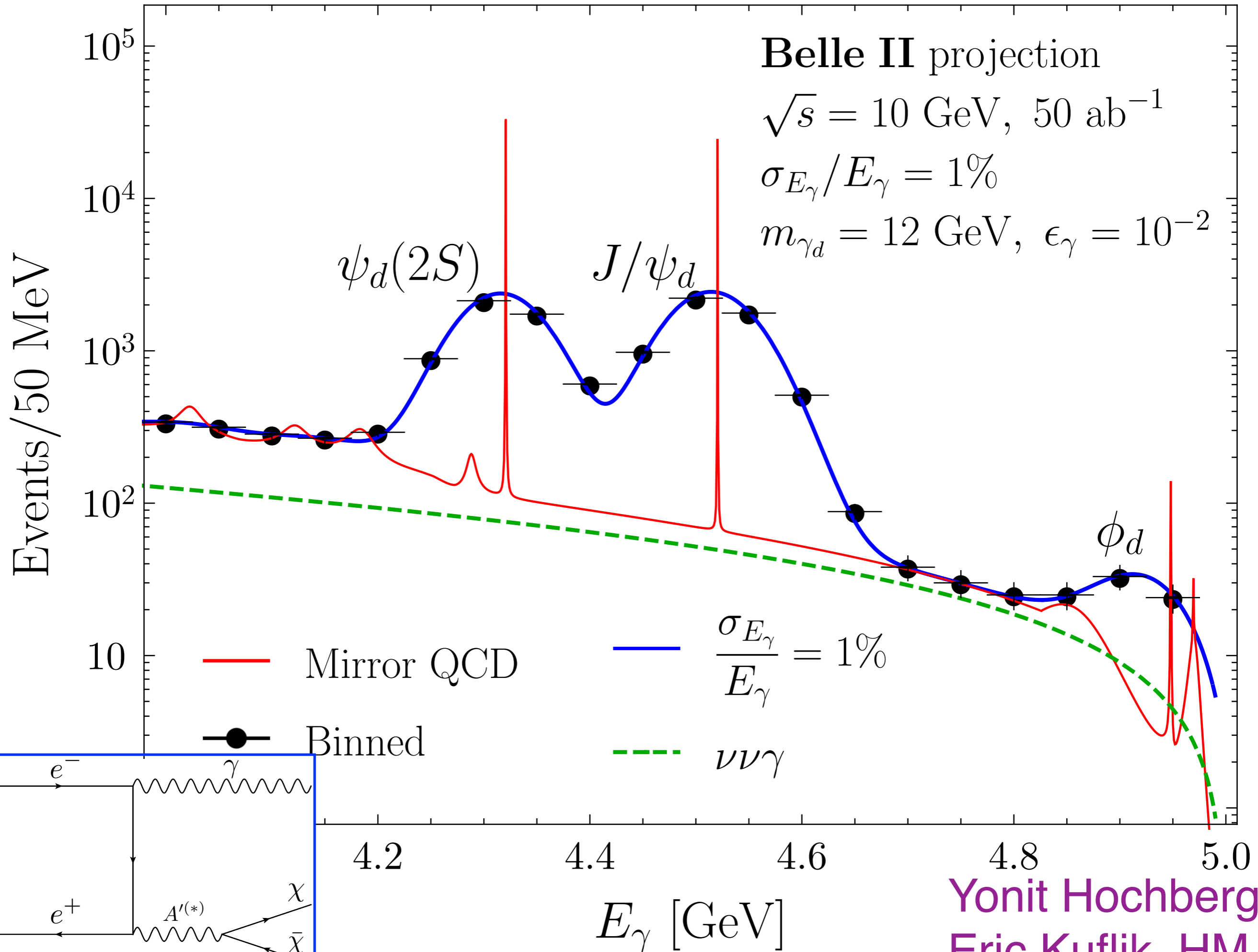
high-lumi e^+e^-



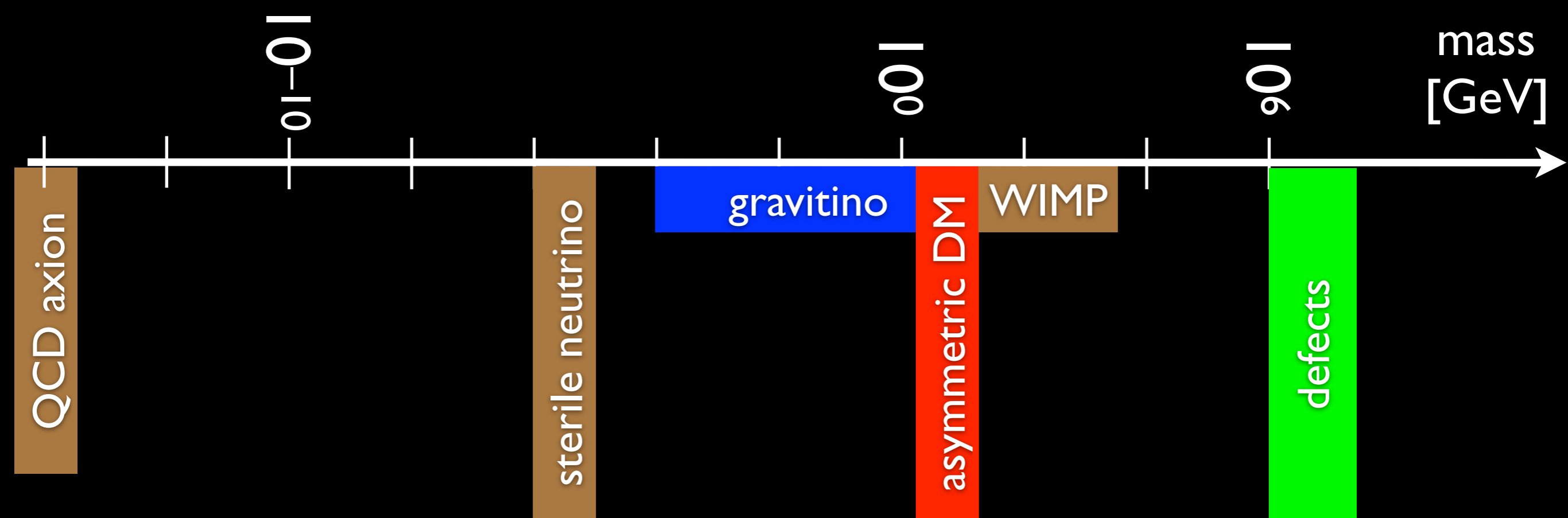
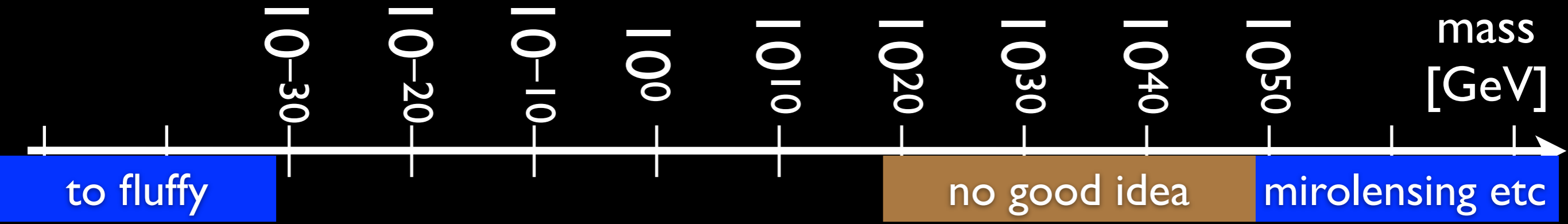
$50 \text{ ab}^{-1}!$



$$E_\gamma = \frac{\sqrt{s}}{2} \left(1 - \frac{M_{\text{inv}}^2}{s} \right)$$



Yonit Hochberg,
Eric Kuflik, HM



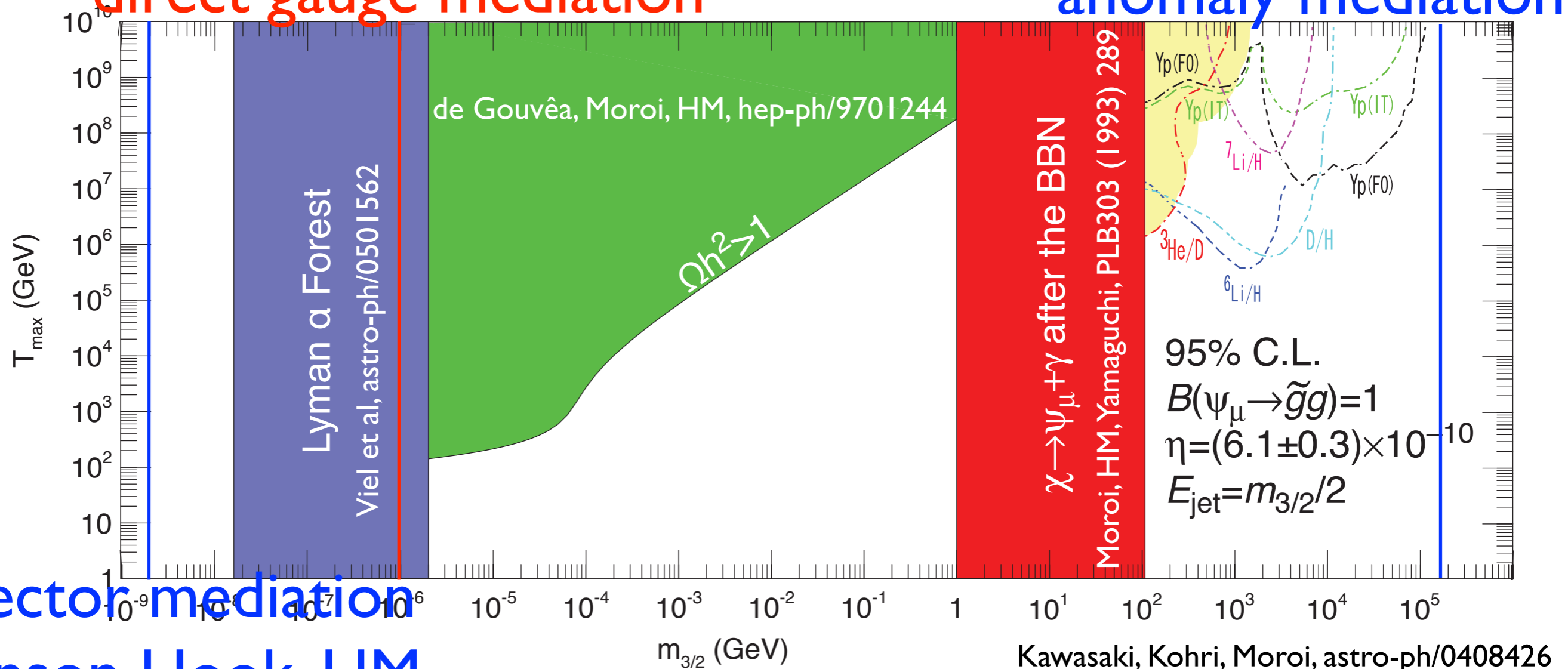
Gravitino problem

- **Gravitinos** produced thermally $\frac{n_{3/2}}{s} \sim 10^{-12} \frac{T_{RH}}{10^{10} \text{GeV}}$
- If decays after the BBN, dissociates synthesized light elements
- Hadronic decays particularly bad

$$m_{3/2}^2 = \frac{1}{3M_{Pl}^2} \left(|F|^2 + \frac{1}{2} D^2 \right)$$

direct gauge mediation

anomaly mediation



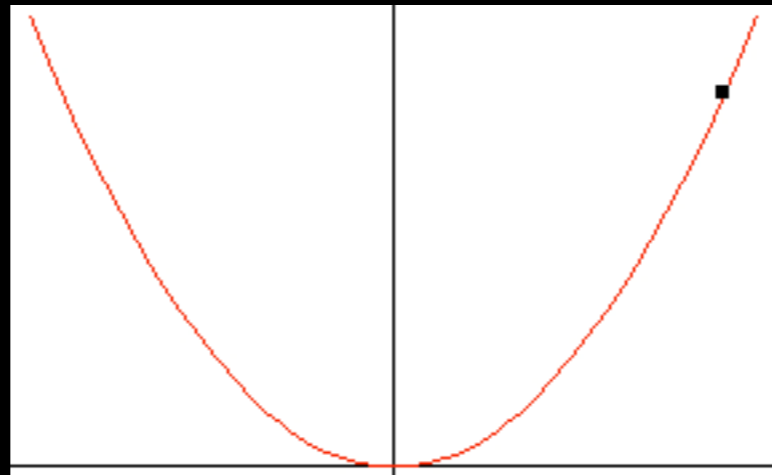
vector mediation

Anson Hook, HM



coherent oscillation

- any scalar field with initial displacement can in principle be dark matter



$$\phi_0 \approx \left(\frac{T_{eq}^2 M_{Pl}^3}{m_\phi} \right)^{1/4} = (3 \times 10^{11} \text{ GeV}) \left(\frac{\text{eV}}{m_\phi} \right)^{1/4}$$



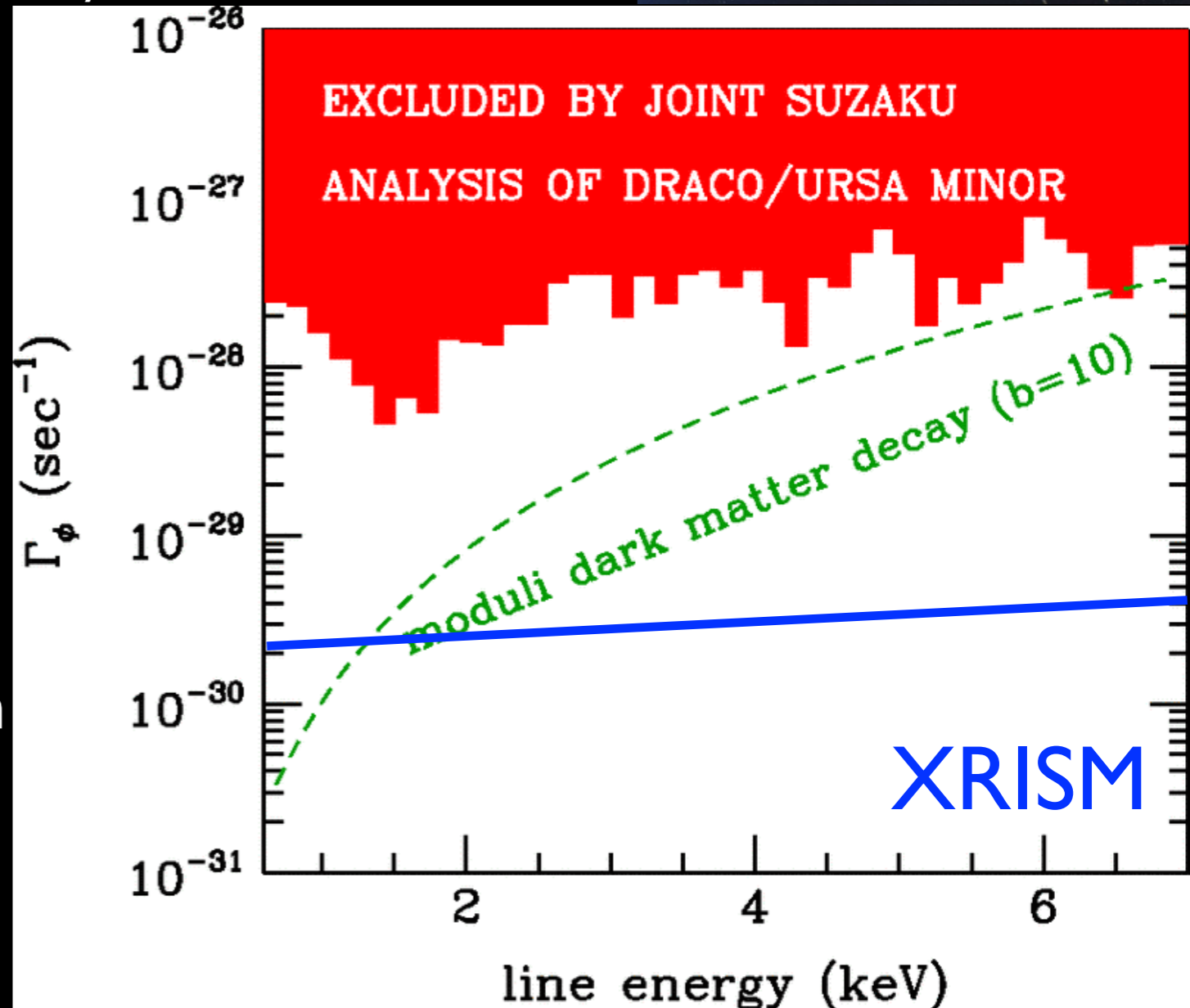
$$\tau(\phi \rightarrow \gamma\gamma) \sim 10^{28} \text{sec} \left(\frac{m_\phi}{10\text{keV}} \right)^{-3}$$



moduli

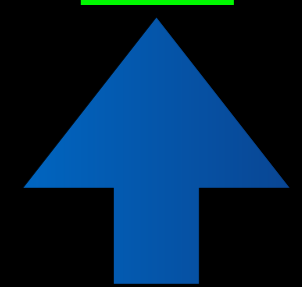
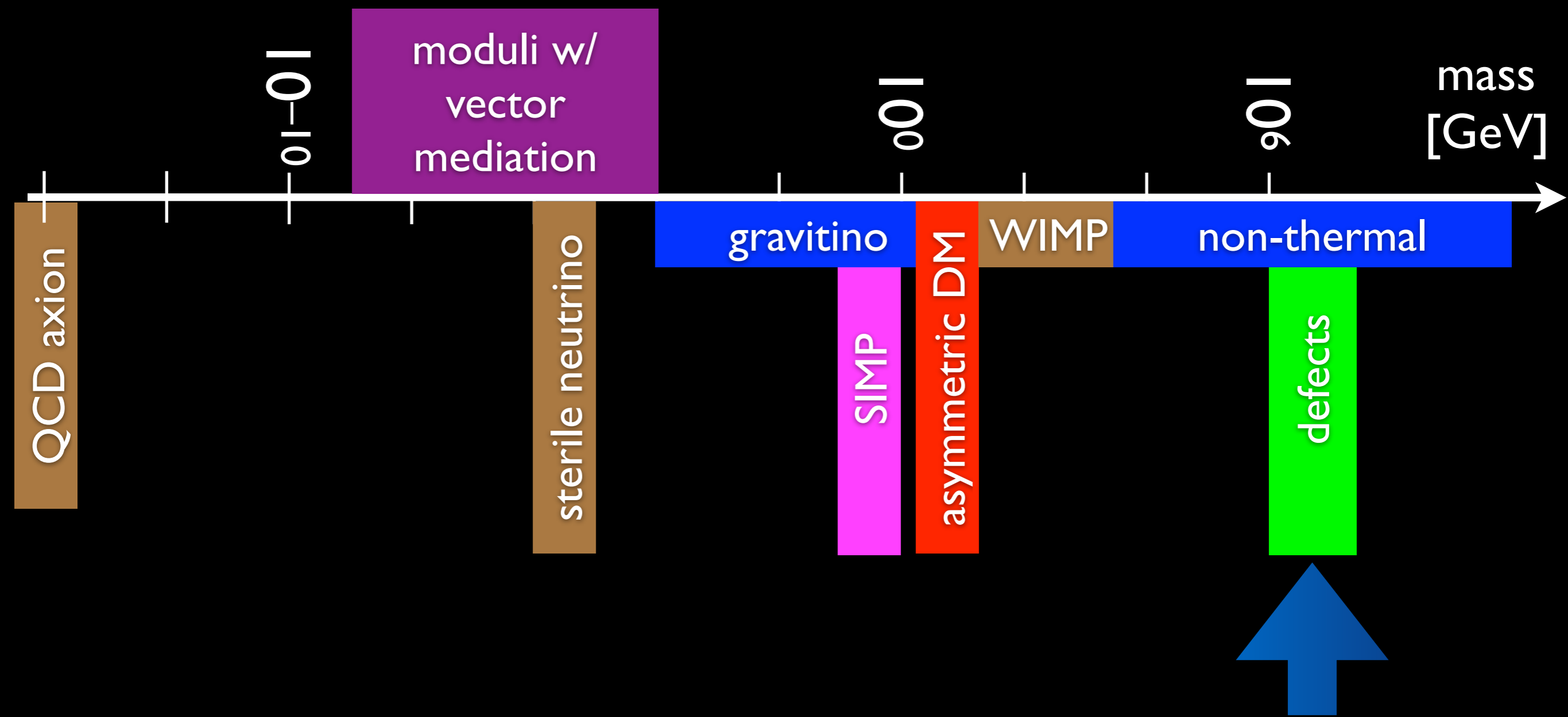
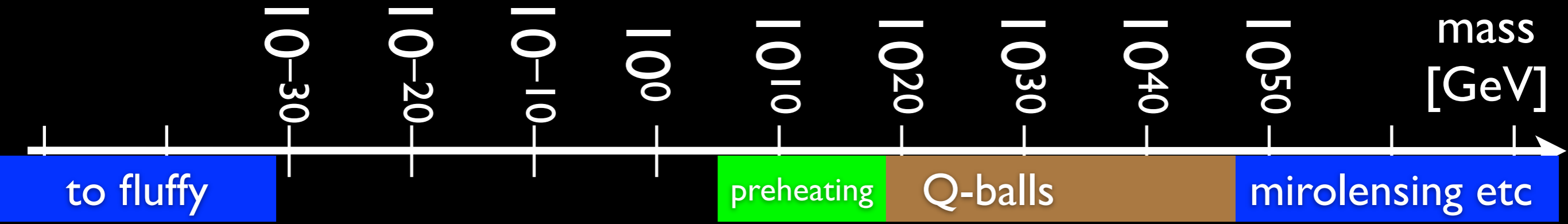
Kusenko, Lowenstein, Yanagida
Phys. Rev. D 87, 043508

- If stabilized by low-energy SUSY breaking ($\sim \text{TeV}$), modulus may be very light
- moduli mass expected to be comparable to the gravitino mass
- modulus coherent oscillation can be dark matter (de Gouvêa, HM, Moroi, hep-ph/9701244)



$$\phi_0 \approx \left(\frac{T_{eq}^2 M_{Pl}^3}{m_\phi} \right)^{1/4} = (3 \times 10^{11} \text{GeV}) \left(\frac{\text{eV}}{m_\phi} \right)^{1/4}$$





Topological defects

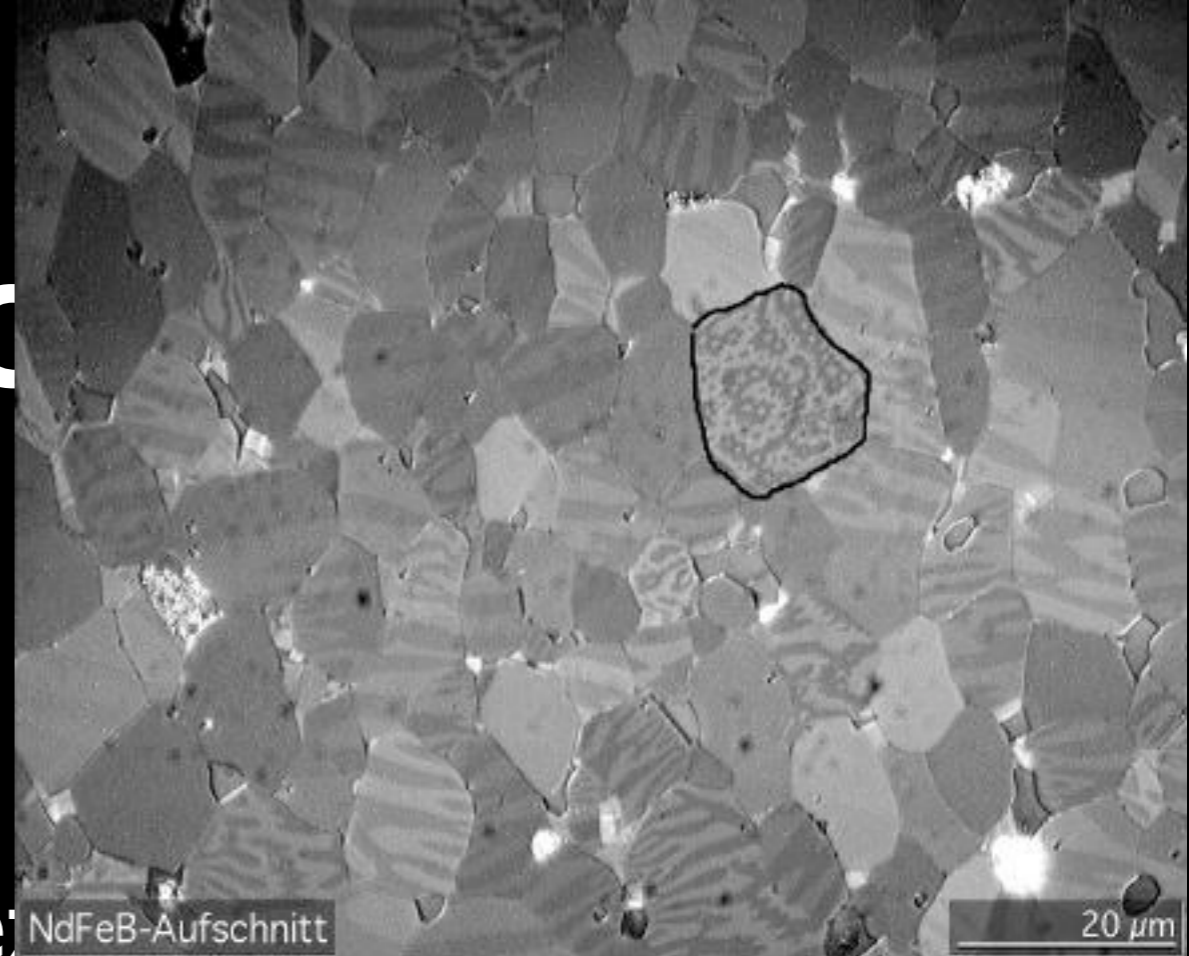
- common interest among AMO, condensed matter, particle physics, algebraic geometry
- symmetry breaking $G \rightarrow H$
- coset space G/H describes vacua
- can the space be mapped non-trivially into the coset space?
- $\pi_0(G/H) \neq 0$: domain walls
- $\pi_1(G/H) \neq 0$: string (vortex) ← Abrikosov
2003 Nobel
- $\pi_2(G/H) \neq 0$: monopole
- $\pi_3(G/H) \neq 0$: skyrmion

Kibble mechanism

- Kibble (1976) argued that phase transitions in expanding universe produce defects
- second-order phase transitions have **infinite correlation length** $\xi \propto |T - T_c|^{-\nu}$
- Therefore, all regions of causally connected space choose the same vacuum on G/H
- However, there is a finite horizon size $H^{-1} \approx M_{Pl}/T^2$
- **Kibble: about one defect per horizon**

Time scale

- We know that we need material slowly to grow (e.g. clear ice in the freezer)
- How does time scale come into the discussion?
- It takes time for things to line up!
relaxation
- *quenched* phase transition
- general discussion by Zurek (1985)



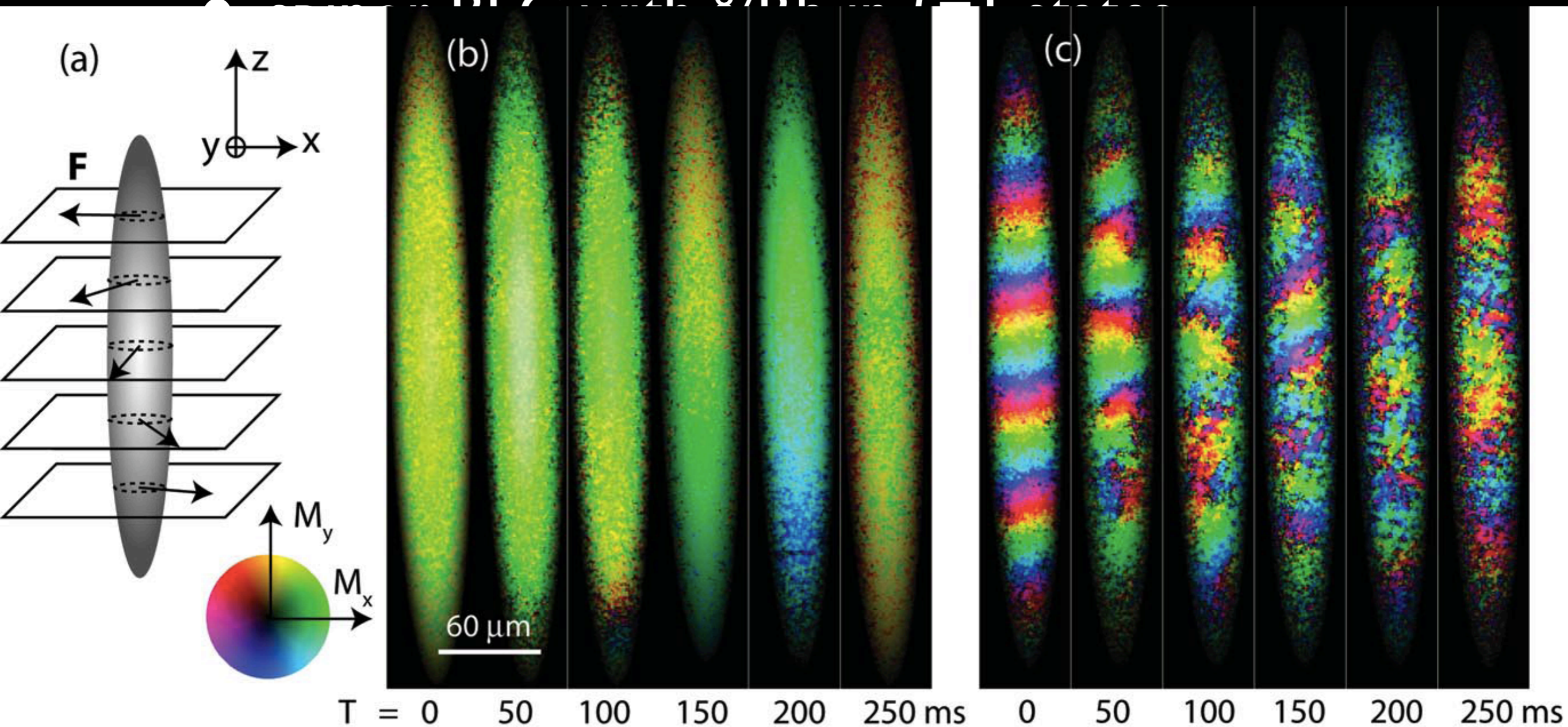
“Cosmological Experiments in Superfluid Helium?”

Phase transition revisited

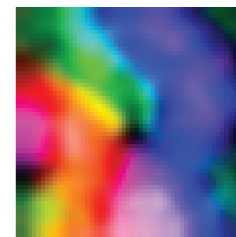
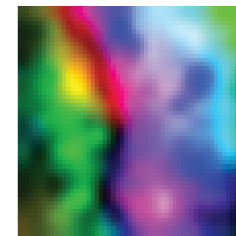
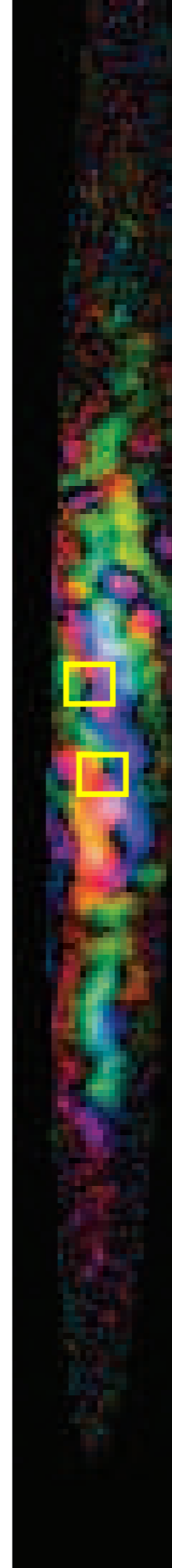
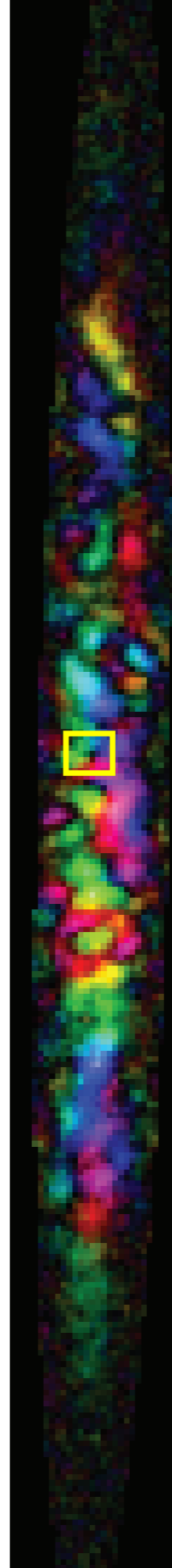
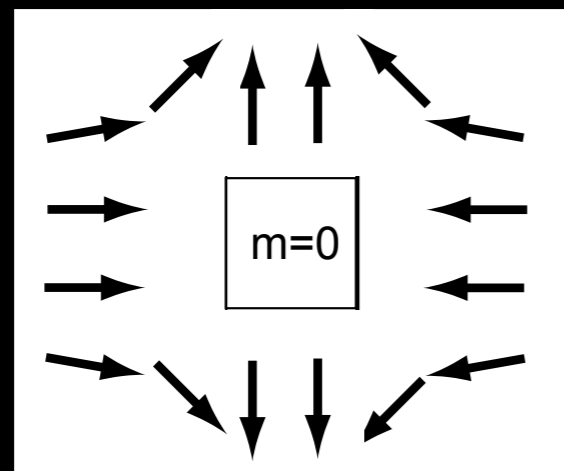
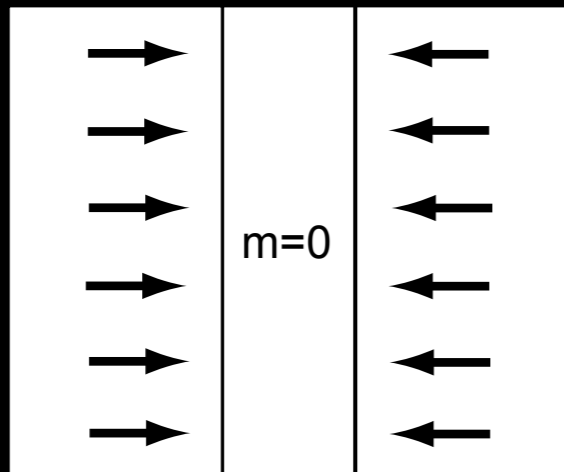
- correlation length: $\xi \propto |T - T_c|^{-\nu}$
- relaxation time: $\tau \propto |T - T_c|^{-\mu}$
- It takes an infinite amount of time for the system to “line up” at T_c
- If the system cools too quickly, it won’t line up even within a causally connected region

Experimental tests

- D. Stamper-Kurn group (Berkeley)

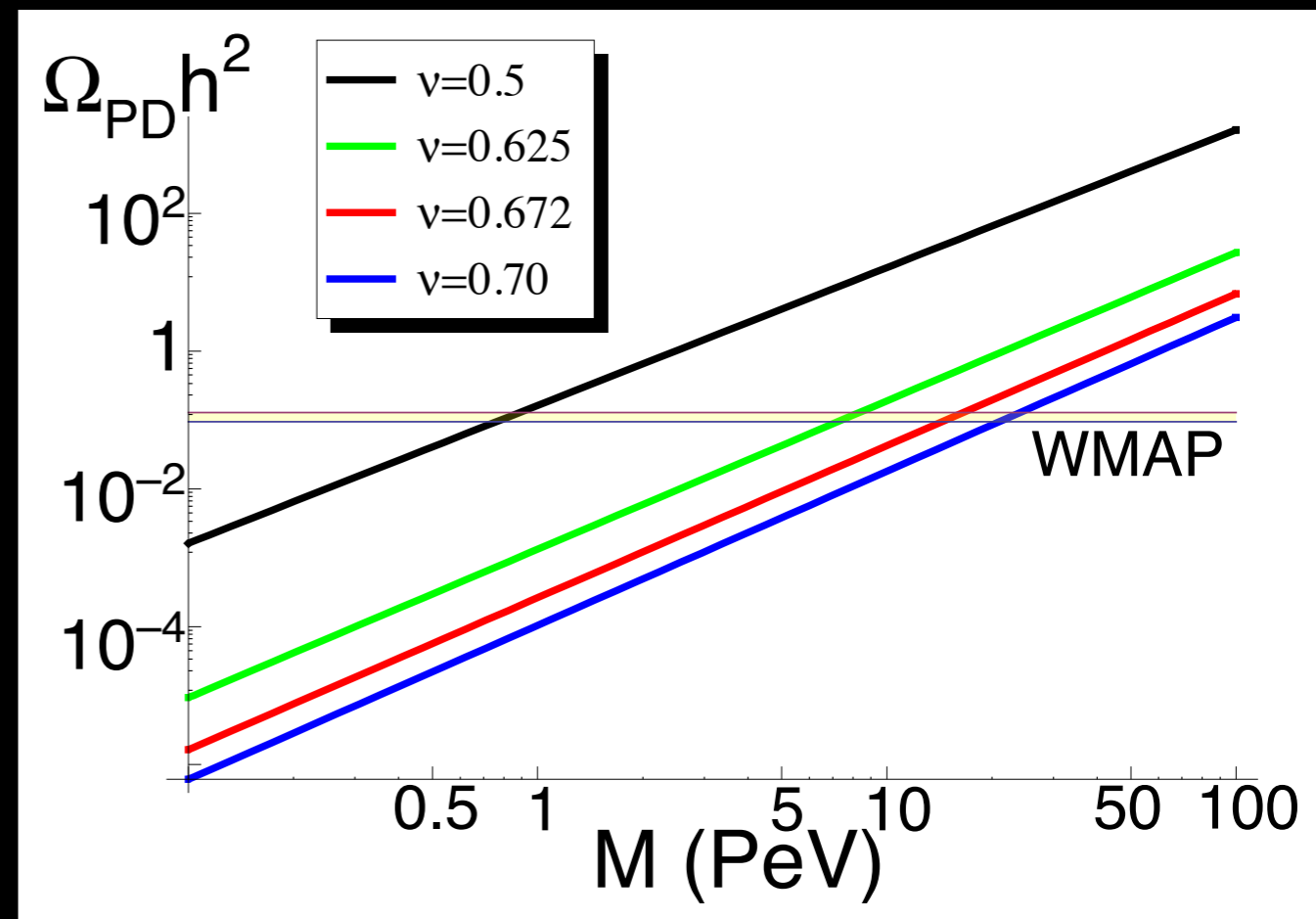


Vortex formation



topological dark matter

- point-like defect
- Kibble estimate: one per $H^{-1} \approx T_c^{-1} |M_{Pl}/T_c|$
- Then it could well be dark matter!
- Zurek estimate: one per $\xi \approx T_c^{-1} |M_{Pl}/T_c|^{1/3}$
- new “long-range force” among dark matter
- explain dwarf galaxies?



Conclusion

- Dark Matter exists, awaiting for discovery
 - In general, Dark Sector may exist, too
- Very little clue on mass scales now
 - **wide parameter space: opportunity!**
- WIMP still main paradigm, reach ν floor
- many new ideas on lighter dark matter
- colliders, beam dump, underground, cosmic rays, cavity, new technologies
- strategy: **look wherever we can!**