Beam-beam effects in plasma acceleration-based linear collider

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Outline

- Laser-driven plasma-based accelerators (LPAs): ultra-high gradient (tens of GV/m) provides compact source of energetic, fs, kA electron beams
 - GeV electron beams in cm-scale plasmas using LPAs
- LPA-based linear collider design considerations
 - operational plasma density
 - beam distribution
 - LPA staging toward high energy
- Beam-beam effects in LPA-based linear colliders
 - Beam-beam interaction effects determine the operational plasma density (determine required laser technology)

High-energy physics application of LPAs

- "Livingston Plot" Saturation of accelerator tech.
 - Practical limit reached for conventional accelerator technology (RF metallic structures)
 - Gradient limited by material breakdown
 - e.g., X-band demonstration ~100 MV/m







- Largest cost driver is acceleration
 - ~50 MV/m implies ~20 km/TeV
 - Facility costs scale roughly with facility size (and power consumption)
 - >50% cost in main linacs (e.g., ILC)

LPA application: Lepton Collider



- Any future linear TeV (>TeV) collider is a massive (ultra-massive) project
 - require >order of magnitude increase in acceleration gradient
- Ultra-high gradient requires structures to sustain high fields:
 - Dielectric structures: ~I GV/m
 - Plasmas: ~10 GV/m
- High gradients require high peak power:
 - Beam driven
 - Laser driven
- Significant progress worldwide in LPAs in the last 20+ years
- Critical developments:
 - Better understanding of LPA physics
 - Development of laser technology (CPA) for high peak power delivery

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Laser-plasma accelerators: compact sources (>10 GV/m) of fs e-beams

Esarey, Schroeder, Leemans, Rev. Mod. Phys. (2009)

• Accelerating field: characteristic size of plasma wave field, driven by the ponderomotive force of a resonant laser pulse with relativistic intensity (>10¹⁸ W/cm²) propagating in underdense plasma:

$$E \sim \left(\frac{mc\omega_p}{e}\right) \approx (96 \text{ V/m}) \sqrt{n_0 [\text{cm}^{-3}]}$$

• E.g., for $\sim 10^{18}$ cm⁻³, gradient ~ 100 GV/m

• Bunch duration:

• Accelerating bucket ~ plasma wavelength



- Beam charge (set by beam loading, plasma density): ~I-100 pC
- Beam duration (set by trapping physics and density): ~1-10 fs

~I-I0 kA peak current

Laser-plasma accelerator (LPA) experimental demonstration of GeV electron beam at LBNL



Plasma-based linear collider concepts



Limits to energy gain in laser-plasma accelerator (LPA): diffraction, dephasing, depletion



Limits to single stage energy gain:

$$mc^2 \Delta \gamma \sim q(mc\omega_p/e)L_{\rm int}$$

- Laser Diffraction: ~ Rayleigh range (typically most severe)
 - Controlled by transverse plasma density tailoring (plasma channel) and/or relativistic selfguiding and ponderomotive self-channeling
- Beam-Wave Dephasing: Slippage between e-beam and plasma wave
 - Controlled by longitudinal plasma density tailoring (plasma tapering)
- Laser Energy Depletion: Rate of laser energy deposition of into plasma wave

$$L_{\rm deplete} \propto n^{-3/2} \lambda^{-2}$$

Plasma density scalings

Laser-plasma interaction (depletion) length:

$$L_{\rm acc} \sim \lambda_p^3 / \lambda_L^2 \propto n^{-3/2}$$

Accelerating gradient:

$$E \sim E_0 = (m_e c \omega_p / e) \propto \sqrt{n}$$

• Energy gain:

$$W \sim (m c \omega_p / e) L_{\rm acc} \propto 1/n$$

For high-energy applications, laser depletion (and reasonable gradient) necessitates staging laser-plasma accelerators



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- Laser peak power:
$$P_{
m laser} \propto n^{-1}$$



L_{acc} ~I cm

U_{laser} ~2 J

Plaser ~100 TW

n ~ 7x10¹⁷ cm⁻³

Lacc ~8 cm

U_{laser} ~ [6]

 $P_{laser} \sim 0.4 P$

BELLA Laser Facility

Leemans et al., PAC Proc. (2013)

BELLA (BErkeley Lab Laser Accelerator) Facility:

- PW-laser for laser-accelerator science
- >42 J in <40 fs (> IPW) at I Hz laser and
- supporting infrastructure at LBNL
- commissioned in 2013





Multi-GeV electron acceleration using BELLA



- ▶ plasma: 9 cm H-discharge capillary, on-axis density 7x10¹⁷/cc
- Iaser: I 6 J, 40 fs
- ▶ 4.25 GeV e-beam, 6% energy spread, 0.3 mrad divergence, 10 pC



Staged LPAs: average gradient determined by driver in-coupling distance

Schroeder et al., PR ST-AB (2010)



10¹⁸

10¹⁷

Operational plasma density [cm-3]

-ength of staged-LPA linac [km]

10¹⁵

10¹⁶



- Operate in "quasi-linear" regime:
 - Quiver momentum weakly-relativistic *a*~1 (Intensity ~ 10¹⁸ W/cm²)
 - Region of acceleration/focusing for both electrons and positrons
 - Stable laser propagation in plasma channel
 - Independent control of accelerating and focusing forces



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hollow plasma channels: Excellent wakefield properties for ultra-low emittance preservation



Excellent wakefield properties in plasma channel and independent control over accelerating and focusing forces:

- Accelerating wakefield uniform in radial position
- Focusing wakefield uniform in longitudinal position (no head-to-tail variation in focusing force) and linear in radial position
- Ion motion negligible
- Mitigates Coulomb scattering

Energy spread minimized using shaped beams

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Ramped triangular current distribution :

 $I = (1 + \zeta/L_b)I_b$



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Positron beams accelerated in linear regime in hollow plasma channel



In quasi-linear regime, acceleration of positrons is symmetric to electrons



Basic scalings indicate disruption small for plasma accelerated (ultra-short) beams

Disruption parameter:

P. Chen and K. Yokoya, Phys. Rev. D 38, 987 (1988)

$$D_x = \frac{2r_e N \sigma_z}{\gamma \sigma_x^* (\sigma_x^* + \sigma_y^*)}$$

Plasma-based accelerators intrinsically produce short (< plasma skin depth) beams</p>

Luminosity enhancement effects from beam disruption are typically weak D<<I for LPA-based colliders owing to the ultrashort LPA bunch length (<< beam-beam lens)</p>

Beamstrahlung minimization: basic scalings

- Beamstrahlung parameter: $\Upsilon = \gamma \langle E + B \rangle / E_c \approx \frac{5r_e^2 \gamma}{6\alpha(\sigma_x^* + \sigma_y^*)} \frac{N}{\sigma_z}$
- average number of beamstrahlung photons/lepton:

P. Chen and K. Yokoya

$$n_{\gamma} \approx 2.54 \left(\alpha^2 / r_e \gamma \right) \sigma_z \Upsilon (1 + \Upsilon^{2/3})^{-1/2}$$

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- ▶ Beamstrahlung suppressed by using short beams (in limit Y>>I): $n_{\gamma} \approx 2.54 \left(\alpha^2/r_e\gamma\right) \Upsilon^{2/3}\sigma_z$ $\delta_{\gamma} \approx 0.722 \left(\alpha^2/r_e\gamma\right) \Upsilon^{2/3}\sigma_z$

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Short beams save power (Y>>I):

$$rac{\mathcal{L}}{U_{
m cm}^2} \propto rac{n_{\gamma}^{3/2} \eta_{wb} P_{
m wall}}{\sigma^* \gamma^{5/2} \sigma_z^{1/2}}$$

Plasma-based accelerators produce short (< plasma skin depth) beams: $\sigma_z < k_{p-18}^{-1}$

Ultra-short beams can be accelerated without energy spread growth

▶ Ultra-short beams are desirable, e.g., beamstrahlung suppression in colliders.

beamstrahlung photons/electron: $n_\gamma \propto {\cal L}^{1/3} \sigma_z^{1/3}$

Trapezoidal current distribution:



Improved efficiency achieved using bunch trains



Improved efficiency achieved using bunch trains:

- Each bunch has same charge
- Experiences same (constant across bunch) accelerating gradient
- Efficiency increased by number of bunches in train



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 η (plasma to beam)= 0.75 gradient = 0.5(peak field)



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Additional laser pulse allows for no energy to remain in coherent plasma oscillations after energy transferred to particle beam

Average power reduced at lower plasma density (Beamstrahlung limits charge/bunch)

22

3 TeV laser-plasma collider example

PA stage laser-plasma parameters.	densit
Plasma density (wall), n ₀ [cm ⁻³]	10 ¹⁷
Plasma wavelength, λ_p [mm]	0.1
Channel radius, $r_c [\mu m]$	22
Laser wavelength, λ [µm]	1
Normalized laser strength, a_0	1.2
Peak laser power, PL [TW]	50
Laser pulse duration (FWHM), τ_L [fs]	130
Laser energy, U _L [J]	6.5
Normalized accelerating field, E_L/E_0	0.2
Peak accelerating field, E_L [GV/m]	6
Laser depletion length, Lpd [m]	8.7
Plasma channel length, L_c [m]	1.7
Laser depletion, η_{pd} [%]	20

Shaped electron/positron beam parameter	rs
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Bunch phase (relative to peak field), φ	π/3
Loaded gradient, E_z [GV/m]	3
Beam beam current, I [kA]	3
Charge/bunch, $eN_b = Q$ [nC]	0.19
Length (triangular shape), L_b [µm]	36

beam energy	1.5 TeV
energy gain/stage	5 GeV
RMS σ z[micron]	8.5
σ x[nm]/ σ y[nm]	18 / 0.5
Luminosity [s ⁻¹ cm- ²]	1E+35
laser rep rate [kHz]	84
Beamstrahlung parameter	16
Beamstahlung photons/e	0.81
Beamstrahlung energy spread	0.20
Disruption parameter	0.046
Power (LPA linacs)	407 MW

Laser-plasma accelerator-based collider concept

Electron

⁵⁰⁰⁻¹⁰⁰⁰ m, 100 Stages

^{Laser in coupling}

 Plasma density scalings [minimize construction (max. average gradient) and operational (min. wall power) costs] indicates: n ~ 10¹⁷ cm⁻³

- Quasi-linear wake (a~I): e- and e+
- Staging & laser coupling into plasma (hollow) channels:
 - tens J laser energy/stage required
 - energy gain/stage ~few GeV in <1m</p>

Positron

⁵⁰⁰⁻¹⁰⁰⁰ m, 100 Stages

10 GeV

 $G_{a_{\mathcal{S}}}$

jet,

Laser technology development required:

- High luminosity requires high rep-rate lasers (10's kHz)
- Requires development of high average power lasers (100's kW)

C_{apillary}

- Bandwidth (support ~100 fs duration)
- High laser efficiency (~tens of %)

Leemans & Esarey, Physics Today (2009)

Laser-plasma accelerator-based collider concept

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Demonstration of acceleration in second independentlypowered laser-plasma accelerator at LBNL

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Steinke et al., Phys. Plasmas (2016)

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Summary and Conclusions

- Laser-pasma accelerators provide ultra-high gradients (compact accelerators) generating short (fs) beams (high peak current)
 - 4 GeV beams in 9-cm plasma using LPA at BELLA
 - 10 GeV beams in <1m will be available in next (few) years
- Beam-beam interaction effects modify the basic scalings and determine the operational plasma density (determines required laser technology, etc.)
 - Basic scalings indicate ~IEI7/cc operating density.
 - Operating at low plasma density increases beamstrahlung effects (higher bunch charge and longer beams)
 - Bunch charge constrained by beamstrahlung requiring multi-bunch format or increase repetition frequency (power).
 - Detailed modeling still to be done (including beam shape, delivery system, etc.)
- Laser-plasma accelerator-based linear collider has many technical challenges and R&D for collider application ongoing
 - Staging LPA experiments underway at LBNL
 - High peak & average power laser technology development

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