

# Beam-Beam beta-beating effects and implication for the HL-LHC and FCC

Javier Barranco, Tatiana Pieloni, Claudia Tambasco, Patrik Jorge Gonçalves (EPFL/LPAP)

Rogelio Tomás, Xavier Buffat (CERN), Simon White (ESRF)

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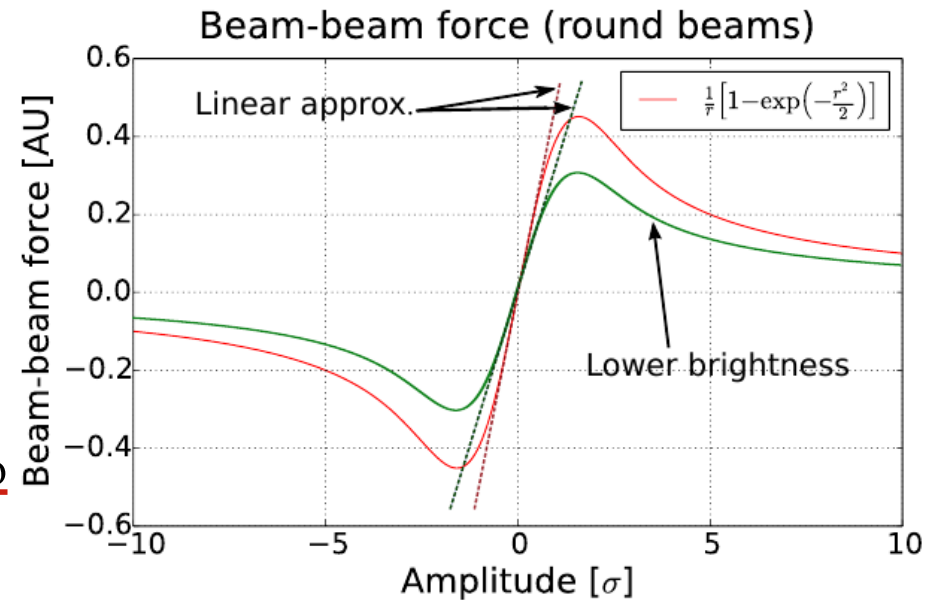
- Beam-beam  $\beta$ -beating
- Linear BB  $\beta$ -beating
- Non-linear BB  $\beta$ -beating
- Beam-beam amplitude detuning with forced oscillations
- Beam-beam  $\beta$ -beating measurements @ LHC
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# $\beta$ -beating beam-beam induced

- The BB interaction non-linearity will cause non-linear amplitude detuning.
- However for small amplitude particles ( $< 1 \sigma$ ) the kick is **linear** (quad-like).
- The change of the  $\beta$ -function assuming a series of small quadrupole errors is given by:

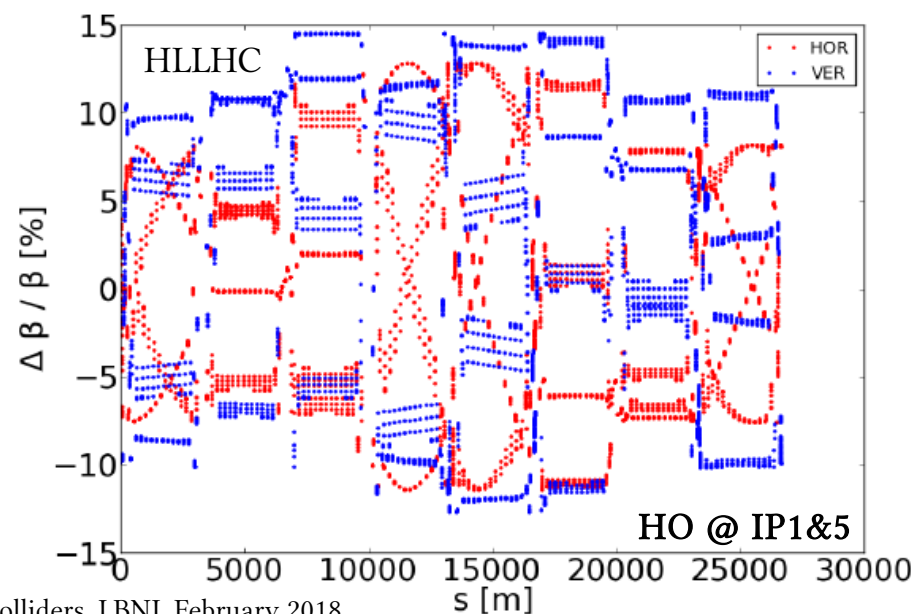
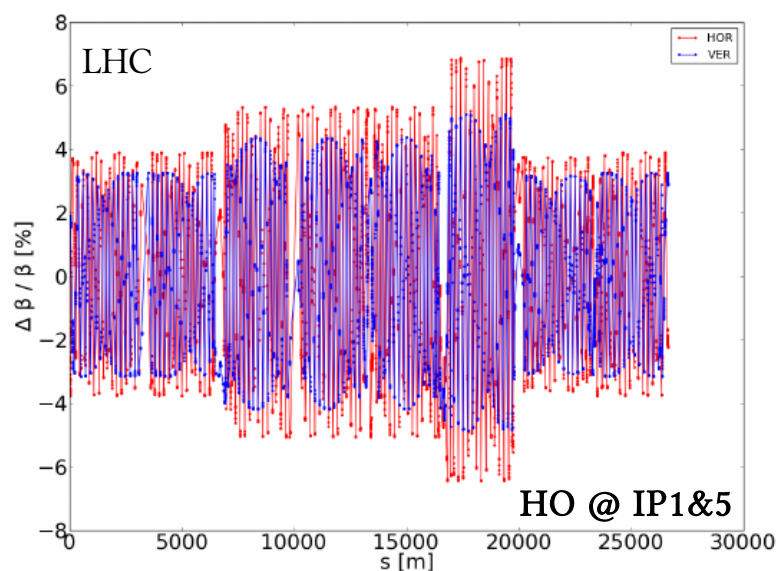
$$\frac{\Delta\beta(s)}{\beta_0(s)} = \frac{2\pi\xi}{\sin(2\pi Q_0)} \sum_{i=0}^N \cos(2|\mu_0(s) - \mu_0(s_i)| - 2\pi Q_0)$$

- The expected beating is directly proportional to the beam-beam parameter. HLLHC and FCC are designed to increase the  $\xi_{bb}$  by 2-3 times
- Operationally the LHC  $\beta$ -beating from lattice errors is routinely measured and corrected during commissioning to 5-7% level.
- **Is the expected BB  $\beta$ -beating comparable with operational requirements? Linear vs Non-linear beating? Impact on machine protection? Luminosity?**

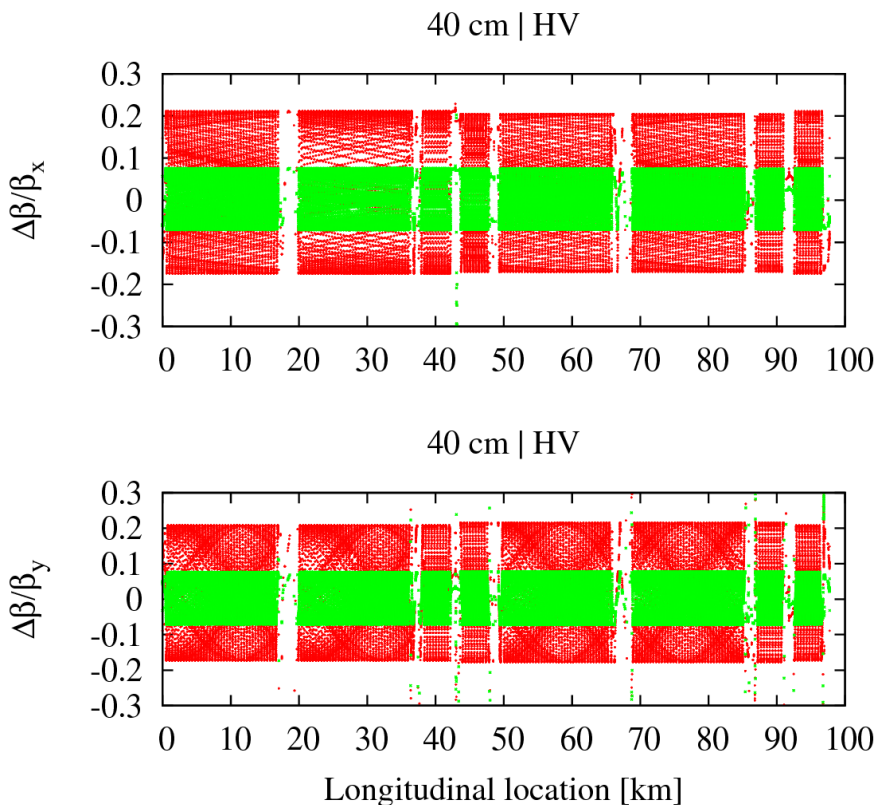


# Linear BB $\beta$ -beating Impact: LHC and HLLHC

- Linear beating from MADX ( $0\sigma$  particles) with head on (HO) interactions in IP1 and 5 and no lattice errors.
- For LHC:  $\xi_{\text{bb}}=0.0037/\text{IP} \Rightarrow \underline{\Delta\beta/\beta \sim 7\%}$  (2IPs)
- For HLLHC:  $\xi_{\text{bb}}=0.01/\text{IP} \Rightarrow \underline{\Delta\beta/\beta \sim 15\%}$  (2IPs) or 24% (3IPs)
- In the **worst case** the beating from BB will **add up** to the beating due to lattice errors (5-7 %). Impossible to know a priori.
- In the HLLHC case since a full crab crossing scenario is considered so the beating is independent on the  $\beta^*$ .
- Collimation experts request  $\Delta\beta/\beta_{\text{max}} < 10\%$  as in the LHC.



# Linear BB $\beta$ -beating Impact: FCC



$$\xi_{bb}=0.03$$

$$\xi_{bb}=0.011$$

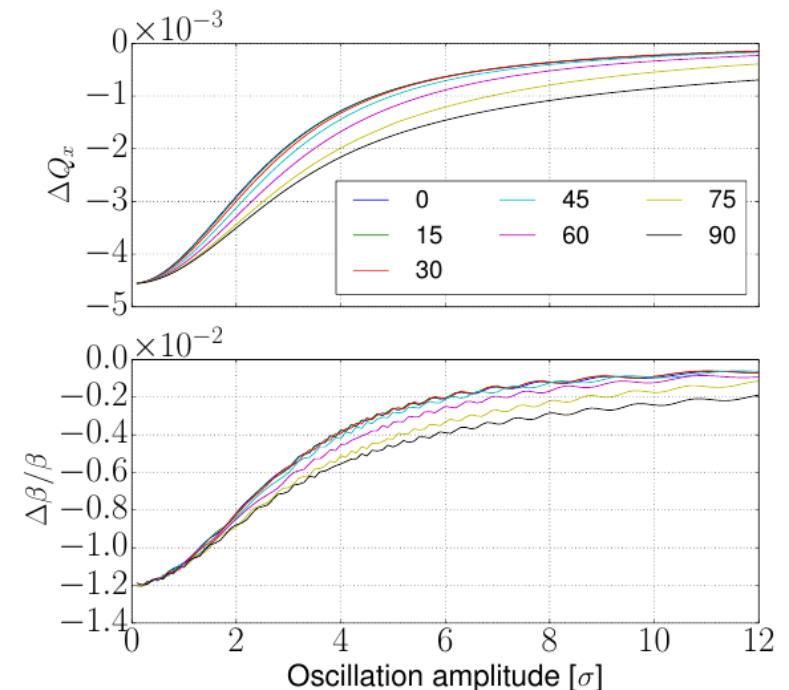
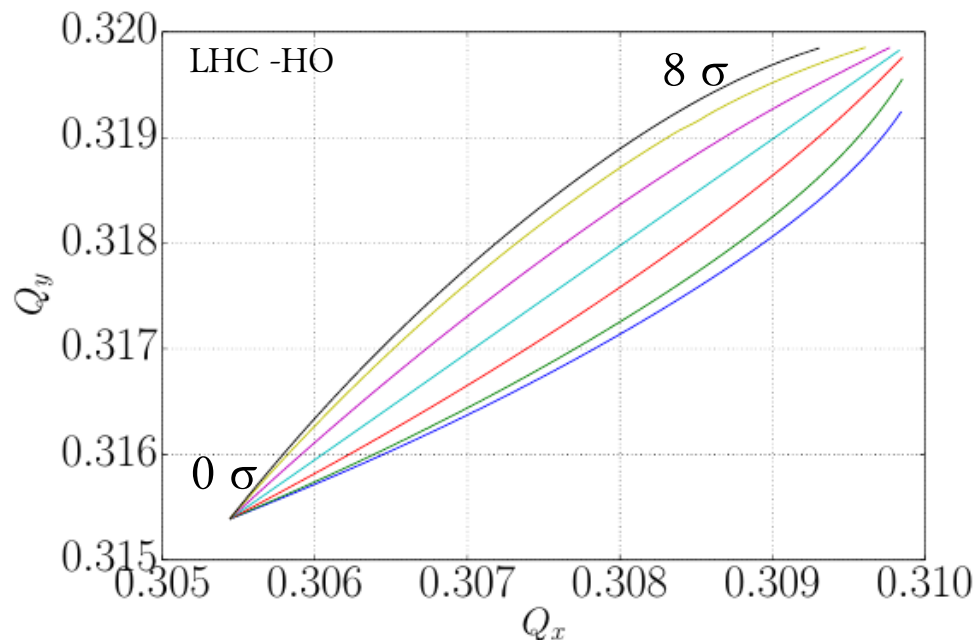
$$\xi_{bb}=0.03$$

$$\xi_{bb}=0.011$$

- Linear beating from MADX ( $0\sigma$  particles) with head on (HO) interactions in IPA and G and no lattice errors.
- Using  $L^*=40\text{m}$  and  $\beta^*=0.3\text{m}$  optics with full crab crossing.
- FCC adds new feature since the  $\xi_{bb}$  changes over the fill and so the beating.
  - $\xi_{bb,tot}=0.011$  (beg. Fill) -  $\Delta\beta/\beta_{max}=\underline{8\%}$
  - $\xi_{bb,tot}=\underline{0.03}$  (max) -  $\Delta\beta/\beta_{max}=\underline{22\%}$ .
- FCC is currently optimizing the phase advances between main experiments @ collision to maximize DA. This optics distortion becomes yet another parameter on the optimization (HO, octupoles,...).
- Collimation experts request  $\Delta\beta/\beta_{max} < 10\%$  as in the LHC.

# Non-linear $\beta$ -beating impact: Head on

- MADX tracking for the LHC case plus SVD analysis (provides effective values for the twiss parameters).
- Limitations for amplitudes  $> 8.3\sigma$  where chaotic motion was found.
- The effective  $\beta$  beating from one IP follows the proportionality to the beam-beam tune shift.
- Beating vanishes asymptotically for large oscillation amplitudes  $\Rightarrow$  halo particles not affected.
- Challenging (impossible?) correction for all amplitudes due to the spread.



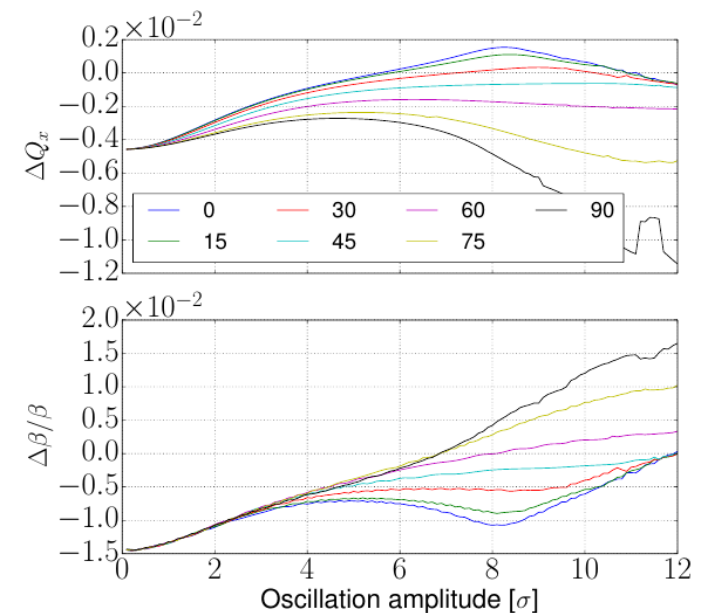
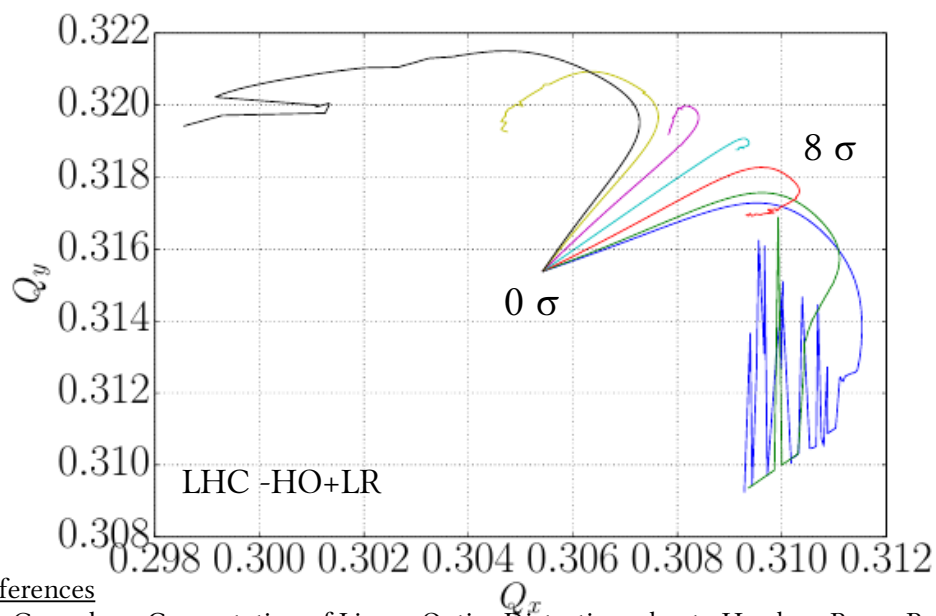
## References

P.J. Gonçalves, Computation of Linear Optics Distortions due to Head-on Beam-Beam Interactions in Hadron Colliders, CERN-THESIS-2015-404

P.J. Gonçalves, Computation of Optics Distortions due to Beam-Beam Interactions in the FCC-hh, CERN-THESIS-2016-317

# Non-linear $\beta$ -beating impact: Long range

- MADX tracking for the LHC case plus SVD analysis (provides effective values for the twiss parameters).
- Unlike for the HO interactions the long-range (LR) are already strong in the LHC in comparison with HLLHC and FCC.
- During LHC operation no impact on cleaning inefficiency was observed at collision.
- The effective  $\beta$  beating does not follow a linear scaling with the tune shift.
- Passive compensation between two main IPs compensate shift from LRs. Not perfect cancellation and some  $\beta$  beating remains. Phase advance between the IPs can be optimized to minimized it.



## References

P.J. Gonçalves, Computation of Linear Optics Distortions due to Head-on Beam-Beam Interactions in Hadron Colliders, CERN-THESIS-2015-404

P.J. Gonçalves, Computation of Optics Distortions due to Beam-Beam Interactions in the FCC-hh, CERN-THESIS-2016-317

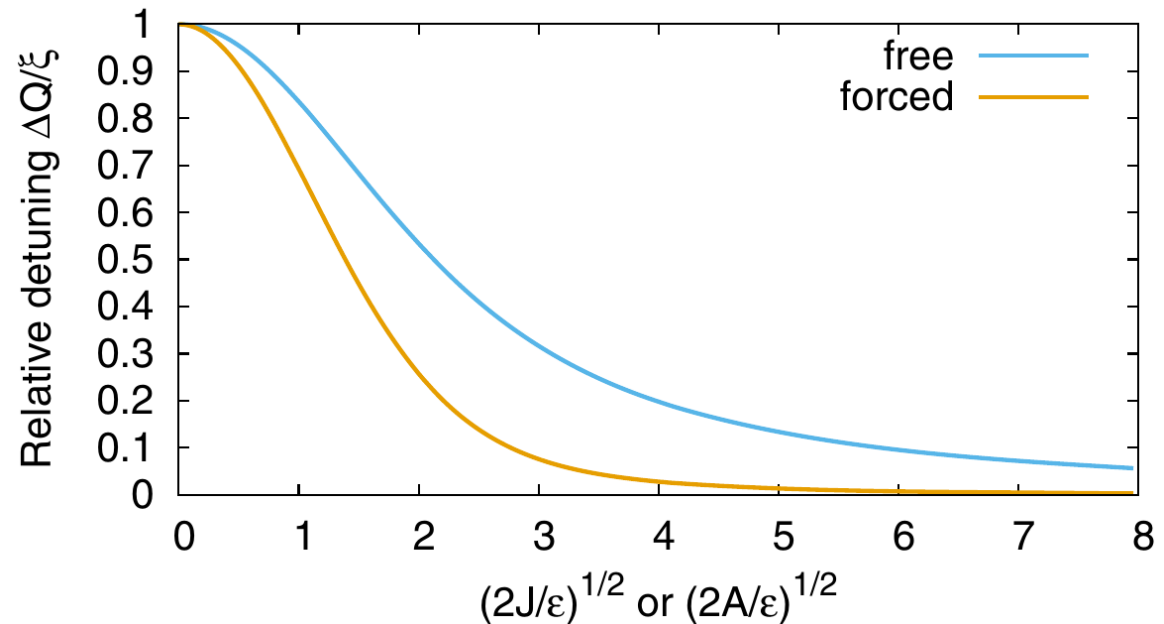
# BB amplitude detuning with forced oscillations

- Can be this effect measured in real operation?
- Recently, some effort was devoted to extend forced oscillations (ADT or AC Dipole) based techniques to take into account the presence of beam-beam interactions (weak-strong regime).
- The free action refers to particles with an offset while for the forced is the oscillation amplitude.
- At small amplitude forced oscillations detune a factor 2 faster than free.

Analytical Detuning

$$Q_x(A_x) = \xi \left[ I_0\left(\frac{A_x}{2\epsilon}\right) - I_1\left(\frac{A_x}{2\epsilon}\right) \right] e^{-\frac{A_x}{2\epsilon}}$$

$$Q_y(A_x) = \xi \left[ I_0\left(\frac{A_x}{2\epsilon}\right) + I_1\left(\frac{A_x}{2\epsilon}\right) \right] e^{-\frac{A_x}{2\epsilon}}$$



## References

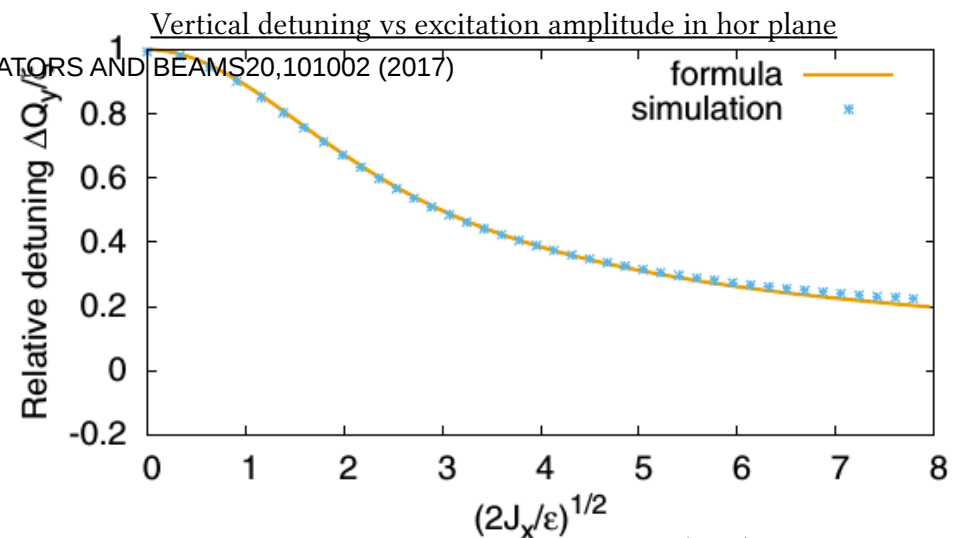
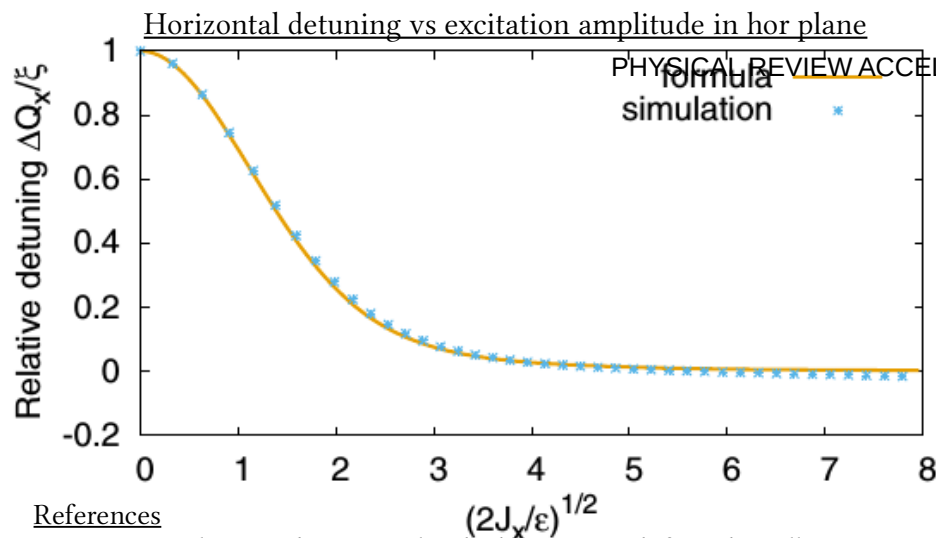
R. Tomas *et al.*, Beam-beam amplitude detuning with forced oscillations, PHYSICAL REVIEW ACCELERATORS AND BEAMS 20, 101002 (2017).

Beam-Beam Effects in Circular Colliders, LBNL February 2018.



# BB amplitude detuning with forced oscillations

- Can be this effect measured in real operation?
- Recently, some effort was devoted to extend forced oscillations (ADT or AC Dipole) based techniques to take into account the presence of beam-beam interactions (weak-strong regime).
- The free action refers to particles with an offset while for the forced is the oscillation amplitude.
- At small amplitude forced oscillations detune a **factor 2** faster than free.
- The forced action is computed from the Fourier amplitude of the spectral line with the forced tune during the excitation plateau.
- Analytical detuning (single particle) benchmarked against MADX tracking (weak-strong) showing very good quantitative agreement for  $0\sigma$  particles.



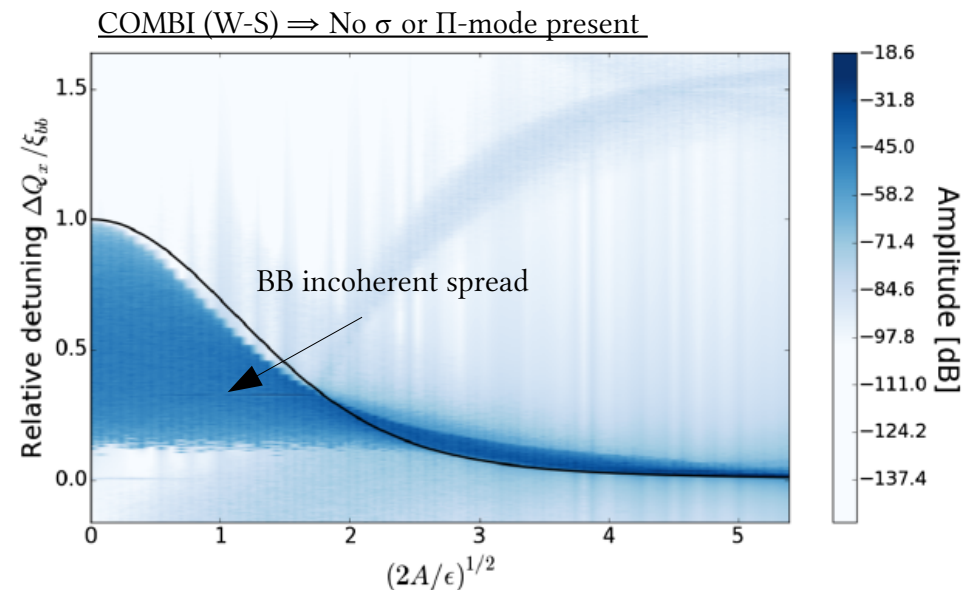
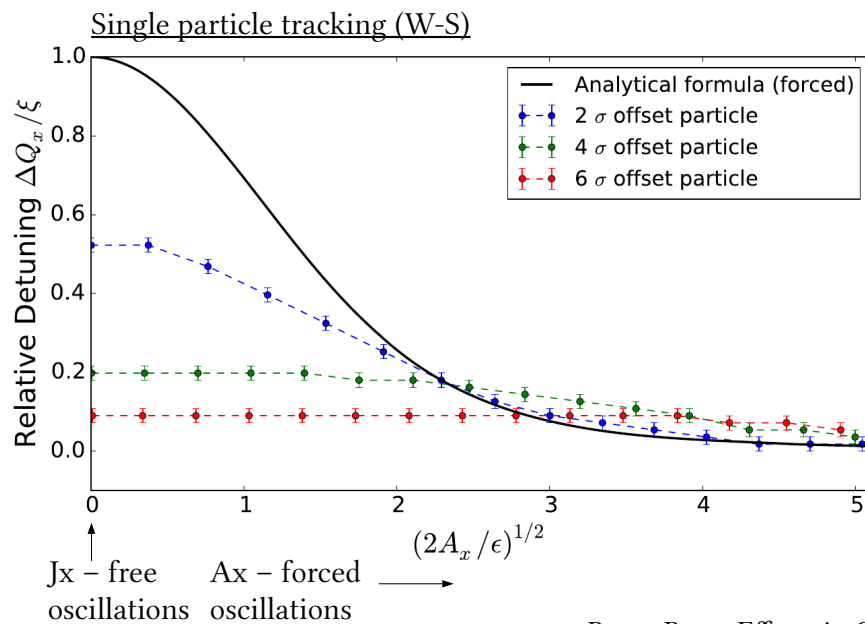
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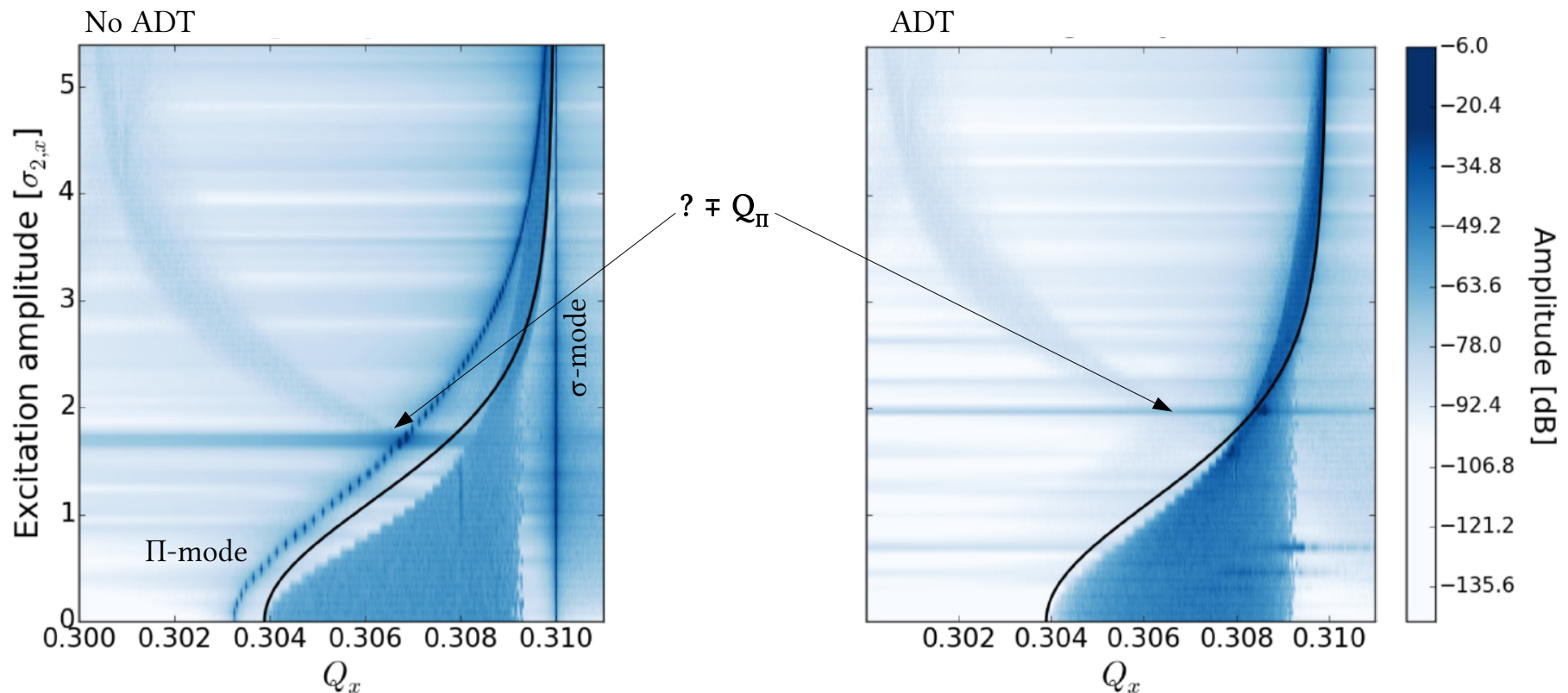
# BB amplitude detuning with forced oscillations

- However the forced detuning is amplitude dependent. Particles with larger free action feature a weaker detuning versus the forced action.
- Between  $2\sigma$  and  $3\sigma$  non-zero amplitude cross the analytical formula ( $J_x = 0$ ). This is explained from shape of the BB force since its derivative changes sign  $\sim 1.6\sigma$ .
- The analytical formula should represent the upper boundary of the incoherent spectrum below  $2\sigma$  and the lower boundary for forced oscillations above  $3\sigma$  (in the plane of excitation).
- In the non-excited plane the analytical formula represents always the upper boundary.
- Self-consistent simulations with COMBI (upgraded with an AC Dipole element) in weak-strong regime confirm the single particle tracking results.



# BB amplitude detuning with forced oscillations

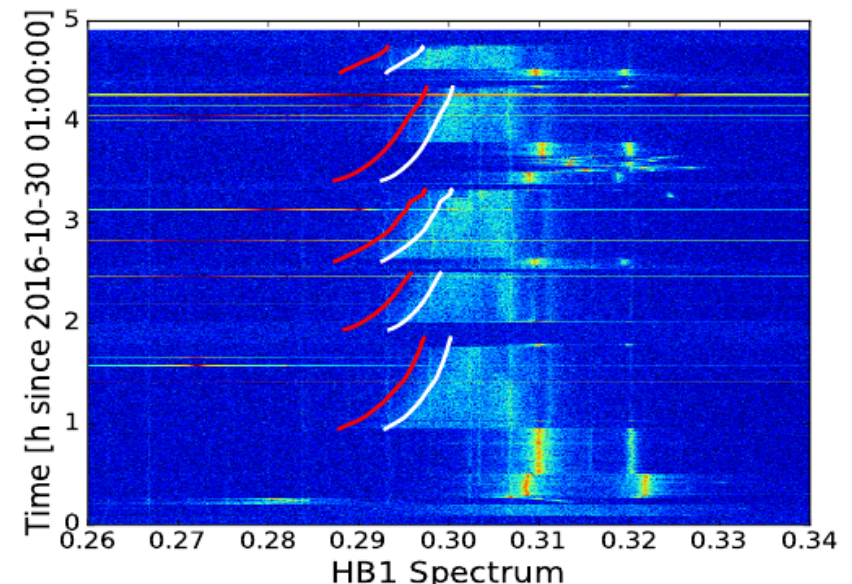
- Another way of forcing a weak-strong configuration is set up the ADT with strong gain.
- The coherent modes are clearly suppressed. However some modes are excited around  $1.8\sigma$  apparently following the  $\Pi$ -mode. Still further analysis is needed.
- The presence of a large incoherent spread is not compatible with single particle models to compute the  $\beta$  beating from AC dipole measurements even in W-S regime. Only the boundary of low oscillation amplitude particles can be predicted.



# Measurement of LHC HO $\beta$ -beating

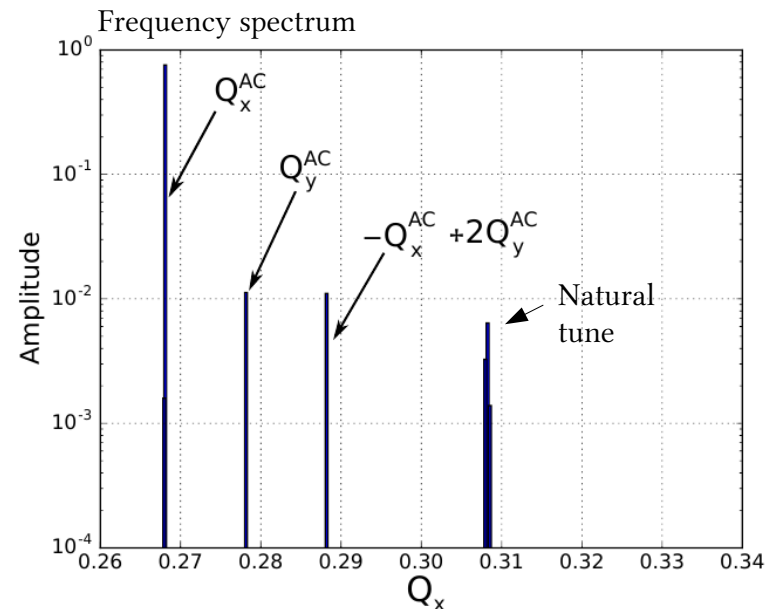
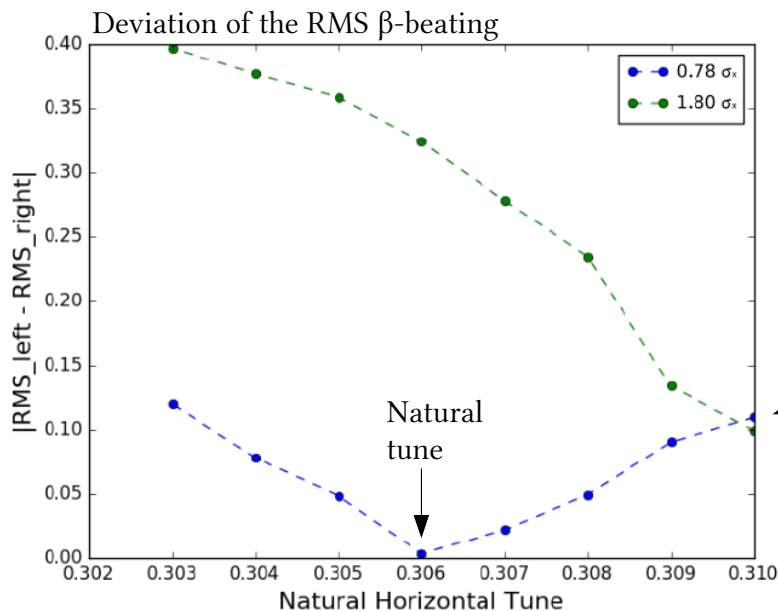
- Is it possible to measure this effect on the LHC?
- A 8h LHC MD was devoted to this purpose at the end of October 2016.
- Bunches were collided at injection energy with collision tunes.
- Weak-strong regime was chosen to avoid coherent effects. Large asymmetry on intensities.
- Collision tunes @ injection.  $\beta^*=11\text{m}$  and  $\theta=340\ \mu\text{rad}$ .
- Forced oscillations with ADT and AC dipole.
- The ADT allows to excite for longer periods ( $\sim 5$  times)
- Very small bunches were delivered by the injectors ( $\epsilon < 1\mu\text{m}$ ) to maximize  $\xi_{\text{bb}}$ , however wire measurements have 20% uncertainty in that range.
- BBQ plots show the effect of the underestimated emittance in terms of  $\Delta q_{\text{bb}}$ . Measurements (red) predicts larger shift than corrected (white).

Parameter	Value
$\beta^*[\text{m}]$	11
$\theta[\mu\text{rad}]$	340
E[GeV]	450
$Q_{x,y}$	0.31/0.32
$I_{1,2}[10^{11}\ \text{ppb}]$	0.07/1.05
ADT[turns]	29000
AC Dipole	6600



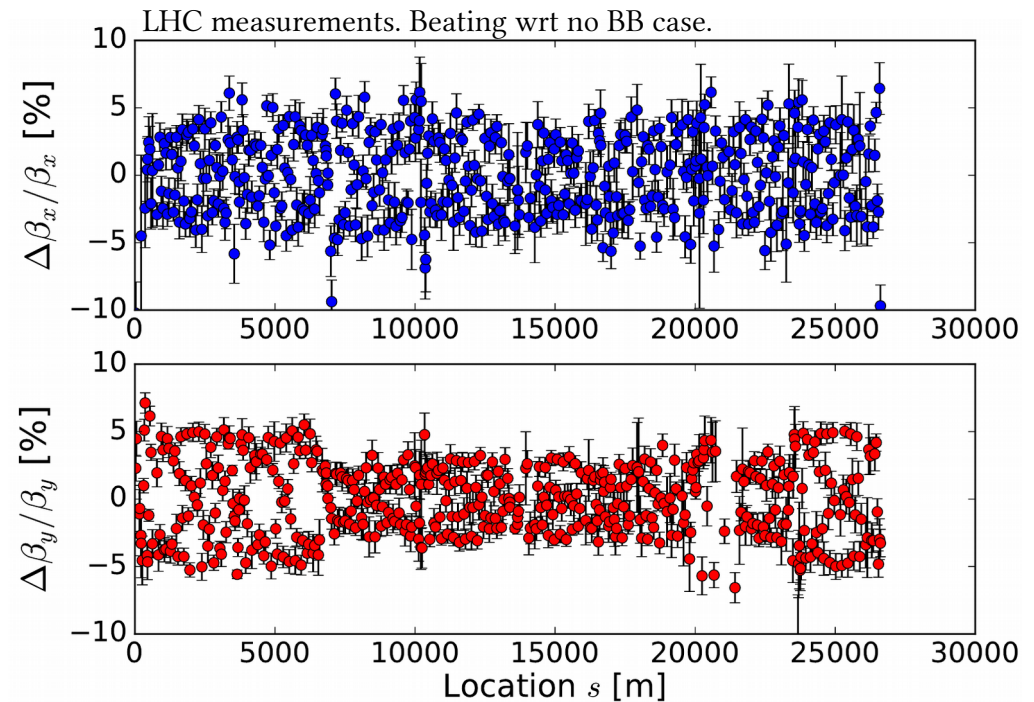
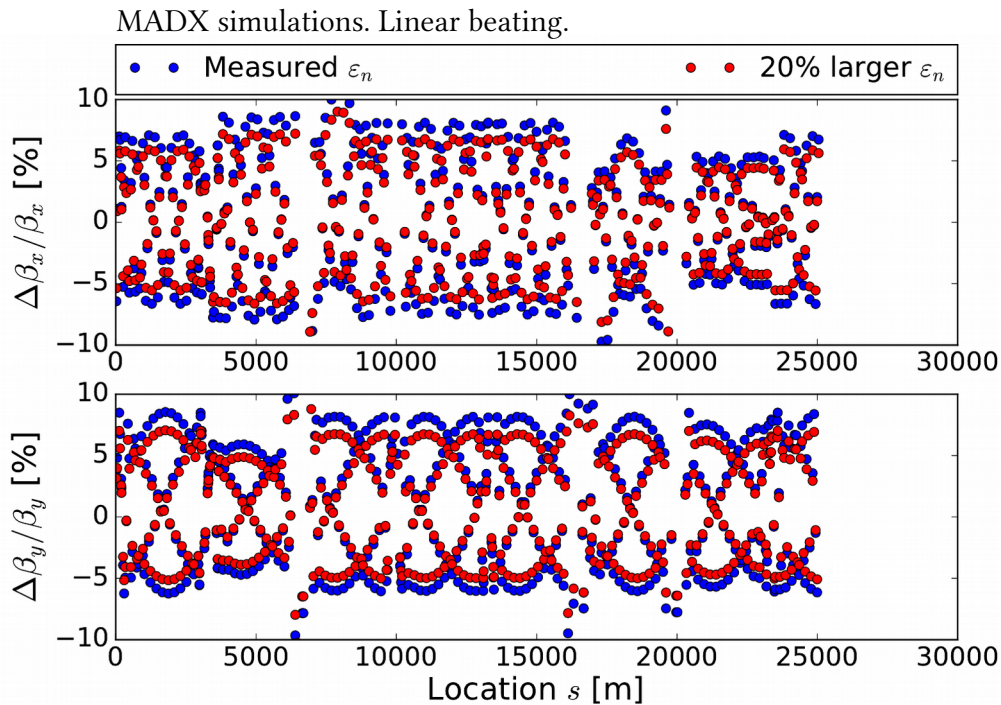
# Measurement of LHC HO $\beta$ -beating

- Optics reconstruction from measurements are based on the existence of a tune representative (natural tune) for the whole bunch. Not evident with BB since large spread of tunes is present.
  - Three methods:
    - Direct observation of the natural tune in the frequency spectrum
    - Deviation of the RMS  $\beta$ -beating on both sides of the AC/ADT.
    - Minimize phase advance deviations from the AC/ADT location (OMC GUI segment-by-segment)
- } Scan tune until perturbation from ADT/AC is compensated for.
- However not conclusive for all measurements. Developments required take into account the tune spread from the BB interaction.



# Measuring $\beta$ -beating in the LHC

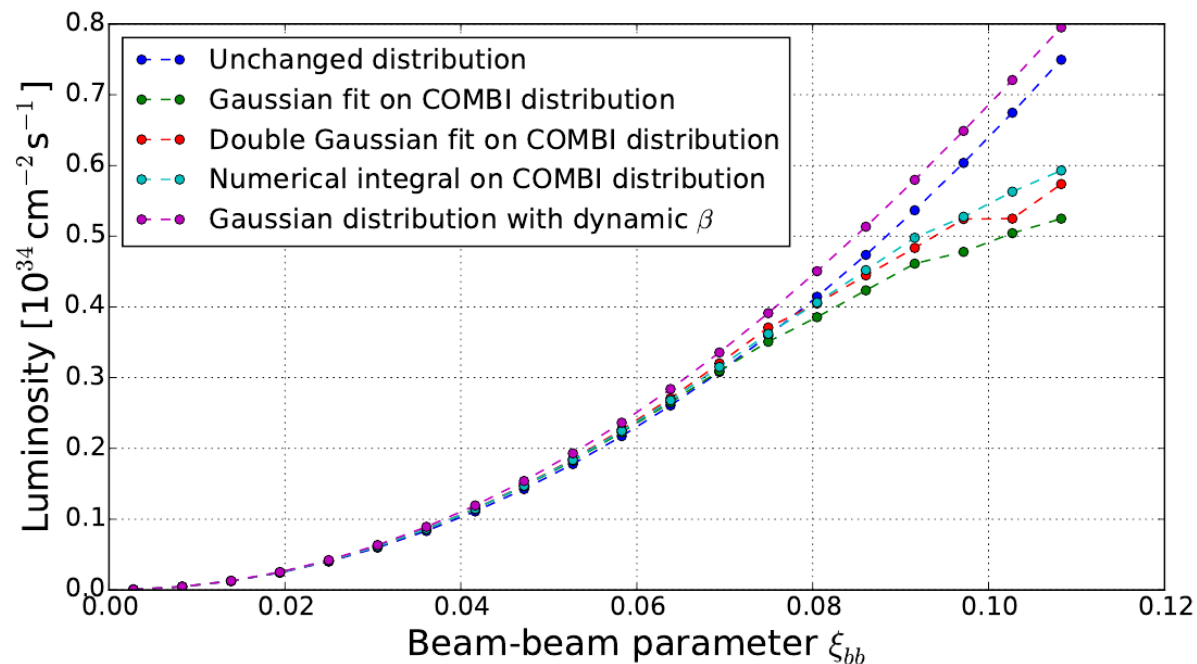
- First successful BB induced  $\beta$ -beating measurement ever.
- Measurements (beating wrt no BB case) and MADX simulations (linear beating wrt perfect machine) agreed qualitatively.
- Reconstruction methods have to be revisited with BB spread and MD should be repeated with correction schemes in the future.



$$1\text{IP} \mid \Delta Q \sim 0.013 \mid Q_{AC} = (0.268, 0.278) \mid A_{AC} = 1.8 \sigma$$

# Impact on the luminosity

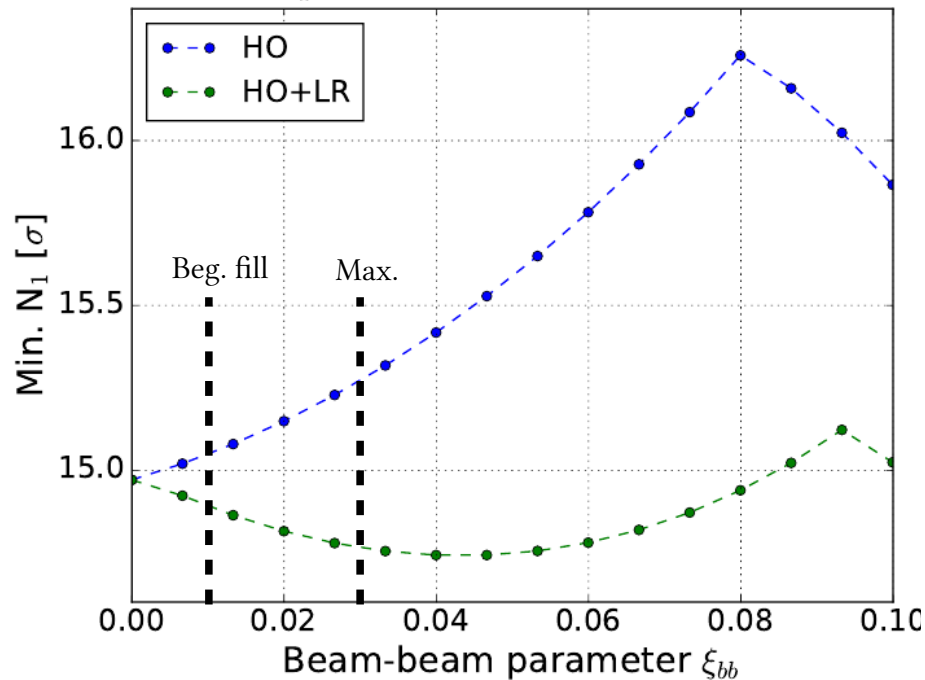
- The BB interact will not only modify the optics @ the IP ( $\beta^*$ ) but as well the distribution itself.
- Luminosity is typically evaluated assuming Gaussian distributions. **Is this the case in strong  $\xi_{bb}$  regimes?**
- Gain in luminosity predicted by dynamic  $\beta$  distribution valid for all cases for  $\xi_{bb} < 0.07$
- Deviation from Gaussian regime above  $\xi_{bb} \sim 0.07$
- Luminosity from double Gaussian  $\approx$  numerical integration  $\forall \xi_{bb}$



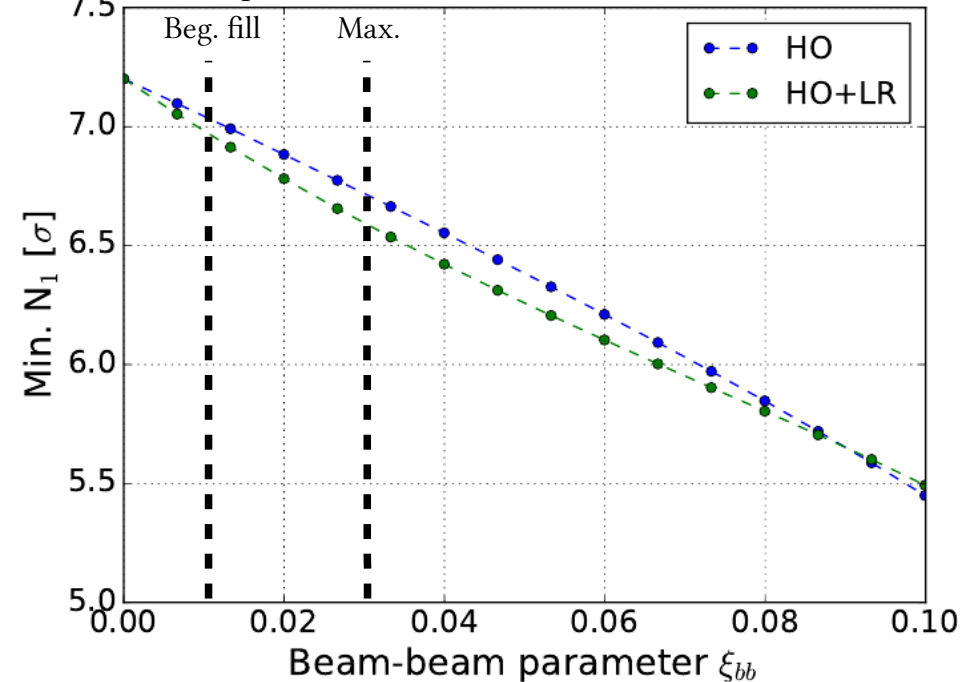
# Impact on Machine aperture

- We explore the impact on machine and collimator apertures for various  $\xi_{bb}$ . Only linear beating is considered (worst case).
- Machine aperture bottleneck in separation dipole MBRD.B4RA.H1.
  - For HO only no aperture decrease for expected  $\xi_{bb}$  FCC range [0.01-0.03].
  - For HO+LRs there is a decrease of  $\sim 0.25 \sigma$  for max  $\xi_{bb}=0.03$ .
- TCPs aperture bottleneck TCP.B6L2.B1 (for  $\xi_{bb}=0.01$  HO,  $\xi_{bb}=0.016$  HO+LRs) then TCP.A6L2.B1. For  $\xi_{bb}=0.03$ , a decrease of  $\sim 0.6 \sigma$  is observed.

Machine Aperture Bottleneck



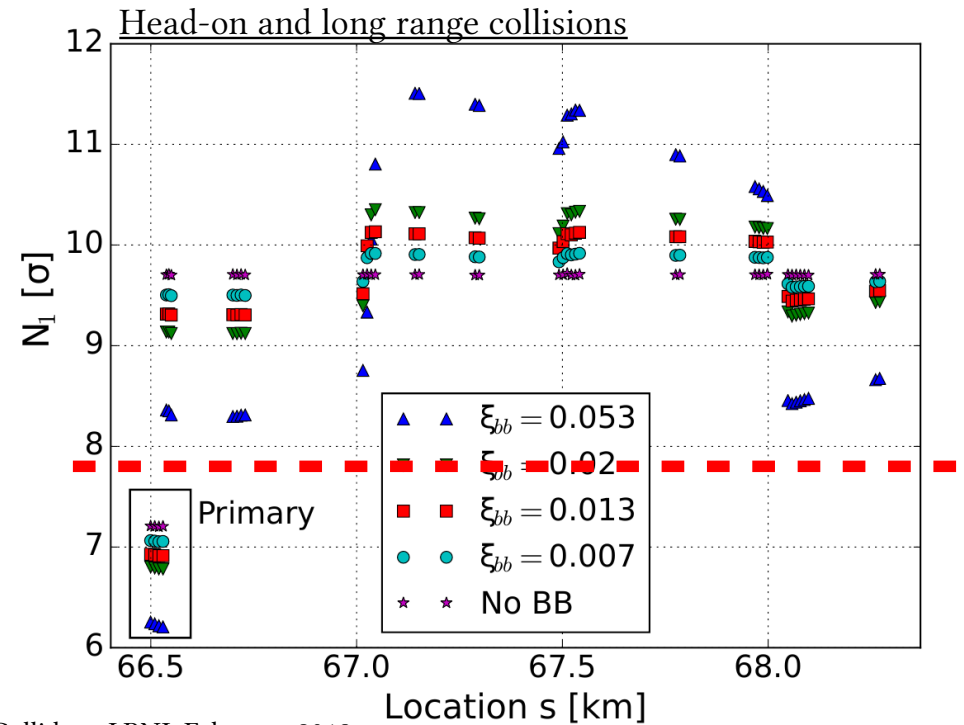
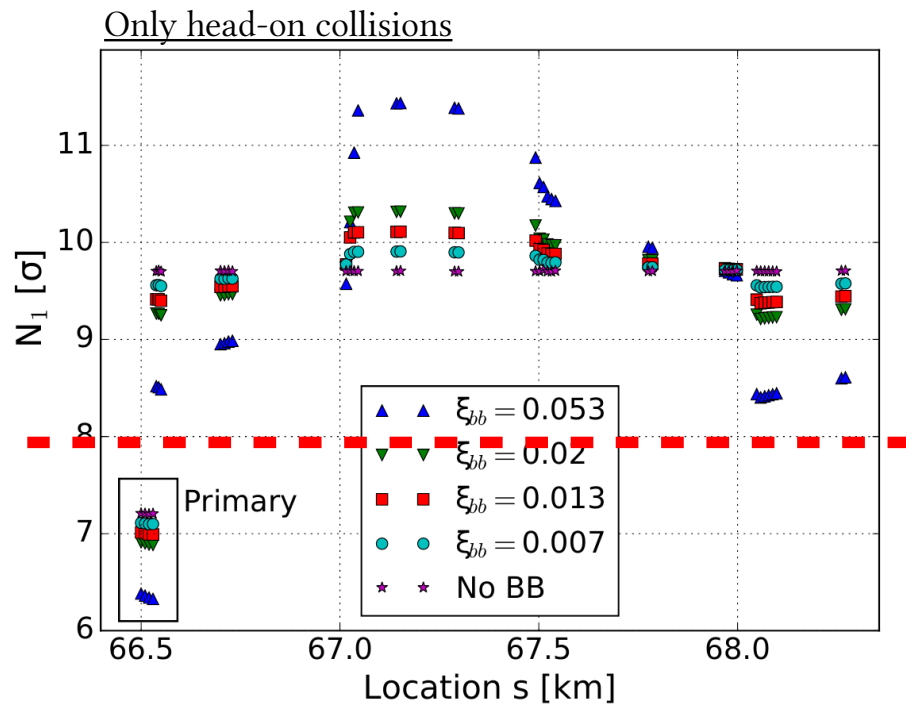
TCPs Aperture Bottleneck





# Collimation hierarchy

- We explore the impact on machine and collimator apertures for various  $\xi_{bb}$ . Only linear beating is considered (worst case).
- Primaries set @  $7.2\sigma$  and secondaries @  $9.7\sigma$ . Only betatron collimation considered.
- The collimation hierarchy is preserved, even for high  $\xi_{bb}$ . However apertures are strongly perturbed.
- The usual beam loss maps including BB are needed to evaluate the impact of these distorted apertures.
- Simulations with SixTrack and BB are under discussion with FCC collimation experts. The tracking should be realistic in terms of amplitude detuning from BB.



# Summary and Outlook

- The distortion of the linear optics due to beam-beam interactions will be non-negligible for the HL-LHC and FCC. Correction is possible (see L. Medina IPAC17), however they only apply to small amplitude particles increasing  $\beta$  beating for particles in the tail.
- Single particle approach does not provide a recipe for determining the “natural tune” for optics reconstruction. Theoretical developments are needed to take into consideration BB tune spreads.
- First AC dipole measurements at injection with large  $\xi_{bb}$  and only HO show qualitative agreement with MADX simulations.
- Preliminary studies with linear  $\beta$ -beating shows no loss of hierarchy in the collimation system even for very large  $\xi_{bb}$ .
- Realistic beam loss maps including beam-beam interaction and collimation system with SixTrack are being planned with the FCC experts.

The possibility to use an e-lens to compensate the  $\beta$ -beating is considered and will be investigated