

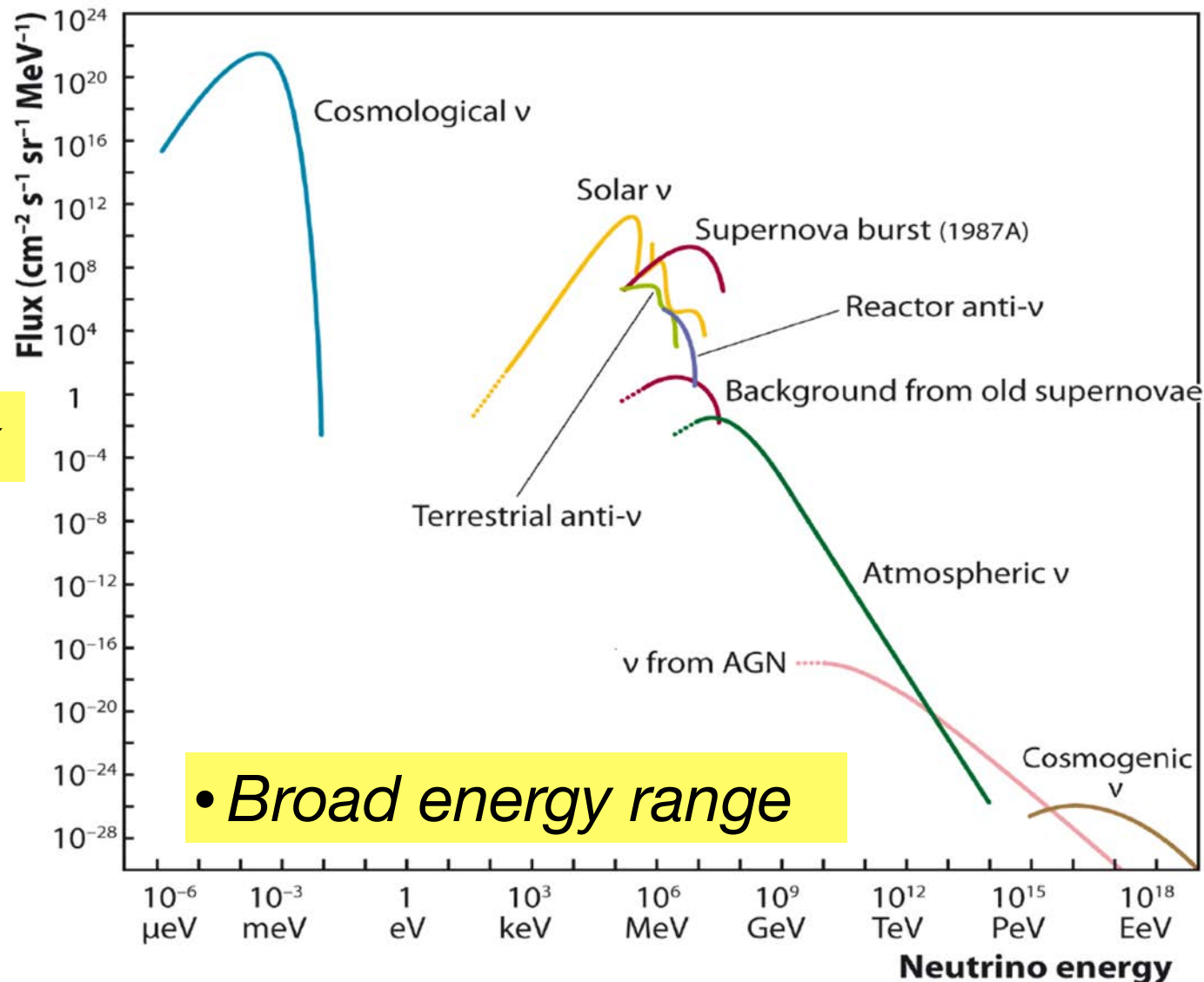
# UC Berkeley P290e

# How to “see” a neutrino?

Alan Poon  
2017.09.27

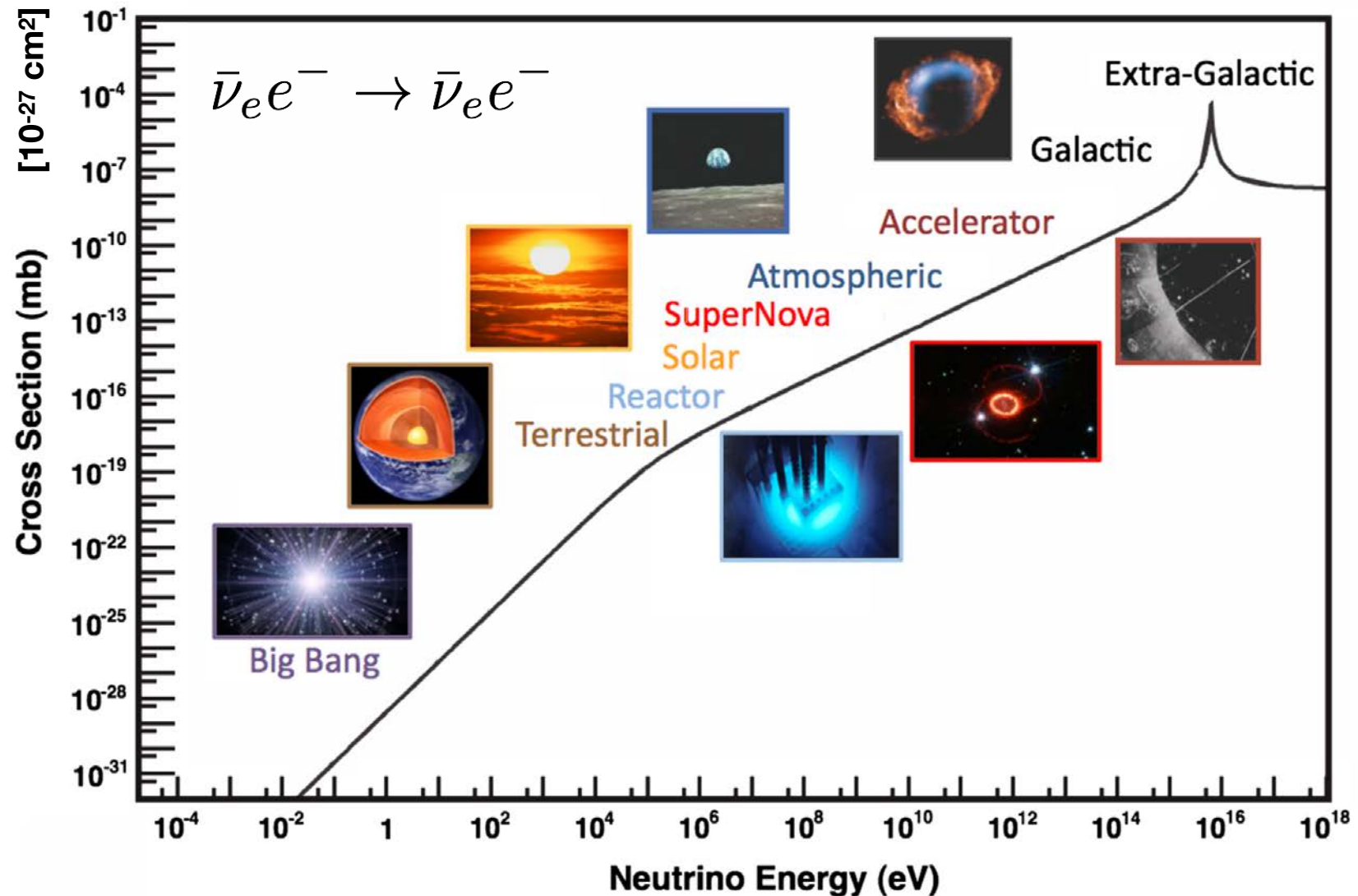
# Neutrino Sources

Most neutrino sources are natural (not from accelerators and reactors)



# Why is it so hard to detect neutrinos?

Neutrinos participate only in weak interactions



# Why is it so hard to detect neutrinos?

- Look for its decay?  
**(AFAIK) Neutrinos don't decay**

- Look for its interactions?

**Ex: 1-MeV  $\bar{\nu}_e$  scattering of atomic electrons in Pb:**

$$\lambda = \frac{1}{\rho\sigma} \quad \text{attenuation length}$$

$$\rho = \frac{(82 \text{ e/atom})(11.3 \text{ g/cm}^3)(6.02 \times 10^{23} \text{ atom/mole})}{(207 \text{ g/mole})} = 2.7 \times 10^{24} \text{ e/cm}^3$$

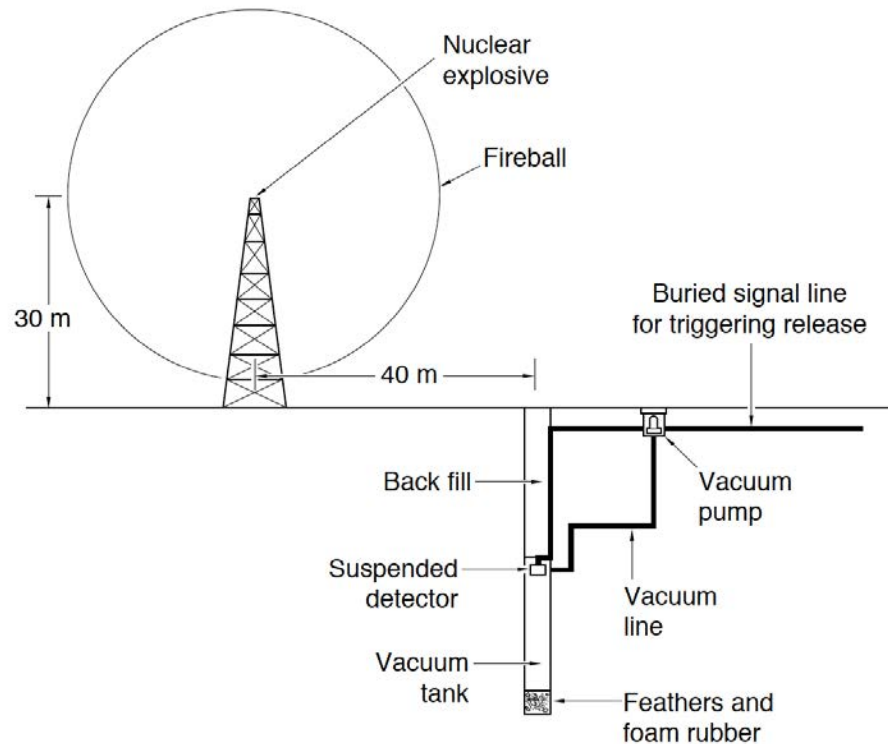
$$\sigma \sim 10^{-43} \text{ cm}^2 \text{ @ 1 MeV}$$

$$\lambda \sim 4 \times 10^{16} \text{ m} = 4 \text{ light years}$$

**Need:  
HUGE flux  
HUGE target**



# An explosive idea - Reines and Cowan



**Figure 1. Detecting Neutrinos from a Nuclear Explosion**

Antineutrinos from the fireball of a nuclear device would impinge on a liquid scintillation detector suspended in the hole dug below ground at a distance of about 40 meters from the 30-meter-high tower. In the original scheme of Reines and Cowan, the antineutrinos would induce inverse beta decay, and the detector would record the positrons produced in that process. This figure was redrawn courtesy of Smithsonian Institution.

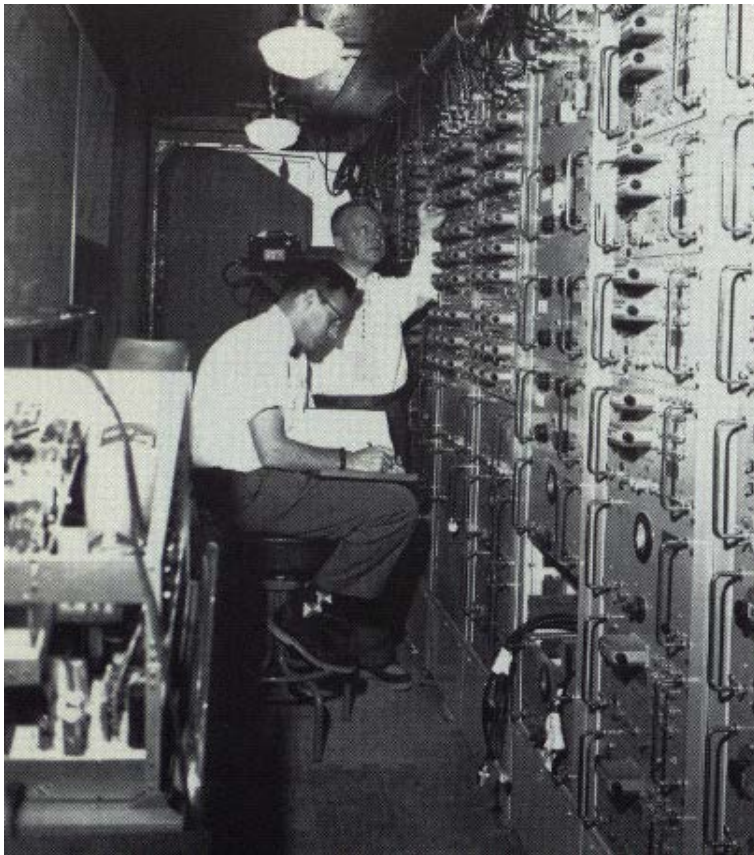
“Our crude knowledge of the expected energy spectrum of neutrinos from a fission bomb suggested that the inverse beta decay reaction would occur several times in a several-ton detector located about 50 meters from the tower-based explosion of a 20-kiloton bomb. (Anyone untutored in the effects of nuclear explosions would be deterred by the challenge of conducting an experiment so close to the bomb, but we knew otherwise from experience and pressed on). The detector we dreamed up was a giant liquid scintillation device, which we dubbed ‘El Monstro.’ This was a daring extrapolation of experience with the newly born scintillation technique. The biggest detector until Cowan and I came along was only a liter or so in volume.”

**- Fred Reines**

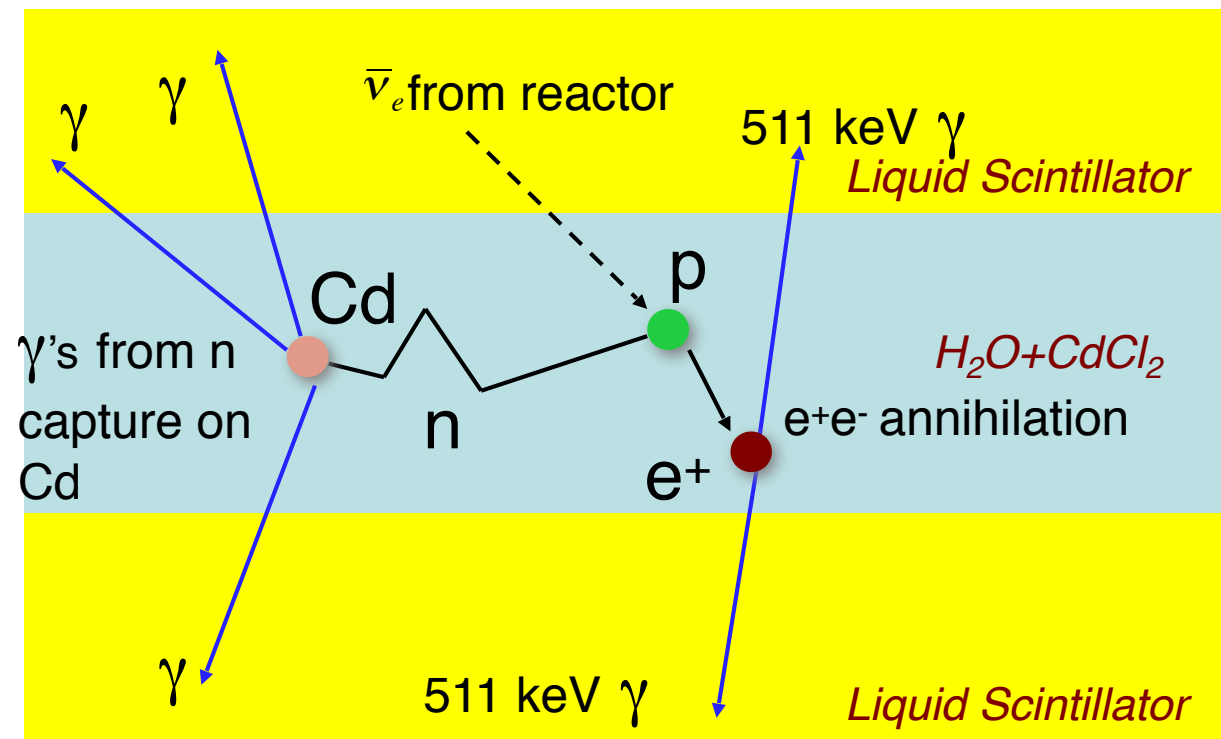
**Reines and Cowan scrapped this idea.**

# Discovery of the (Anti-)Neutrinos

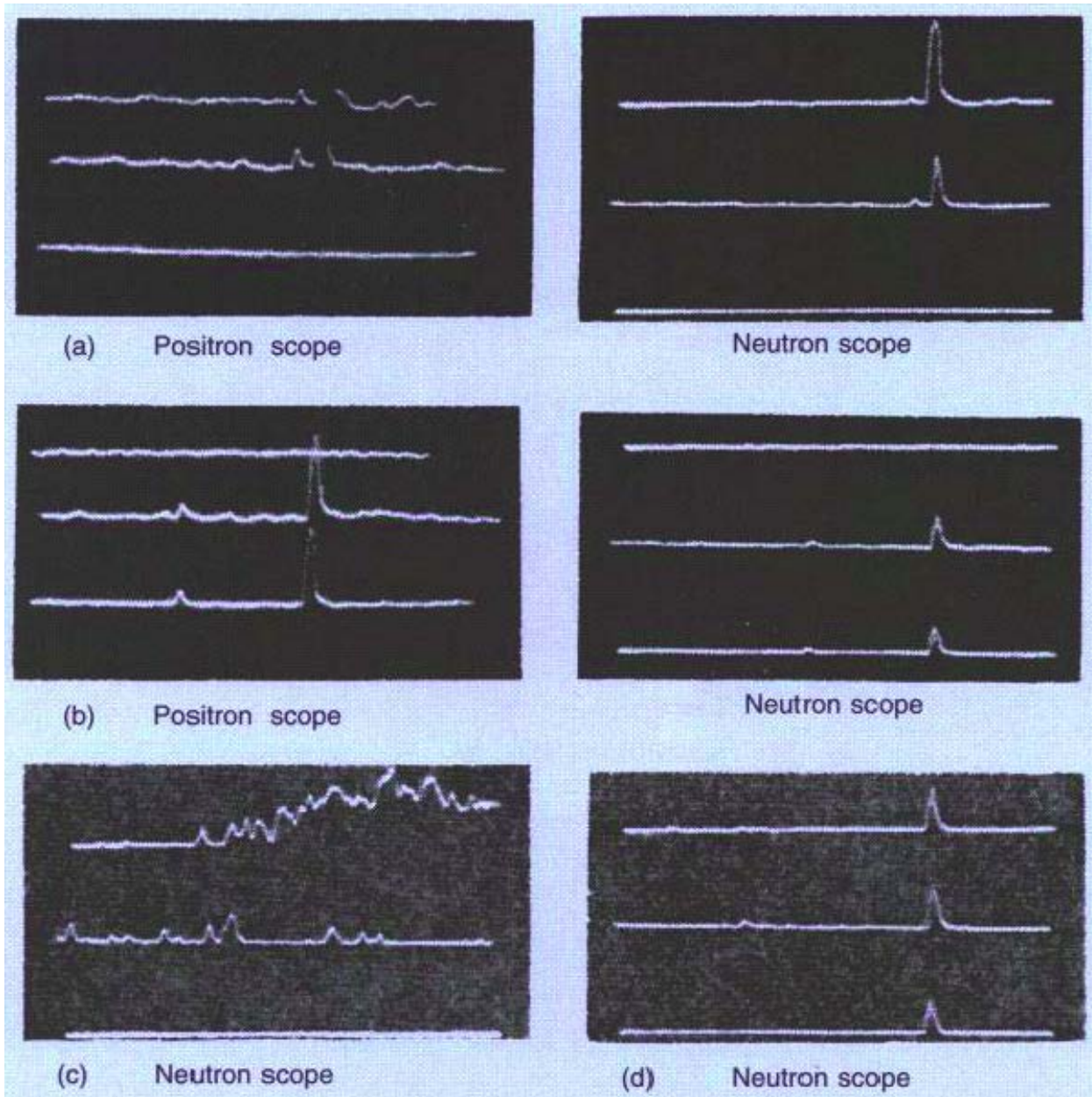
- F. Reines & C.L. Cowan [*Physical Review* 117, 160 (1960)]
- Detection at Savannah River reactor plant



## Inverse Beta Decay



# “Saw” the coincidences!



neutrino

neutrino

noise

cosmic ray

**Leptonic processes  
and  
coherent elastic neutrino-nucleus scattering**

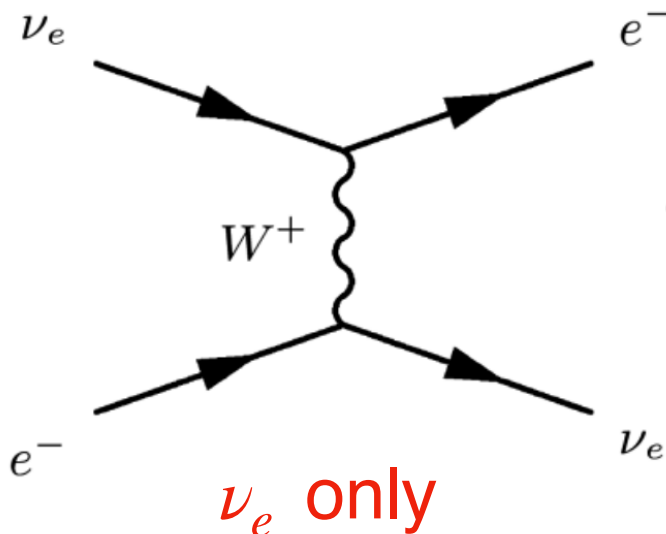


# Neutrino-electron scattering

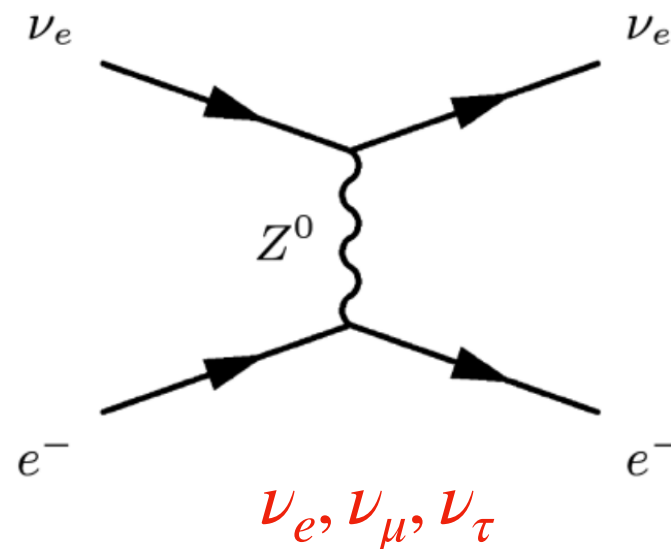
Targets have a lot of atomic electrons

Tree level diagrams:

**Charged Current (CC)**



**Neutral Current (NC)**



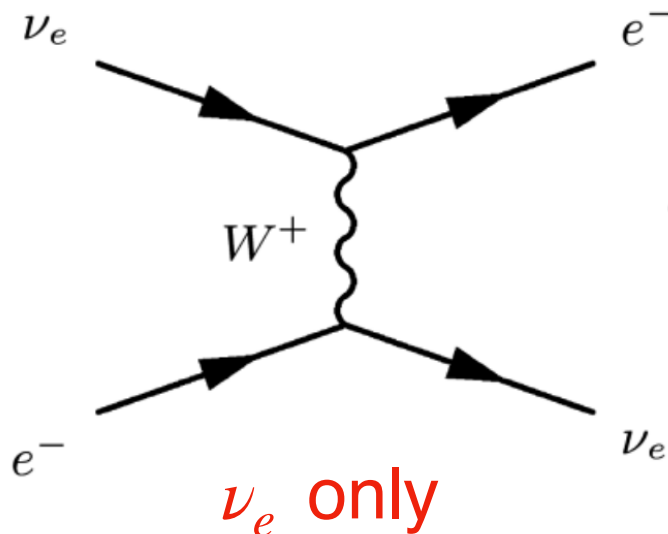
$$\mathcal{L} = -\frac{G_F}{\sqrt{2}}[\bar{\nu}_e\gamma^\mu(1-\gamma^5)e][\bar{e}\gamma_\mu(1-\gamma^5)\nu_e] + [\bar{\nu}_e\gamma^\mu(1-\gamma^5)\nu_e][\bar{e}\gamma_\mu(g_V^e - g_A^e\gamma^5)e]$$

# Neutrino-electron scattering

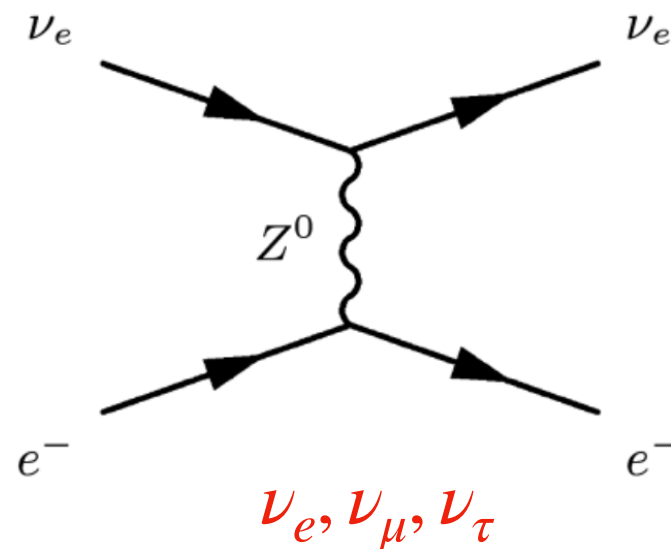
Targets have a lot of atomic electrons

Tree level diagrams:

**Charged Current (CC)**



**Neutral Current (NC)**



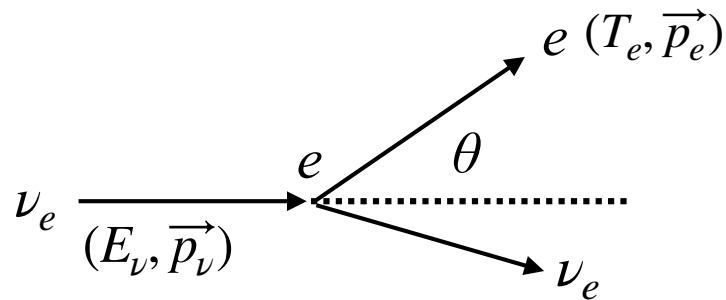
$$\sigma = \frac{2G_F^2 m_e}{\pi} \left[ (g_L^2 + \frac{g_R^2}{3} E_\nu) - \frac{g_L g_R}{2} m_e \right]$$

$$g_L = \sin^2 \theta_W \pm_{\mu, \tau}^e \frac{1}{2}$$

$$g_R = \sin^2 \theta_W$$

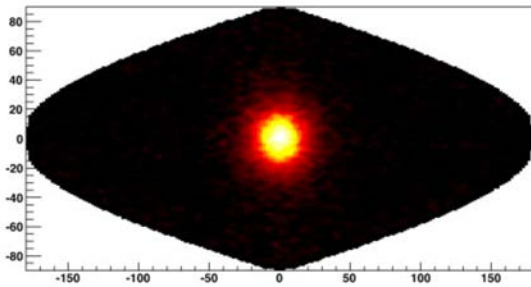
$$g_L \leftrightarrow g_R \text{ for } \bar{\nu}$$

# Neutrino-electron scattering



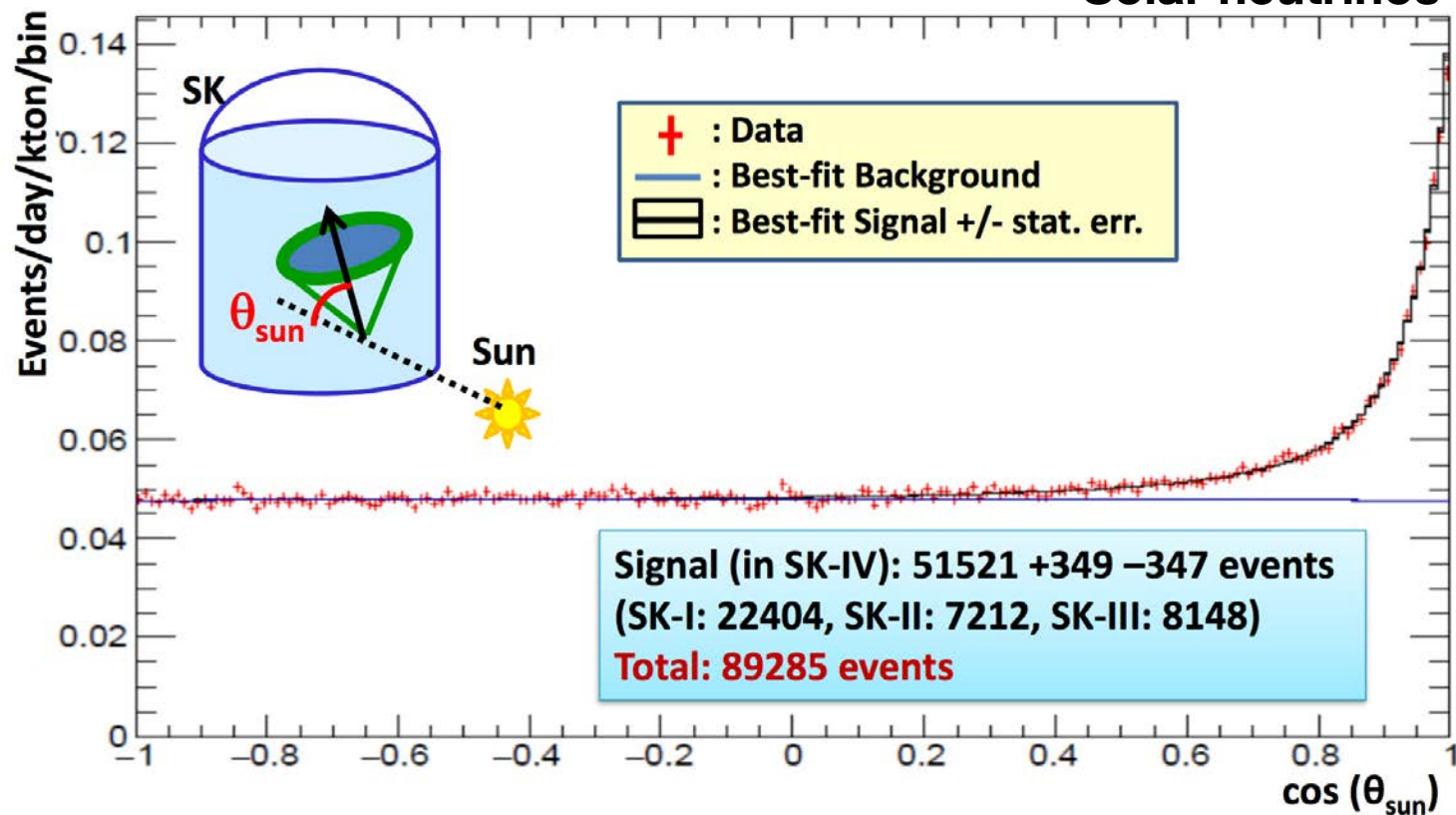
$$T_e = \frac{2m_e E_\nu^2 \cos^2 \theta}{(m_e + E_\nu)^2 - E_\nu^2 \cos^2 \theta}$$

- Electron emitted at very small angle with respect to the neutrino direction :  $E_e \theta_e^2 \leq 2m_e$



Solar neutrino image

Solar neutrinos

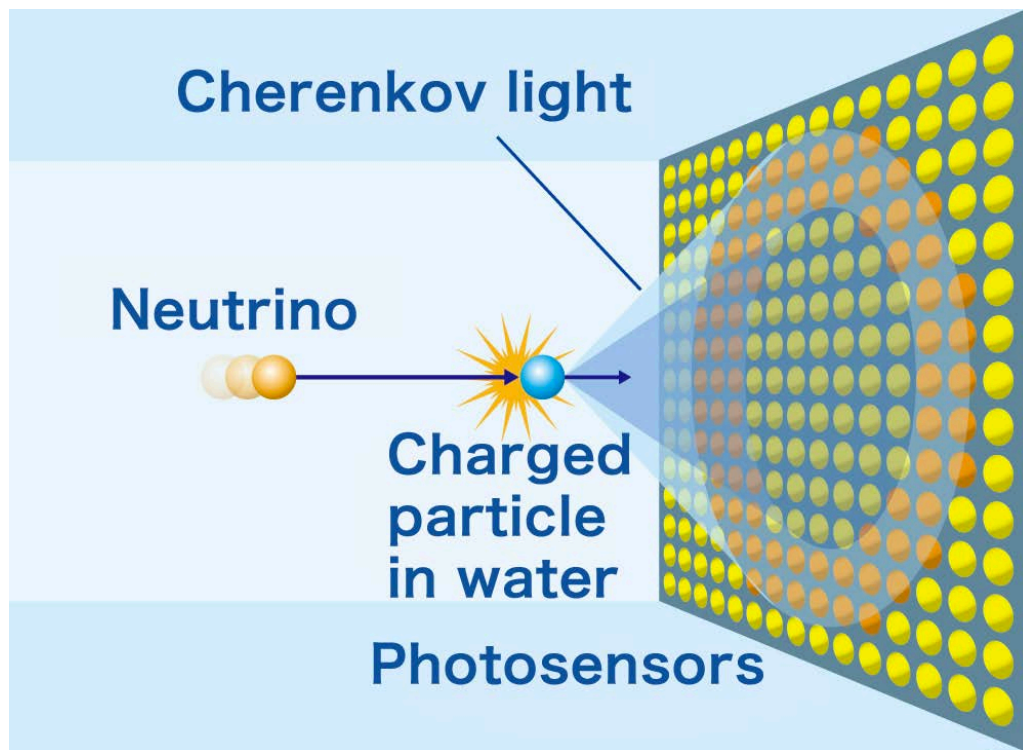


# Cherenkov radiation - seeing relativistic charged particles

Cherenkov light is emitted when a charged particle passes through a dielectric medium at a speed higher than the speed of light in that medium.

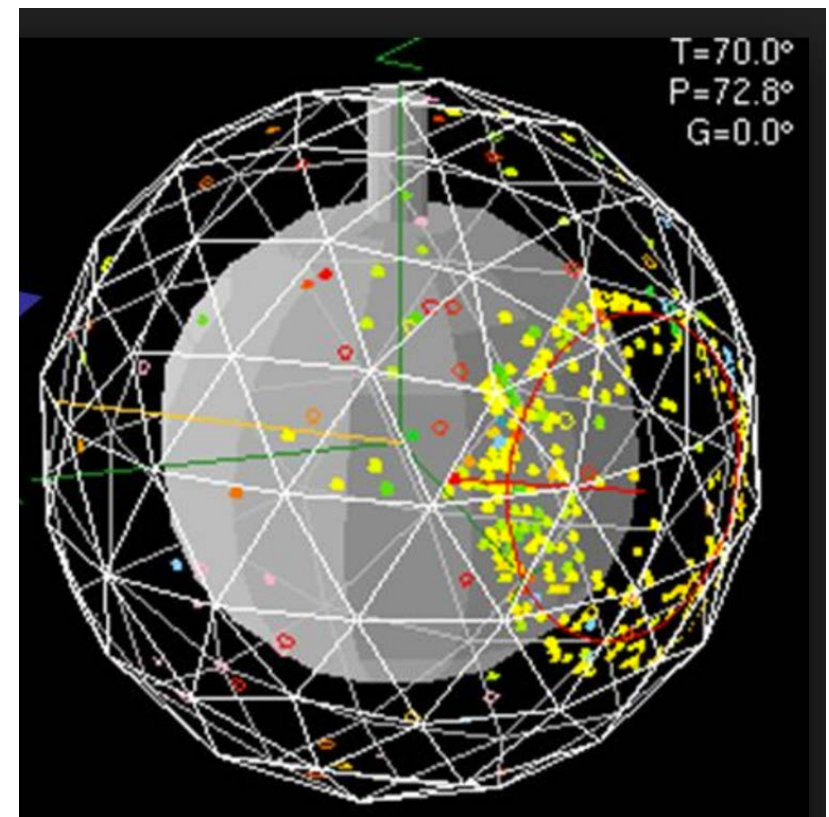
$$\cos \theta_C = \frac{1}{\beta n}$$

$$\theta_C = 41^\circ \text{ in H}_2\text{O } (\beta \sim 1)$$



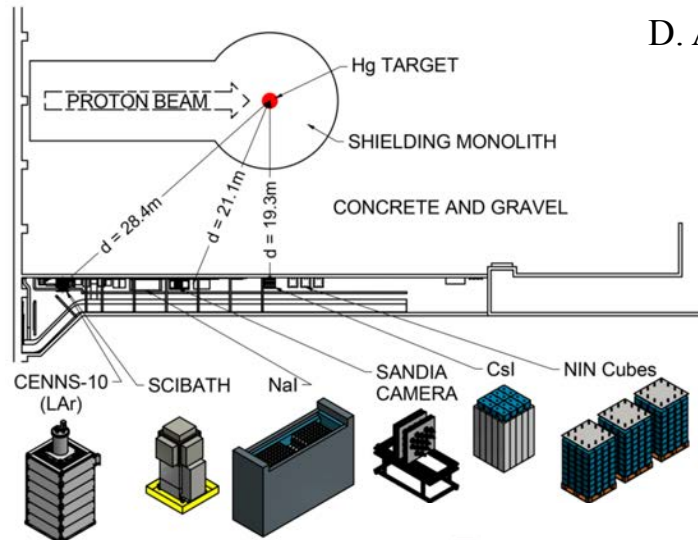
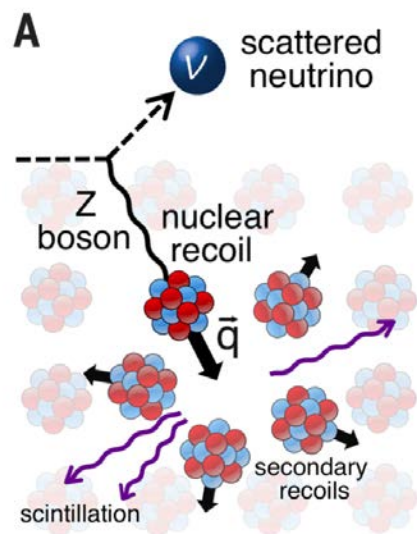
Graphics from <http://physicsopenlab.org/>

Event in SNO





# Coherent Elastic Neutrino-Nucleus Scattering



D. Akimov et al., Science 10.1126/science.aao0990 (2017).

Science

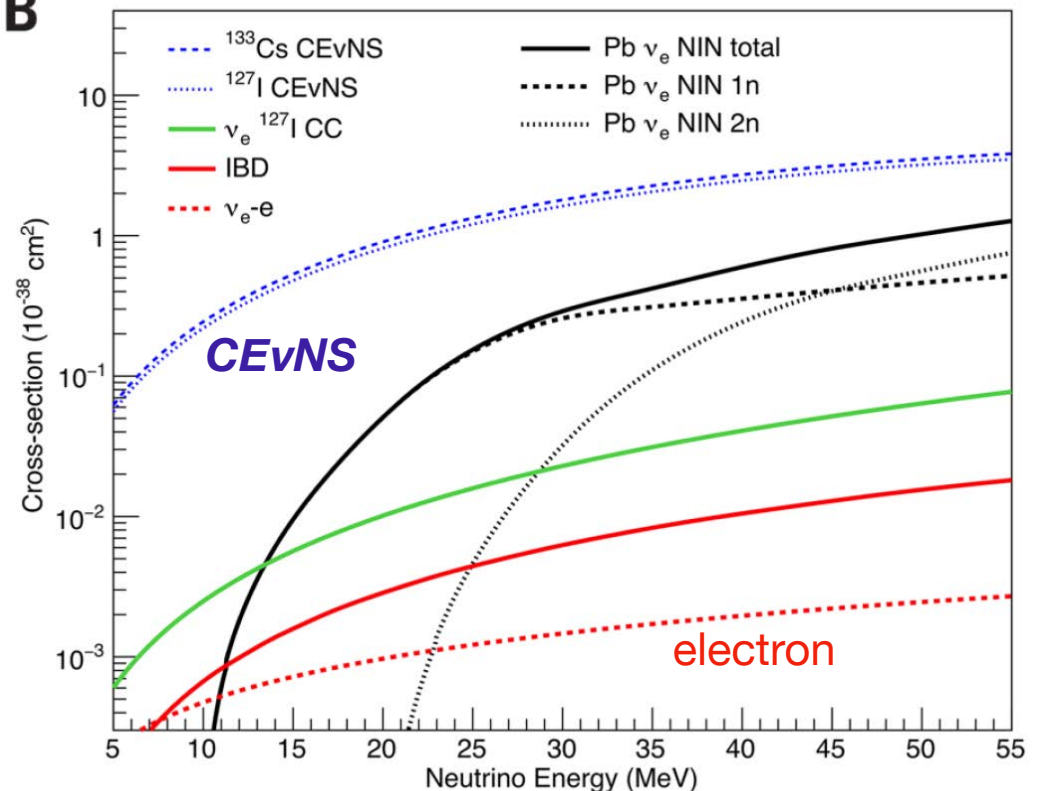
REPORTS

Cite as: D. Akimov et al., Science 10.1126/science.aao0990 (2017).

## Observation of coherent elastic neutrino-nucleus scattering

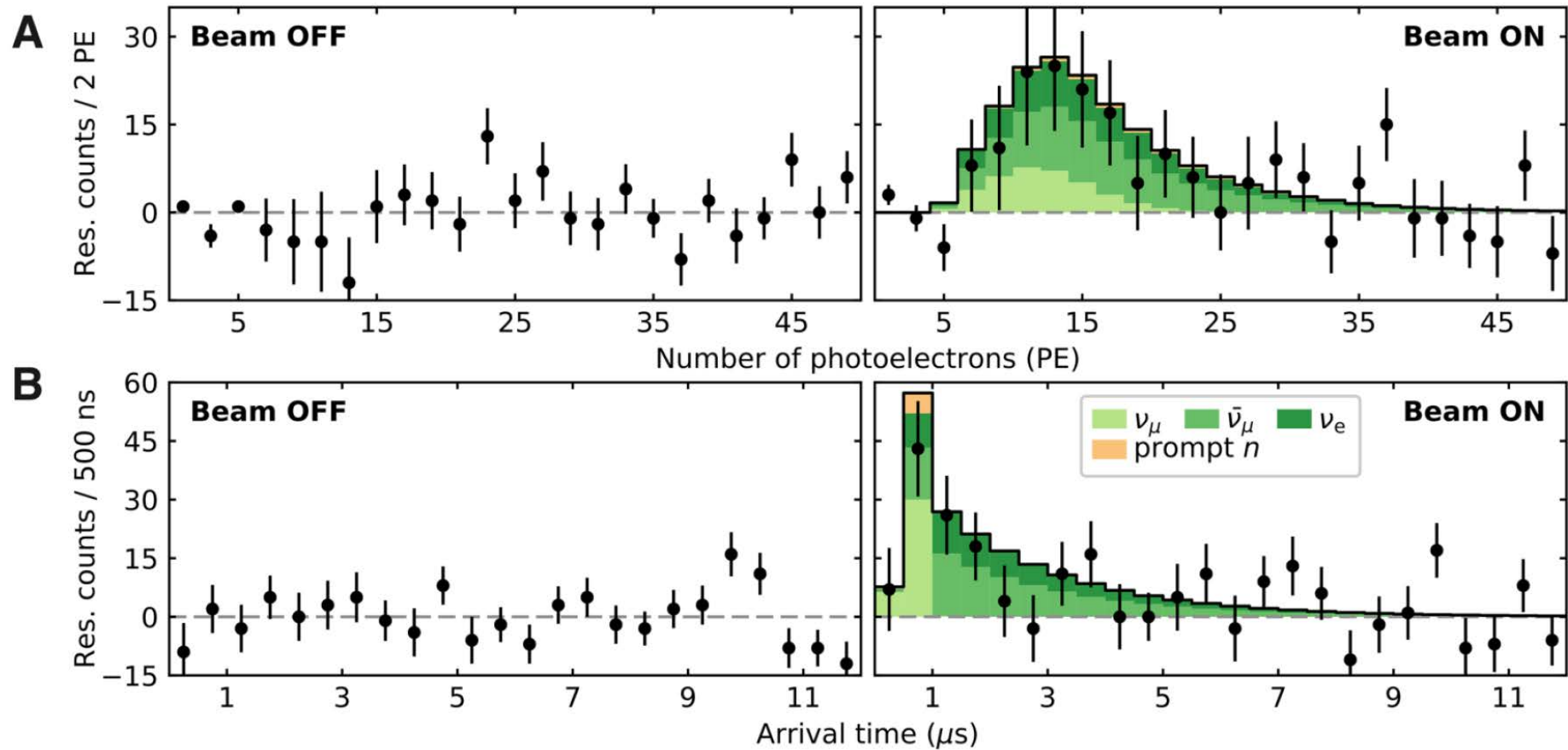
D. Akimov,<sup>1,2</sup> J. B. Albert,<sup>3</sup> P. An,<sup>4</sup> C. Awe,<sup>4,5</sup> P. S. Barbeau,<sup>4,5</sup> B. Becker,<sup>6</sup> V. Belov,<sup>1,2</sup> A. Brown,<sup>4,7</sup> A. Bolozdynya,<sup>2</sup> B. Cabrera-Palmer,<sup>8</sup> M. Cervantes,<sup>2</sup> J. I. Collar,<sup>9a</sup> R. J. Cooper,<sup>10</sup> R. L. Cooper,<sup>11,12</sup> C. Cuesta,<sup>13a</sup> D. J. Dean,<sup>14</sup> J. A. Detwiler,<sup>15</sup> A. Eberhardt,<sup>16</sup> Y. Efremenko,<sup>6,14</sup> S. R. Elliott,<sup>17</sup> E. M. Erkela,<sup>18</sup> L. Fabris,<sup>14</sup> M. Febraro,<sup>14</sup> N. E. Fields,<sup>9a</sup> W. Fox,<sup>2</sup> Z. Fu,<sup>19</sup> A. Galindo-Uribarri,<sup>14</sup> M. P. Green,<sup>4,14,15</sup> M. Hai,<sup>9a</sup> S. M. R. Heath,<sup>2</sup> S. Hedges,<sup>4,5</sup> D. Hornback,<sup>14</sup> T. W. Hossbach,<sup>16</sup> E. B. Iverson,<sup>14</sup> L. J. Kaufman,<sup>20</sup> S. Ki,<sup>4,5</sup> S. R. Klein,<sup>10</sup> A. Khromov,<sup>2</sup> A. Kononov,<sup>12,17</sup> M. Kremer,<sup>4</sup> A. Kumpan,<sup>2</sup> C. Leadbetter,<sup>4</sup> L. Li,<sup>4,5</sup> W. Lu,<sup>14</sup> K. Mann,<sup>4,15</sup> D. M. Markoff,<sup>4,7</sup> K. Miller,<sup>4,5</sup> H. Moreno,<sup>11</sup> P. E. Mueller,<sup>14</sup> J. Newby,<sup>14</sup> J. L. Orrell,<sup>16</sup> C. T. Overman,<sup>16</sup> D. S. Parno,<sup>14a</sup> S. Penttila,<sup>14</sup> G. Perumpilly,<sup>9</sup> H. Ray,<sup>14</sup> J. Rayburn,<sup>5</sup> D. Reyna,<sup>8</sup> G. C. Rich,<sup>4,14,19</sup> D. Rimal,<sup>10</sup> D. Rudik,<sup>12</sup> K. Scholberg,<sup>2</sup> B. J. Scholz,<sup>9</sup> G. Sinev,<sup>2</sup> W. M. Snow,<sup>2</sup> V. Sosnovtsev,<sup>2</sup> A. Shkurov,<sup>2</sup> S. Suchyta,<sup>10</sup> B. Suh,<sup>4,5,14</sup> R. Taylor,<sup>2</sup> R. T. Thornton,<sup>2</sup> I. Tolstukhin,<sup>2</sup> J. Vanderwerp,<sup>9</sup> R. L. Varner,<sup>14</sup> C. J. Virtue,<sup>20</sup> Z. Wan,<sup>4</sup> J. Yoo,<sup>21</sup> C.-H. Yu,<sup>14</sup> A. Zawada,<sup>4</sup> J. Zettlemoyer,<sup>2</sup> A. M. Zderic,<sup>14</sup> COHERENT Collaboration#

**B**

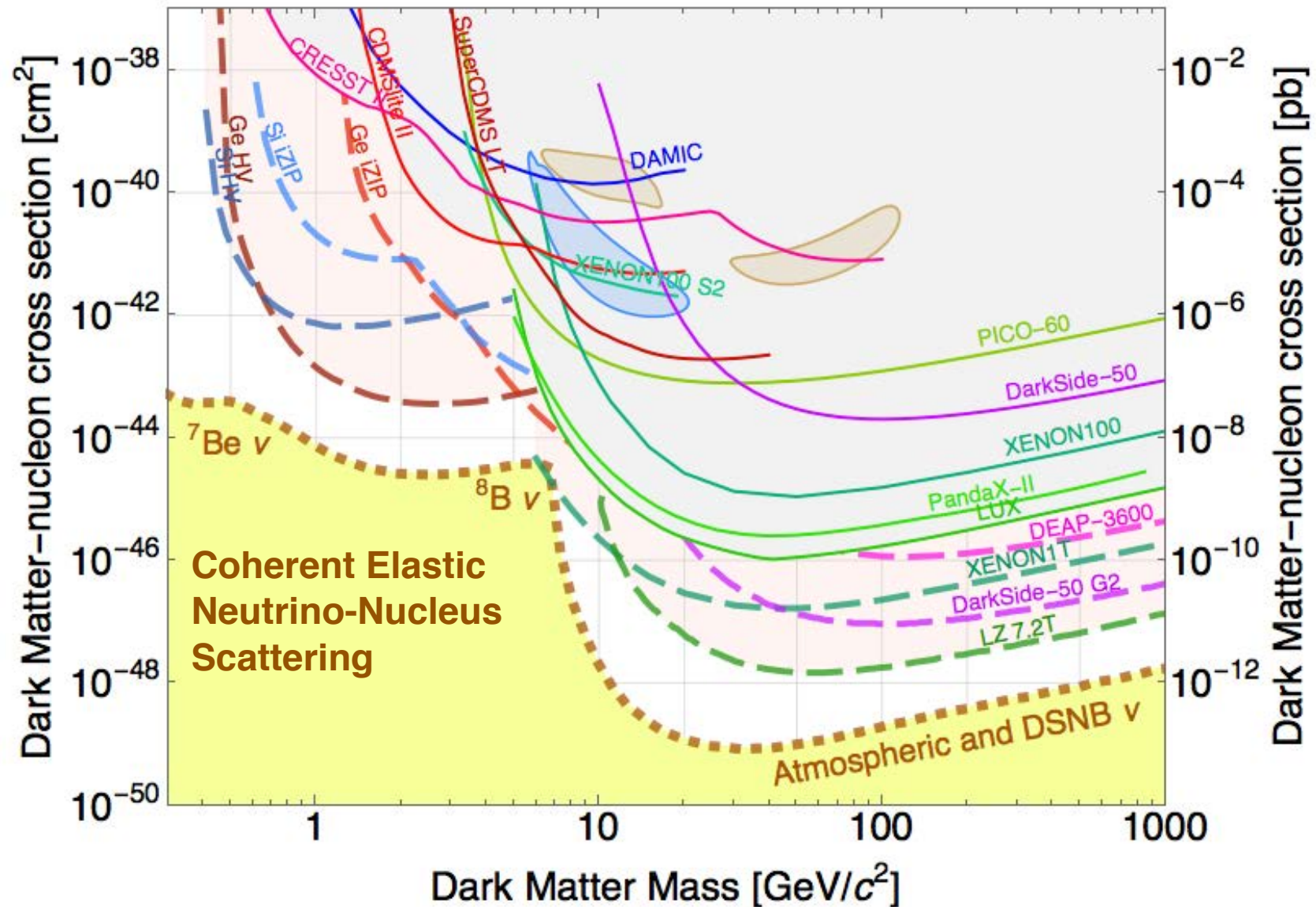


- When  $q \ll 1/R$  ( $E_\nu < 50 \text{ MeV}$ ),  $\sigma_{\text{Total}} \sim N^2$ , but the nucleus recoil energy is very low.
- First observation was made in a CsI detector using neutrinos from the Spallation Neutron Source at ORNL.

# Coherent Elastic Neutrino-Nucleus Scattering



# Their signals, your backgrounds



**Inverse beta decay  
and  
low-energy neutrino-nucleus interactions**

# Inverse Beta Decay (IBD)

- Recall (the discovery of neutrinos by Reines & Cowan):

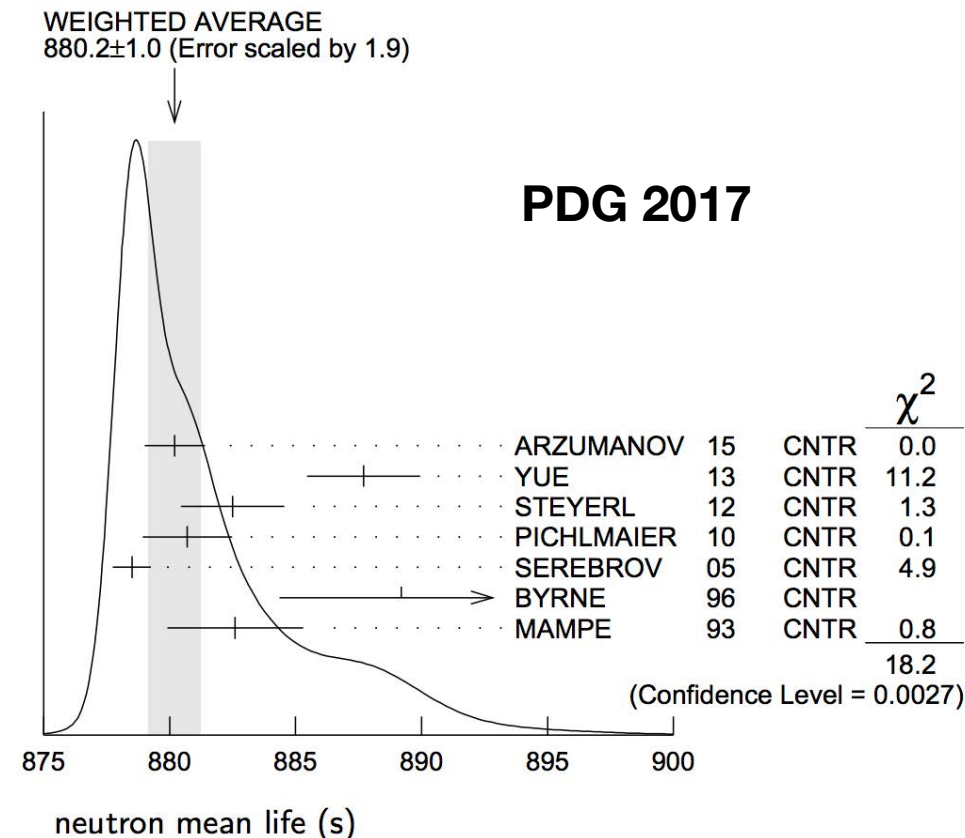
**Inverse Beta Decay:**  $\bar{\nu}_e + p \rightarrow n + e^+$   $E_{\bar{\nu}_e} > 1.8 \text{ MeV}$

- The cross section of this process at low neutrino energy ( $\sim$  a few MeV) is:

$$\sigma_{tot} = \frac{2\pi^2}{m_e^5} \frac{E_{e^+} p_{e^+}}{f \tau_n}$$

where  $f = 1.715$  and  $\tau_n = 880.2 (1.0) \text{ s}$   
(but with controversial measurements).

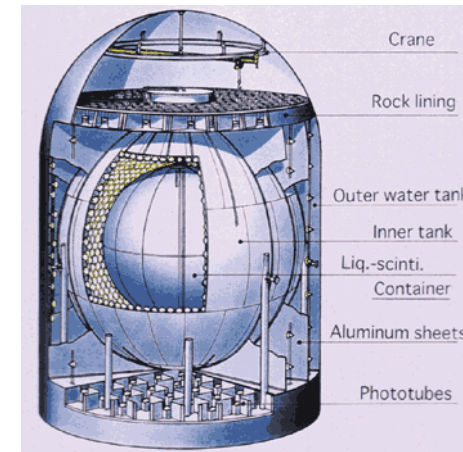
- The neutron lifetime is an important parameter that fixes the cross section for single nucleon processes.



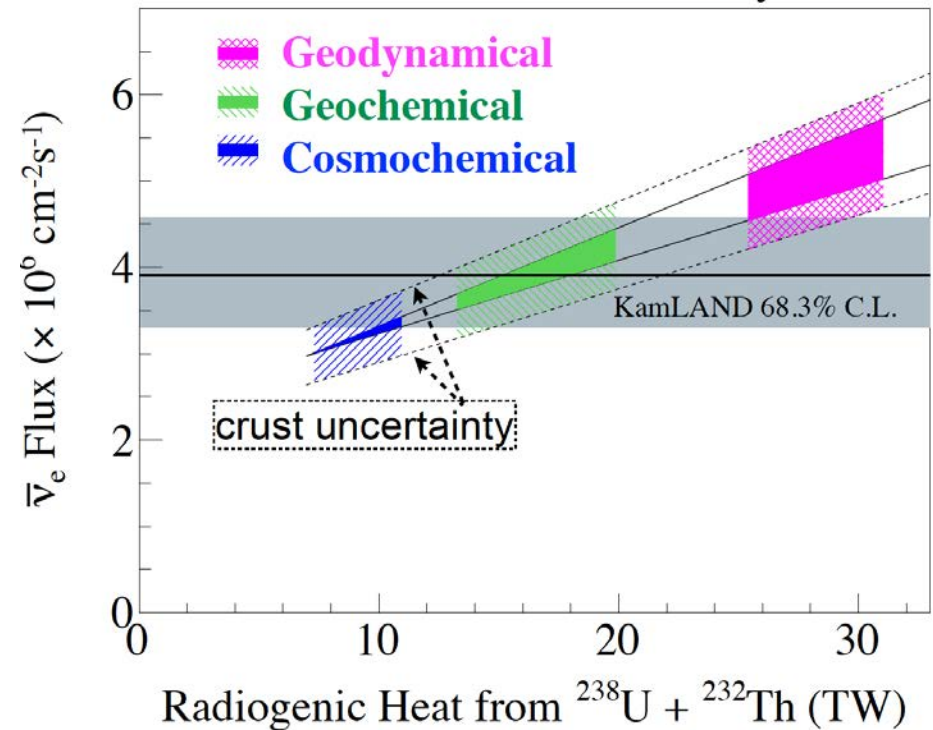
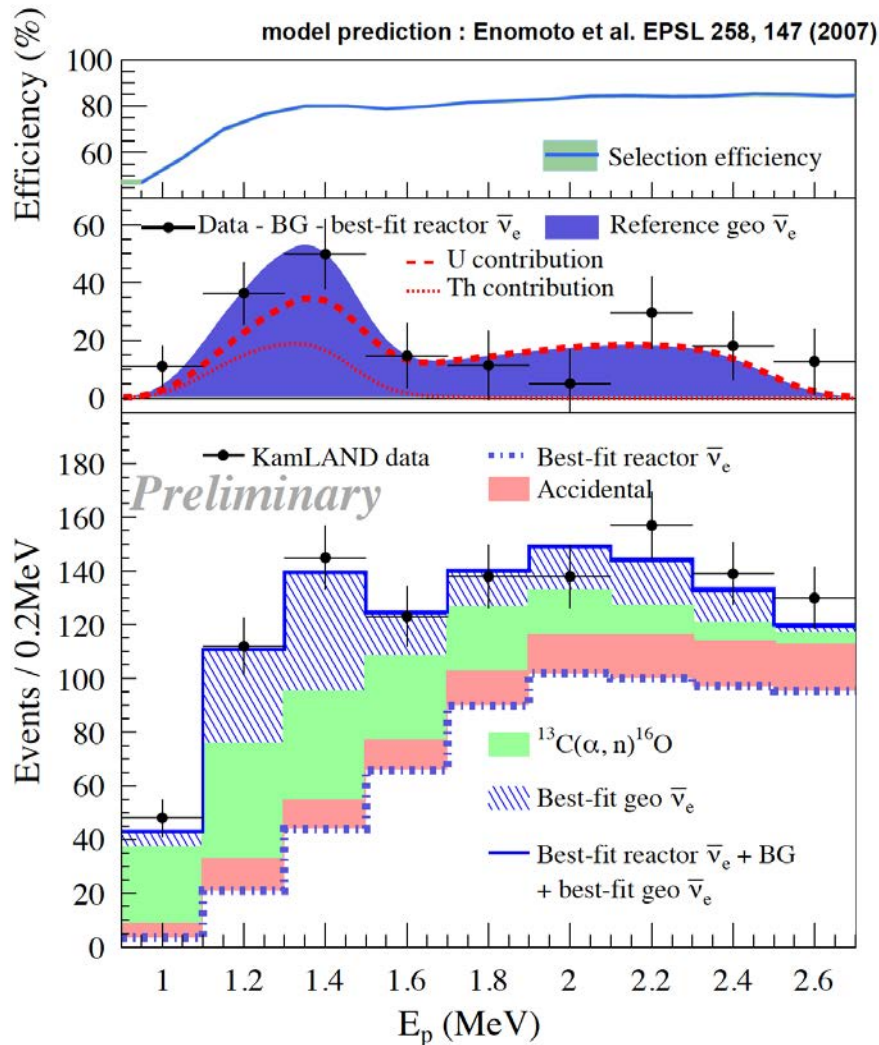


# Geo-neutrinos

- 1 kt liquid scintillator
- Detect anti-neutrinos from reactors and earth's core by IBD



2016 Preliminary Result



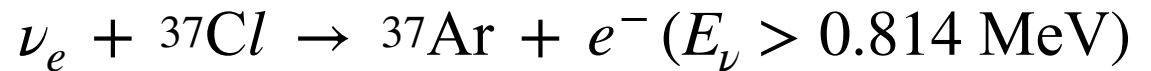
✓ Radiogenic Heats :  $15.5^{+6.5}_{-6.3}$  TW

✓ Cosmochemical, Geodynamical Models

are getting to be rejected

# Using other nucleus as neutrino target

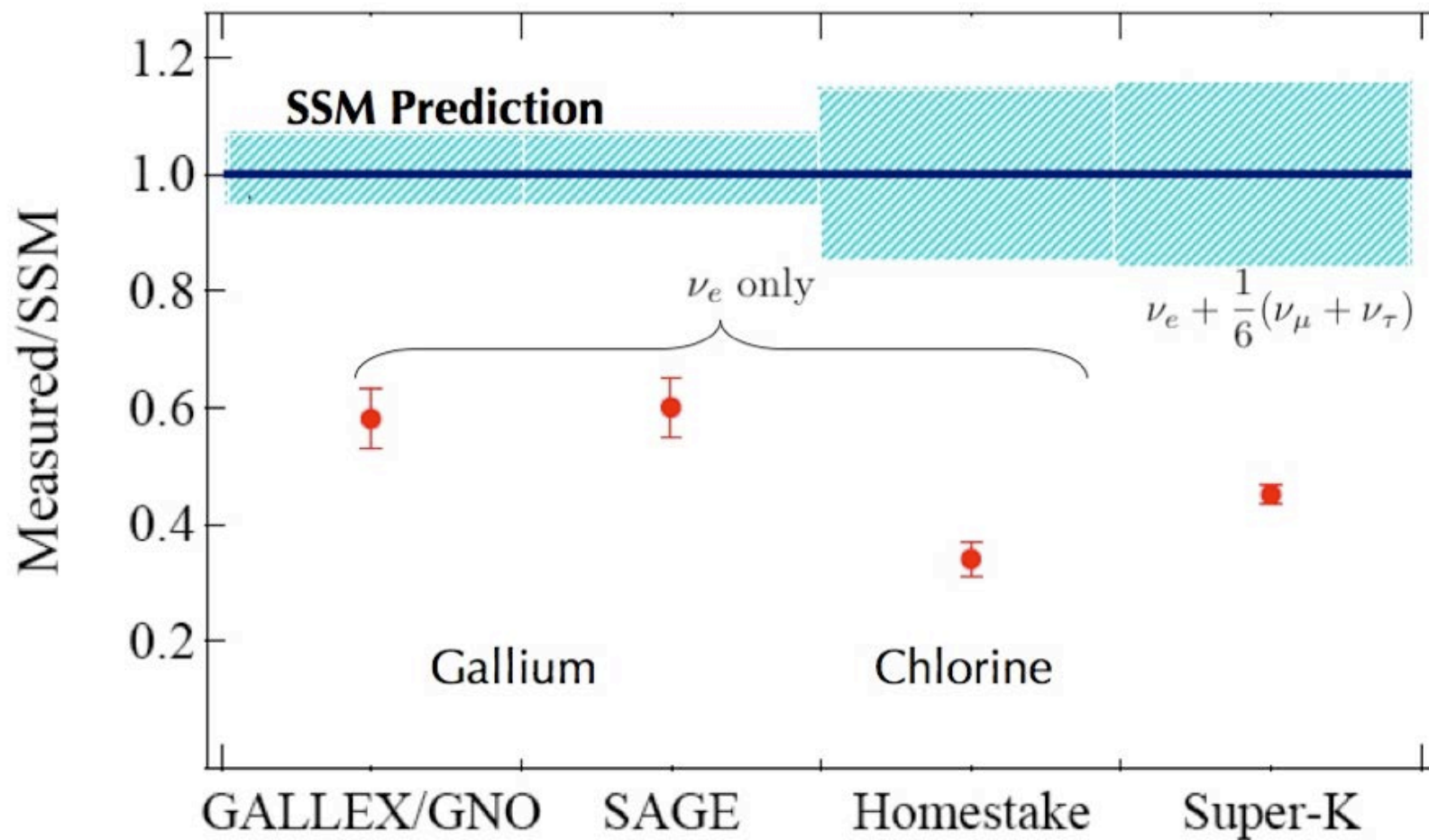
- The first detection of solar neutrinos by Ray Davis (615t of  $\text{C}_2\text{Cl}_4$  at Homestake mine (now SURF) in SD:



- Flushed tank, collect  ${}^{37}\text{Ar}$ , looked for its decay back to  ${}^{37}\text{Cl}$ .
- Solar Neutrino Problem: only 1/3 of the expected number of solar neutrinos was observed.
- Ray Davis won the Nobel Prize in Physics (with M. Koshiba) in 2002.
- Note:**
  - The Sun only emits  $\nu_e$  ( $p$ - $p$  chain)
  - Charged-current (in detection) only sensitive to  $\nu_e$

# Solar Neutrino Problem (~2000)

- Are the Standard Solar Model predictions wrong?
- Or is there something about the neutrinos that we don't understand?






# Measure CC and NC ( $\nu_e$ vs all flavors)

**Measure:**


$$\frac{CC}{NC} = \frac{\nu_e}{\nu_e + \nu_\mu + \nu_\tau}$$

**Transformation to another active flavor if:**


$$\phi^{CC}(\nu_e) < \phi^{NC}(\nu_x)$$

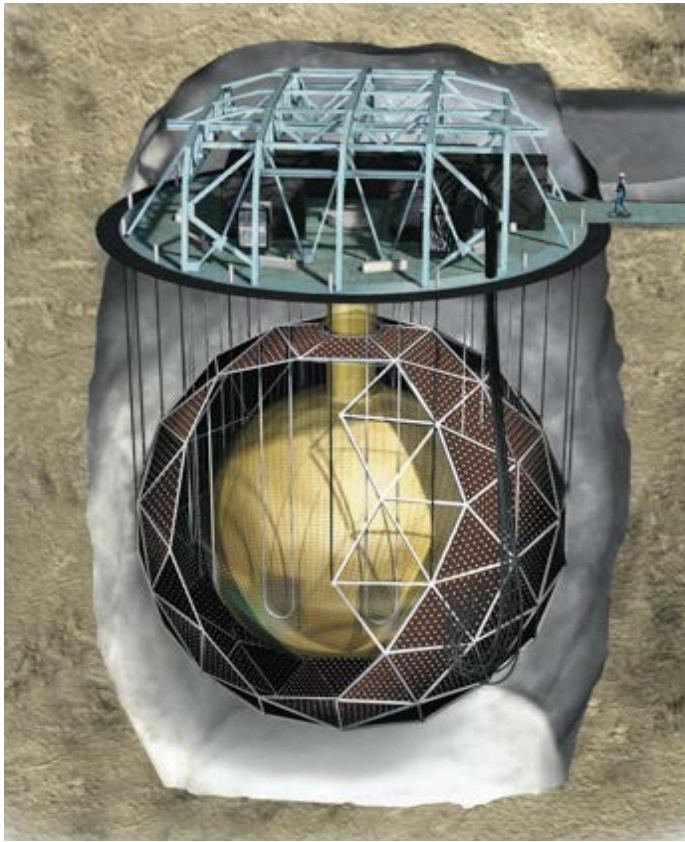
*Alternatively...*

$$\frac{CC}{ES} = \frac{\nu_e}{\nu_e + 0.15(\nu_\mu + \nu_\tau)}$$


$$\phi^{CC}(\nu_e) < \phi^{ES}(\nu_x)$$

Flavor transformation (particle physics) can be tested without any assumption on the Standard Solar Model prediction of the total neutrino flux.

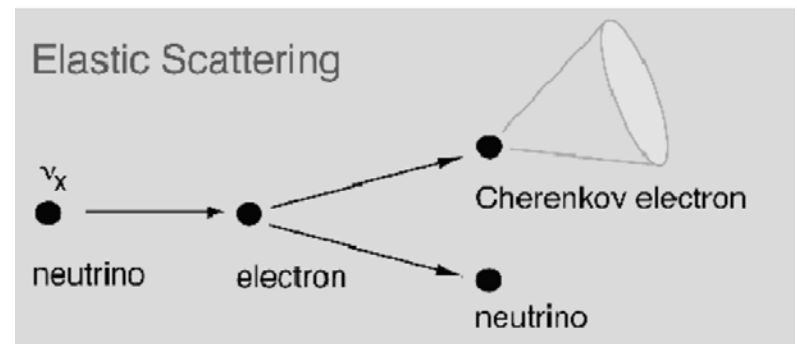
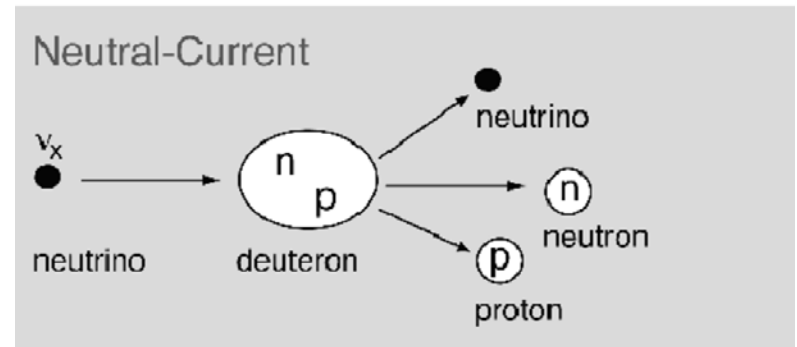
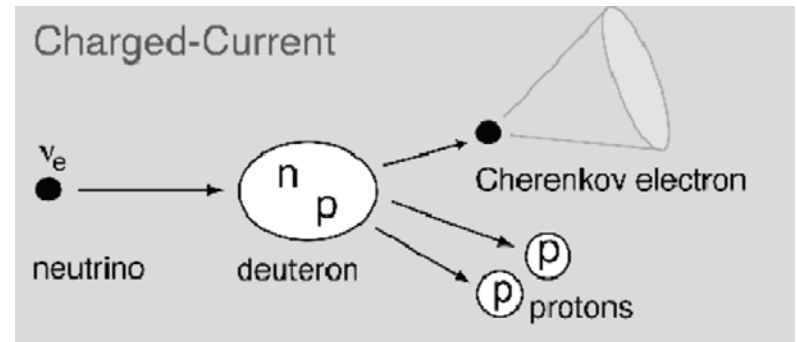
<b>Is there a magic target ?</b>
----------------------------------



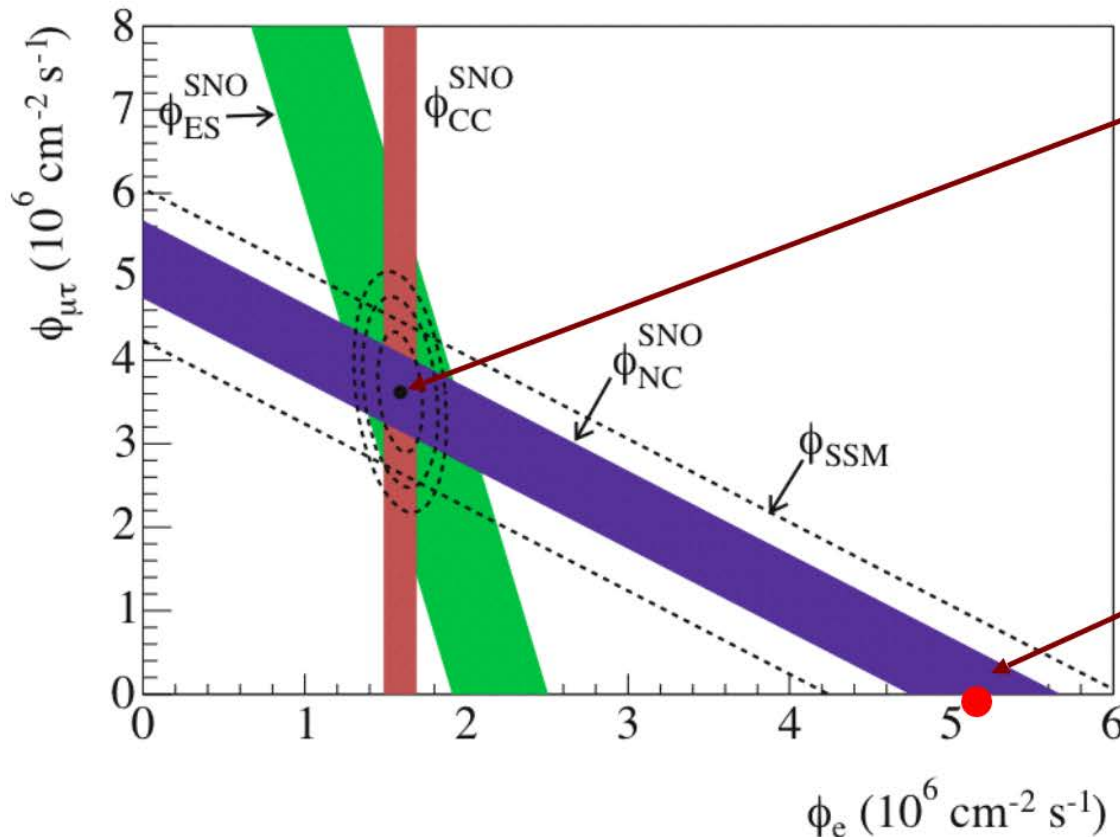
# The deuteron

- 2 km underground at Vale's Creighton mine near Sudbury, ON, Canada
- 1000t of D<sub>2</sub>O in a 12-m  $\phi$  acrylic sphere

<b>CC</b>	$\nu_e + d \rightarrow p + p + e^-$
<b>NC</b>	$\nu_x + d \rightarrow p + n + \nu'_x$
<b>ES</b>	$\nu_x + e^- \rightarrow \nu_x + e^-$



# Sudbury Neutrino Observatory (SNO)



Standard Solar Model  
**CORRECT**

Standard Model of Elementary Particles  
( $m_\nu=0$ )  
**WRONG**

**~2/3** of the  $\nu_e$  produced in the Sun have transformed into  $\nu_\mu$  or  $\nu_\tau$

**SNO provided the first direct observation of neutrino flavor transformation  
(which requires neutrinos to be massive)**

# Aside: neutrino mixing

- A weak eigenstate  $|\nu_\alpha\rangle$  is a linear combination of mass eigenstates  $|\nu_i\rangle$ :

$$|\nu_\alpha\rangle = \sum_{i=1}^3 U_{\alpha i} |\nu_i\rangle$$

where  $U$  = Maki-Nakagawa-Sakata-Pontecorvo (MNSP) matrix.

$$|U| = \begin{pmatrix} 0.779 \leftrightarrow 0.848 & 0.510 \leftrightarrow 0.604 & 0.122 \leftrightarrow 0.190 \\ 0.183 \leftrightarrow 0.568 & 0.385 \leftrightarrow 0.728 & 0.613 \leftrightarrow 0.794 \\ 0.200 \leftrightarrow 0.576 & 0.408 \leftrightarrow 0.742 & 0.589 \leftrightarrow 0.775 \end{pmatrix}$$

$$|\nu_e\rangle = (\sim 0.81) |\nu_1\rangle + (\sim 0.55) |\nu_2\rangle + (\sim 0.16) |\nu_3\rangle$$

$$|\nu_\mu\rangle = (\sim 0.38) |\nu_1\rangle + (\sim 0.56) |\nu_2\rangle + (\sim 0.70) |\nu_3\rangle$$

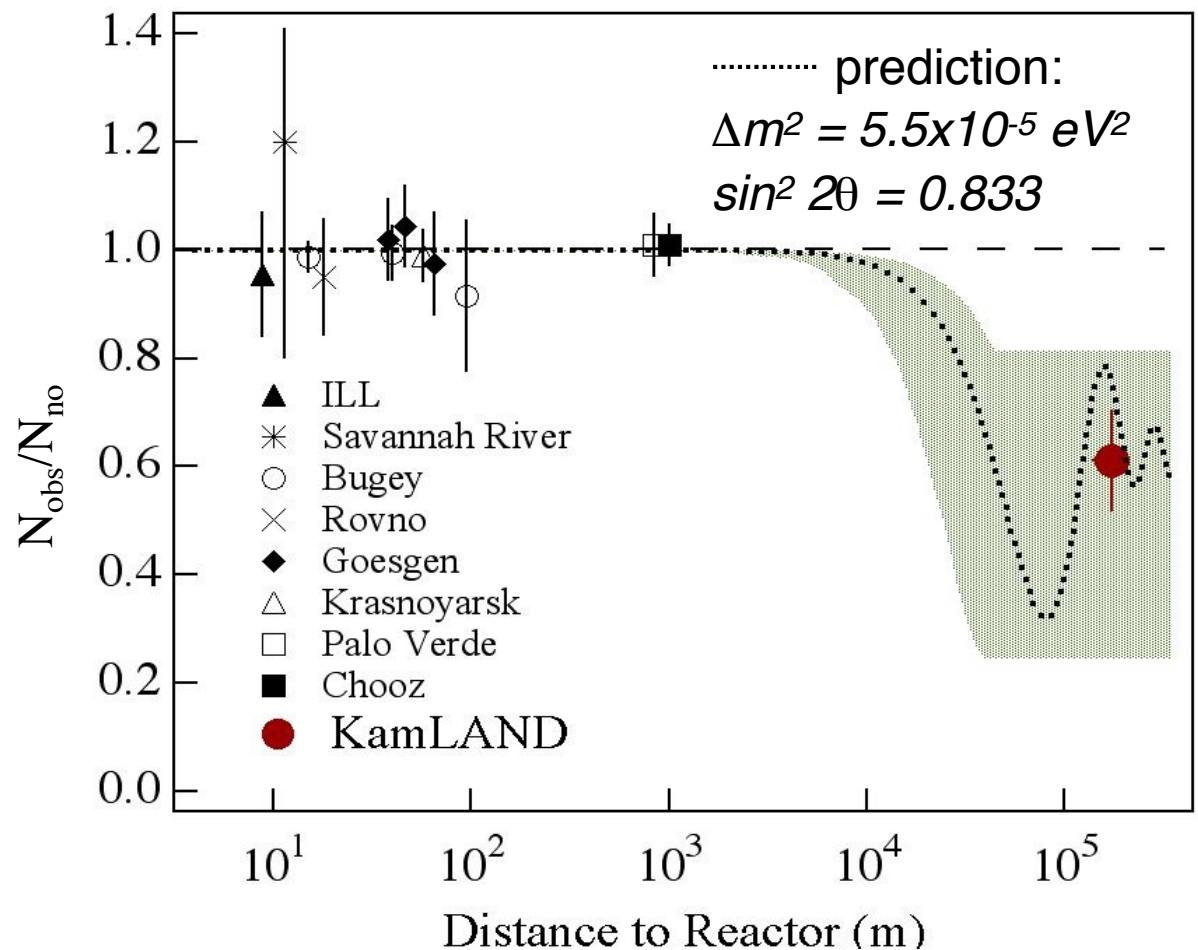
$$|\nu_\tau\rangle = (\sim 0.39) |\nu_1\rangle + (\sim 0.58) |\nu_2\rangle + (\sim 0.68) |\nu_3\rangle$$

# KamLAND - Reactor Anti-Neutrino

KamLAND showed that neutrino oscillation is the original of flavor transformation seen in SNO



$$P_{\nu_e \rightarrow \nu_e} = 1 - \sin^2 2\theta \sin^2 \left( 1.27 \frac{\Delta m^2 [\text{eV}^2] L [\text{m}]}{E [\text{MeV}]} \right)$$





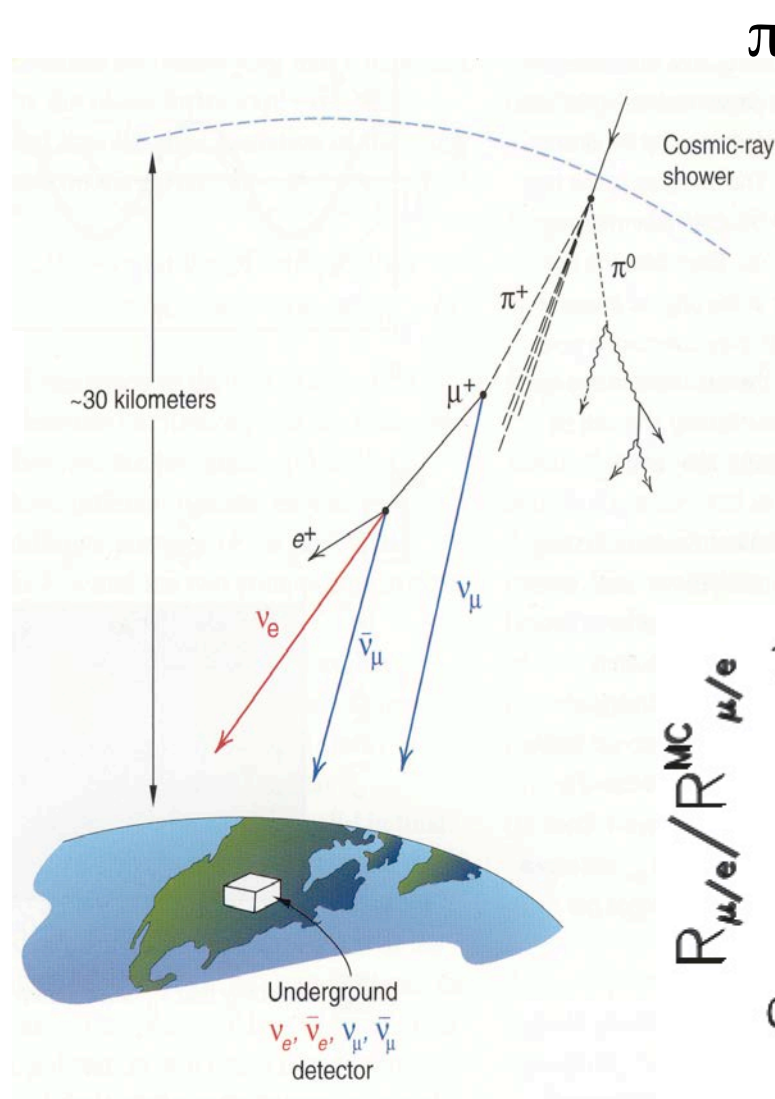
# Other nuclear targets for $\nu$ detection

- A common target is liquid scintillator (lots of C and H), but there have been other nuclei that have been studied quite extensively
- Theory vs experimental cross section agreement generally good for low energy (1-300 MeV)

Isotope	Reaction Channel	Source	Experiment	Measurement ( $10^{-42} \text{ cm}^2$ )	Theory ( $10^{-42} \text{ cm}^2$ )
$^2\text{H}$	$^2\text{H}(\nu_e, e^-)pp$	Stopped $\pi/\mu$	LAMPF	$52 \pm 18(\text{tot})$	54 (IA) (Tatara, Kohyama, and Kubodera, 1990)
$^{12}\text{C}$	$^{12}\text{C}(\nu_e, e^-)^{12}\text{N}_{\text{g.s.}}$	Stopped $\pi/\mu$	KARMEN	$9.1 \pm 0.5(\text{stat}) \pm 0.8(\text{sys})$	9.4 [Multipole](Donnelly and Peccei, 1979)
		Stopped $\pi/\mu$	E225	$10.5 \pm 1.0(\text{stat}) \pm 1.0(\text{sys})$	9.2 [EPT] (Fukugita, Kohyama, and Kubodera, 1988).
	$^{12}\text{C}(\nu_e, e^-)^{12}\text{N}^*$	Stopped $\pi/\mu$	LSND	$8.9 \pm 0.3(\text{stat}) \pm 0.9(\text{sys})$	8.9 [CRPA] (Kolbe, Langanke, and Vogel, 1999)
		Stopped $\pi/\mu$	KARMEN	$5.1 \pm 0.6(\text{stat}) \pm 0.5(\text{sys})$	5.4–5.6 [CRPA] (Kolbe, Langanke, and Vogel, 1999)
	$^{12}\text{C}(\nu_\mu, \nu_\mu)^{12}\text{C}^*$	Stopped $\pi/\mu$	E225	$3.6 \pm 2.0(\text{tot})$	4.1 [Shell] (Hayes and Towner, 2000)
		Stopped $\pi/\mu$	LSND	$4.3 \pm 0.4(\text{stat}) \pm 0.6(\text{sys})$	
		Stopped $\pi/\mu$	KARMEN	$3.2 \pm 0.5(\text{stat}) \pm 0.4(\text{sys})$	2.8 [CRPA] (Kolbe, Langanke, and Vogel, 1999)
		Stopped $\pi/\mu$	KARMEN	$10.5 \pm 1.0(\text{stat}) \pm 0.9(\text{sys})$	10.5 [CRPA] (Kolbe, Langanke, and Vogel, 1999)
$^{12}\text{C}$	$^{12}\text{C}(\nu_\mu, \mu^-)X$	Decay in flight	LSND	$1060 \pm 30(\text{stat}) \pm 180(\text{sys})$	1750–1780 [CRPA] (Kolbe, Langanke, and Vogel, 1999)
	$^{12}\text{C}(\nu_\mu, \mu^-)^{12}\text{N}_{\text{g.s.}}$	Decay in flight	LSND	$56 \pm 8(\text{stat}) \pm 10(\text{sys})$	1380 [Shell] (Hayes and Towner, 2000) 1115 [Green's Function] (Meucci, Giusti, and Pacati, 2004) 68–73 [CRPA] (Kolbe, Langanke, and Vogel, 1999)
$^{56}\text{Fe}$	$^{56}\text{Fe}(\nu_e, e^-)^{56}\text{Co}$	Stopped $\pi/\mu$	KARMEN	$256 \pm 108(\text{stat}) \pm 43(\text{sys})$	56 [Shell] (Hayes and Towner, 2000) 264 [Shell] (Kolbe, Langanke, and Martínez-Pinedo, 1999)
$^{71}\text{Ga}$	$^{71}\text{Ga}(\nu_e, e^-)^{71}\text{Ge}$	$^{51}\text{Cr}$ source	GALLEX, ave.	$0.0054 \pm 0.0009(\text{tot})$	0.0058 [Shell] (Haxton, 1998)
		$^{51}\text{Cr}$	SAGE	$0.0055 \pm 0.0007(\text{tot})$	
		$^{37}\text{Ar}$ source	SAGE	$0.0055 \pm 0.0006(\text{tot})$	0.0070 [Shell] (Bahcall, 1997)
$^{127}\text{I}$	$^{127}\text{I}(\nu_e, e^-)^{127}\text{Xe}$	Stopped $\pi/\mu$	LSND	$284 \pm 91(\text{stat}) \pm 25(\text{sys})$	210–310 [Quasiparticle] (Engel, Pittel, and Vogel, 1994)

# **Intermediate-energy and high-energy neutrino-nucleus interactions**

# Atmospheric $\nu$ problem (before 1998)



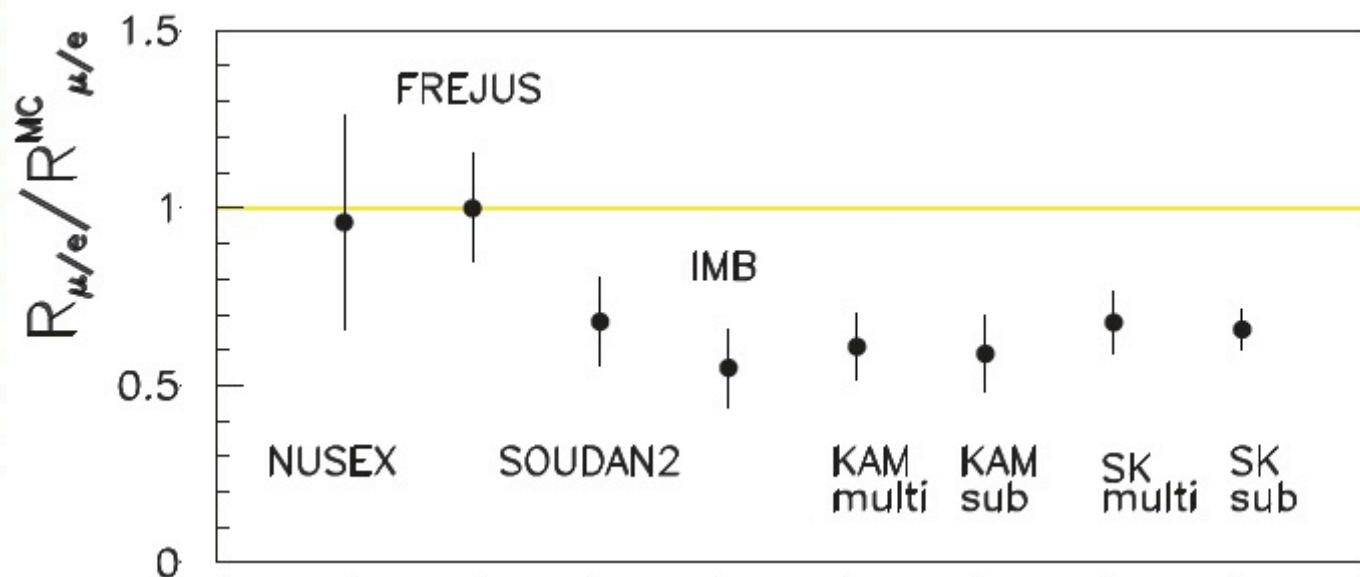
$$\pi^+ \rightarrow \mu^+ + \nu_\mu$$

$$\pi^- \rightarrow \mu^- + \bar{\nu}_\mu$$

$$e^+ + \nu_e + \bar{\nu}_\mu$$

$$e^- + \bar{\nu}_e + \nu_\mu$$

**Expect  $R_{\mu/e}$ :  $(\nu_\mu + \bar{\nu}_\mu) / (\nu_e + \bar{\nu}_e) \sim 2$**   
**Measured  $\sim 0.6-0.7$  of expectation**



**Much higher energy  
than solar neutrinos**



# Intermediate-energy neutrino cross section

- The nucleus is typically described in terms of individual quasi-free nucleons that participate in the scattering process

## 1. Quasielastic scattering (QE)

- Example:  $\nu_\mu n \rightarrow \mu^- p$ ,  $\bar{\nu}_\mu p \rightarrow \mu^+ n$
- Final-state nucleon usually invisible in water Cherenkov detector

## 2. Resonant (RES)

- Neutrino interaction produces a baryon resonance, which quickly decays and most often to a nucleon and single pion final state:

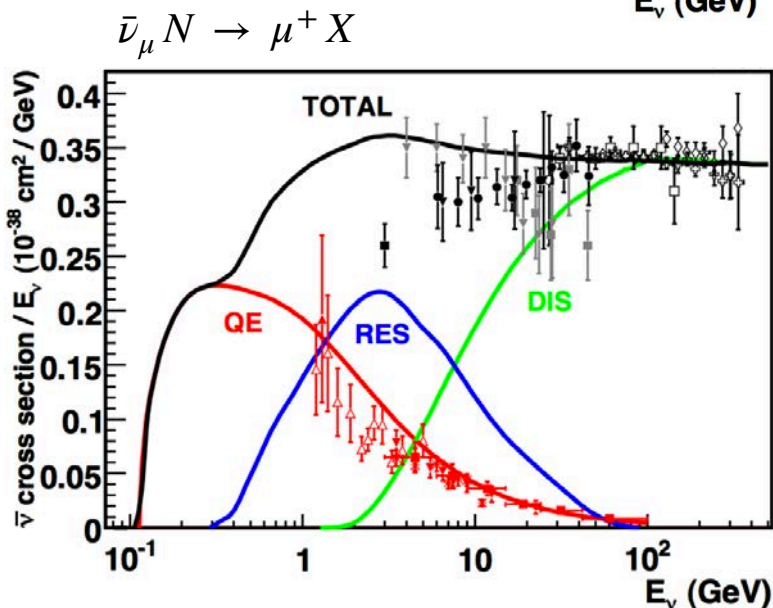
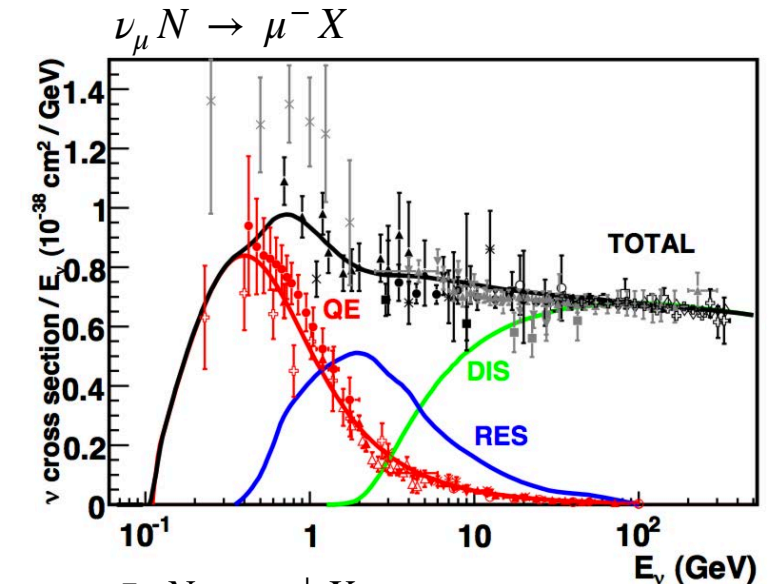
$$\nu_\mu N \rightarrow \mu^- N^*; N^* \rightarrow \pi N'$$

## 3. Deep Inelastic Scattering (DIS)

- Both CC and NC possible
- Example:  $\nu + q \rightarrow l^- q'$ ;  $q' \rightarrow \text{hadrons}$

## 4. NC Neutrino-Nucleon Interactions

$$\nu + N \rightarrow \nu + X$$



# The axial mass $M_A$ puzzle

QE scattering at O(GeV) needs to take into account the nucleon structure:

$$j^\mu = [F_1^V(Q^2)\gamma^\mu + i\frac{\kappa}{2M}F_2^V(Q^2)\sigma^{\mu\nu}q_\nu - F_A(Q^2)\gamma^\mu\gamma^5 + F_P(Q^2)q^\mu\gamma^5]\tau^\pm$$

# The axial mass $M_A$ puzzle

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**Vector - OK**  
(from electron scattering)

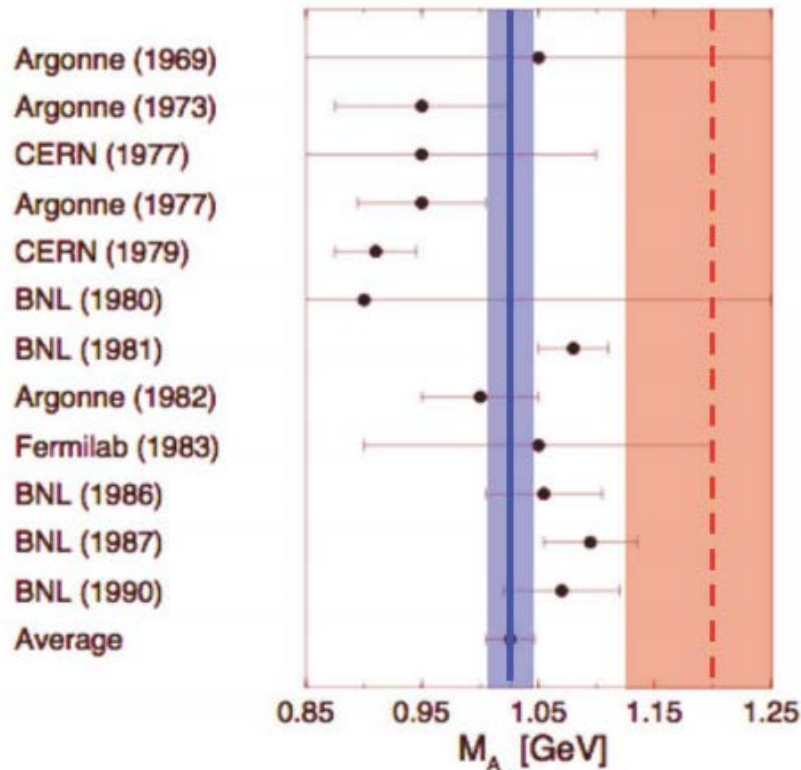
**Pseudoscalar - small**  
 $(\sim m_l/M)^2$

# The axial mass $M_A$ puzzle

QE scattering at O(GeV) needs to take into account the nucleon structure:

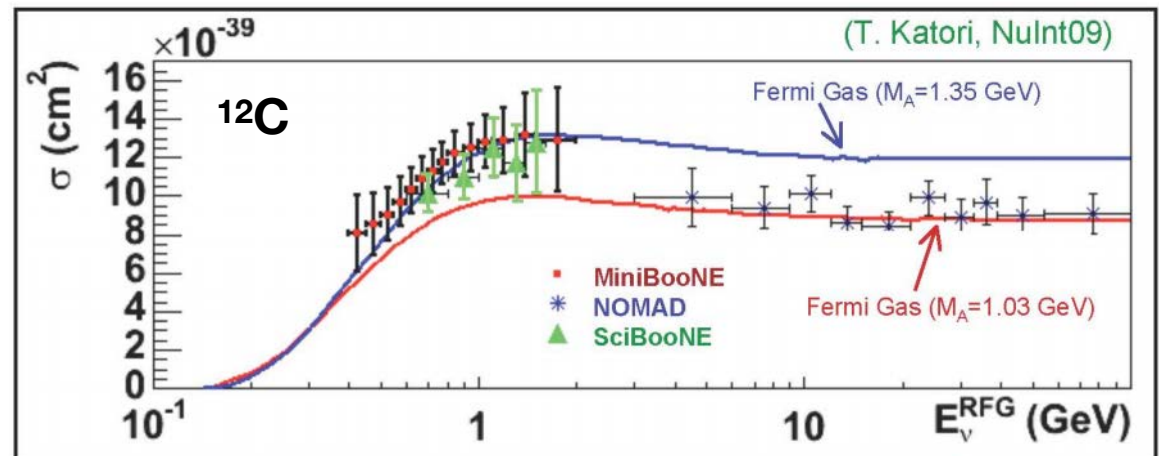
$$j^\mu = [F_1^V(Q^2)\gamma^\mu + i\frac{\kappa}{2M}F_2^V(Q^2)\sigma^{\mu\nu}q_\nu - \underbrace{F_A(Q^2)}_{\uparrow}\gamma^\mu\gamma^5 + F_P(Q^2)q^\mu\gamma^5]\tau^\pm$$

$$F_A(Q^2) = \frac{1.267}{(1 + Q^2/M_A^2)^2}$$

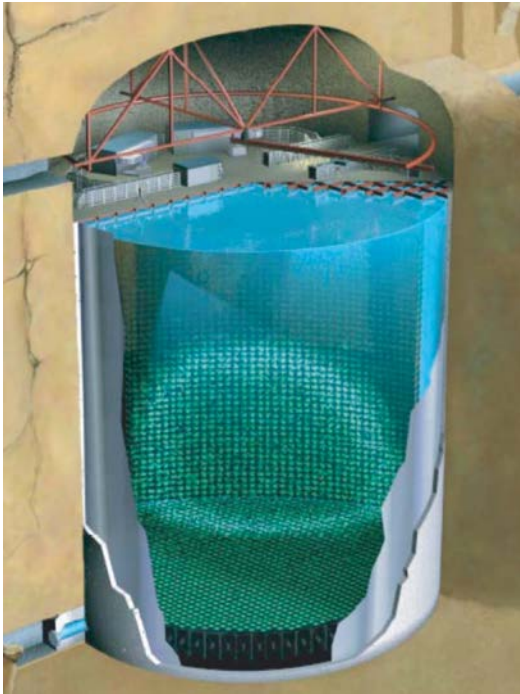


Old (pre-1990) average:  $M_A = 1.03 \pm 0.02$  GeV

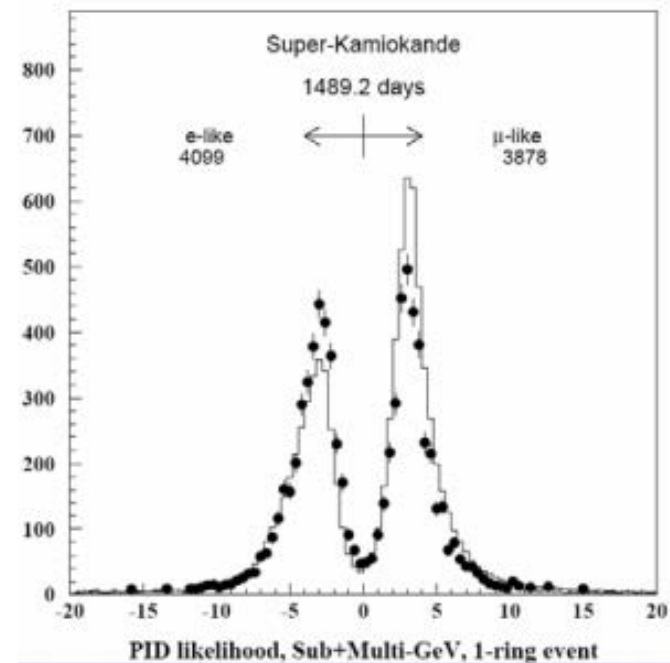
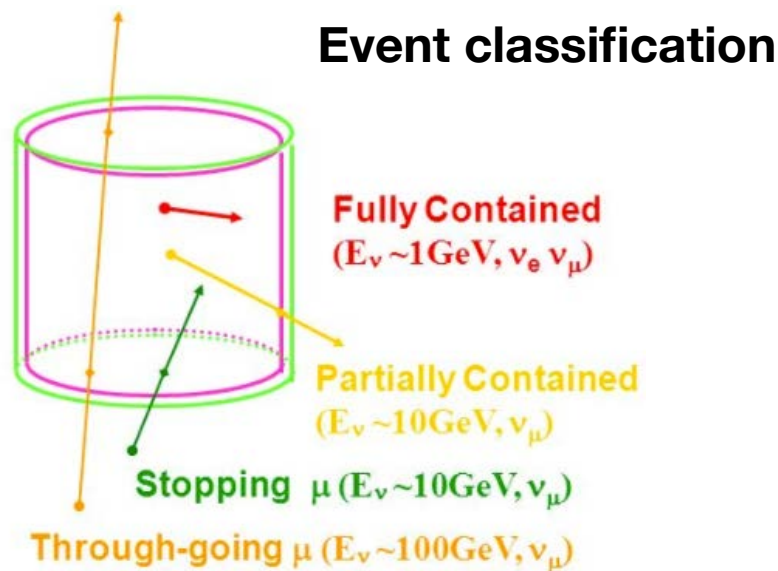
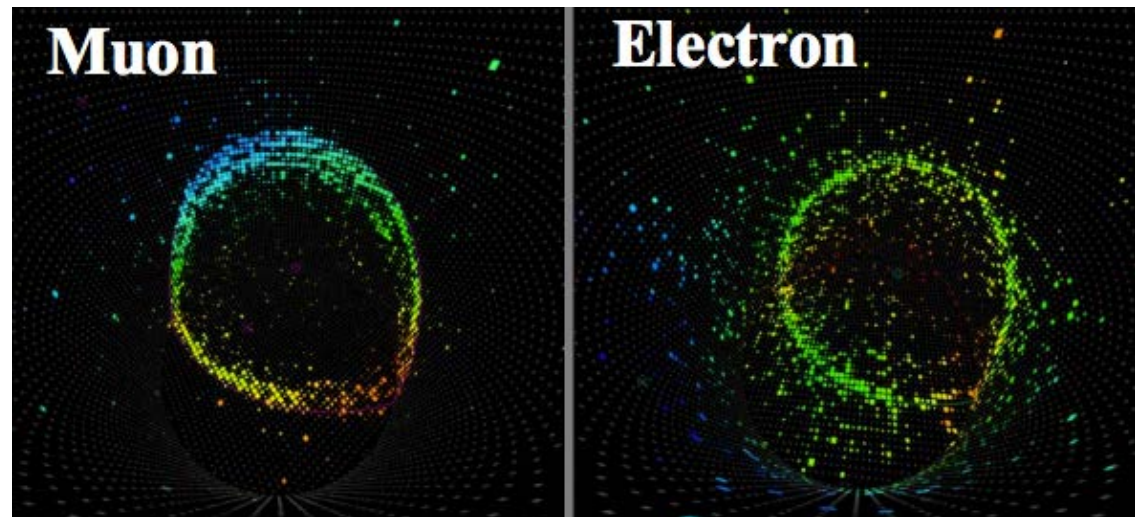
Newer measurements (K2K, MINOS, MiniBooNE...etc) are higher, up to **~1.35 GeV**



# Super-Kamiokande



- 50 kt  $\text{H}_2\text{O}$ , 22 kt fiducial volume
- Water Cherenkov detector

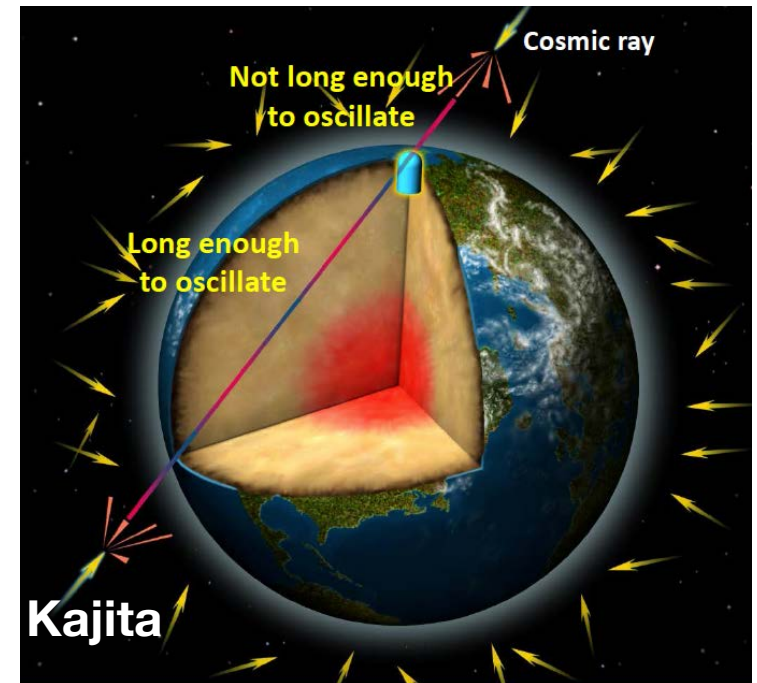
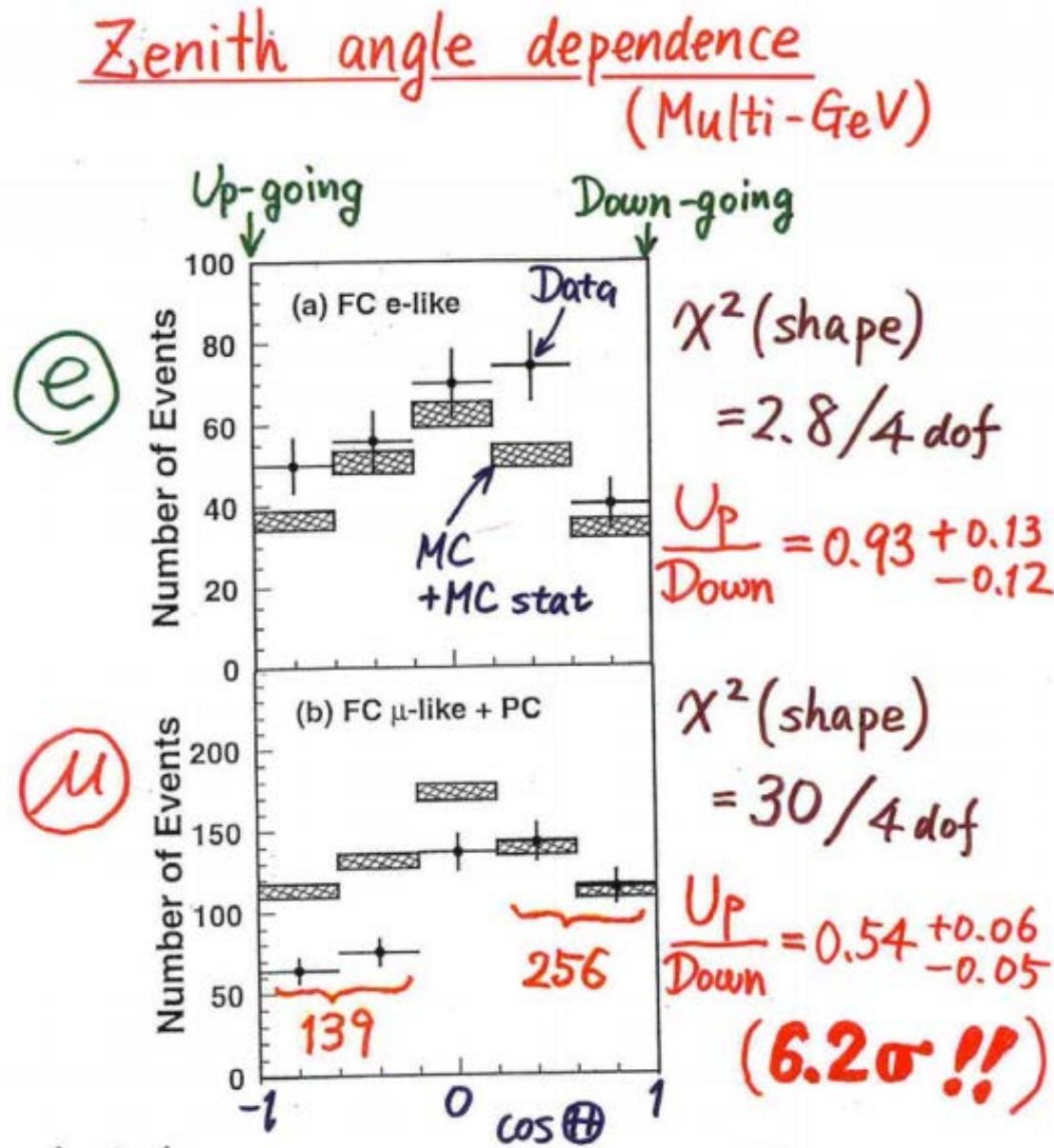




# Super-Kamiokande



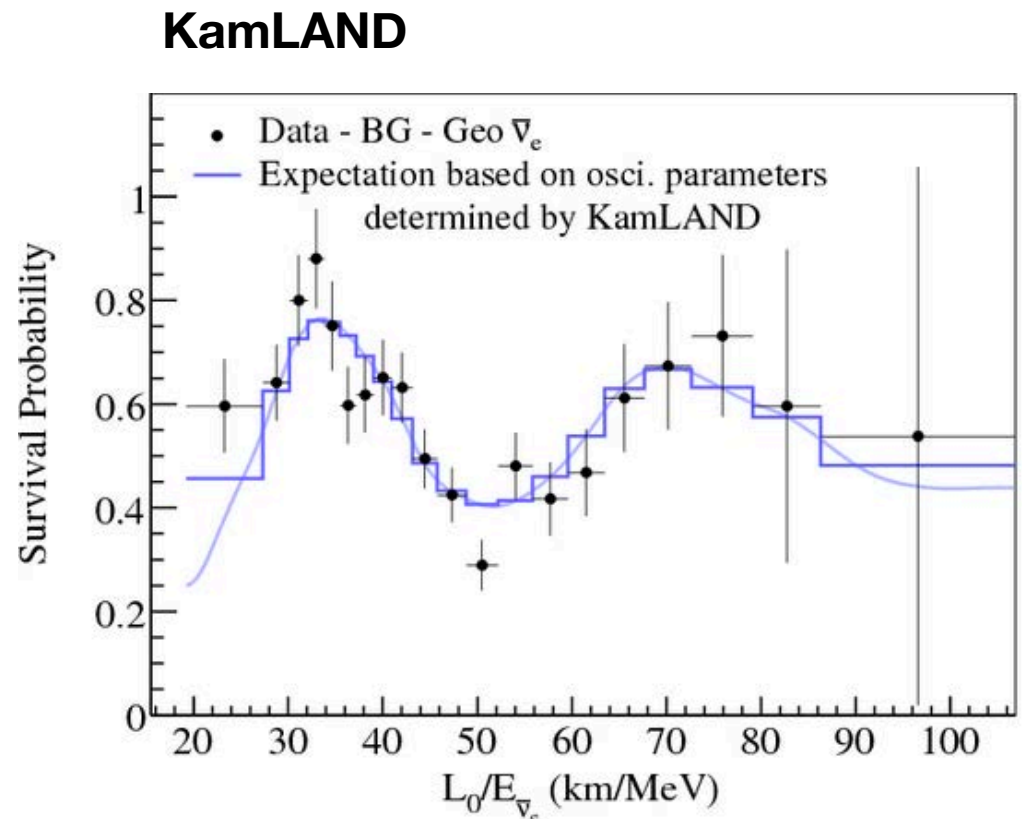
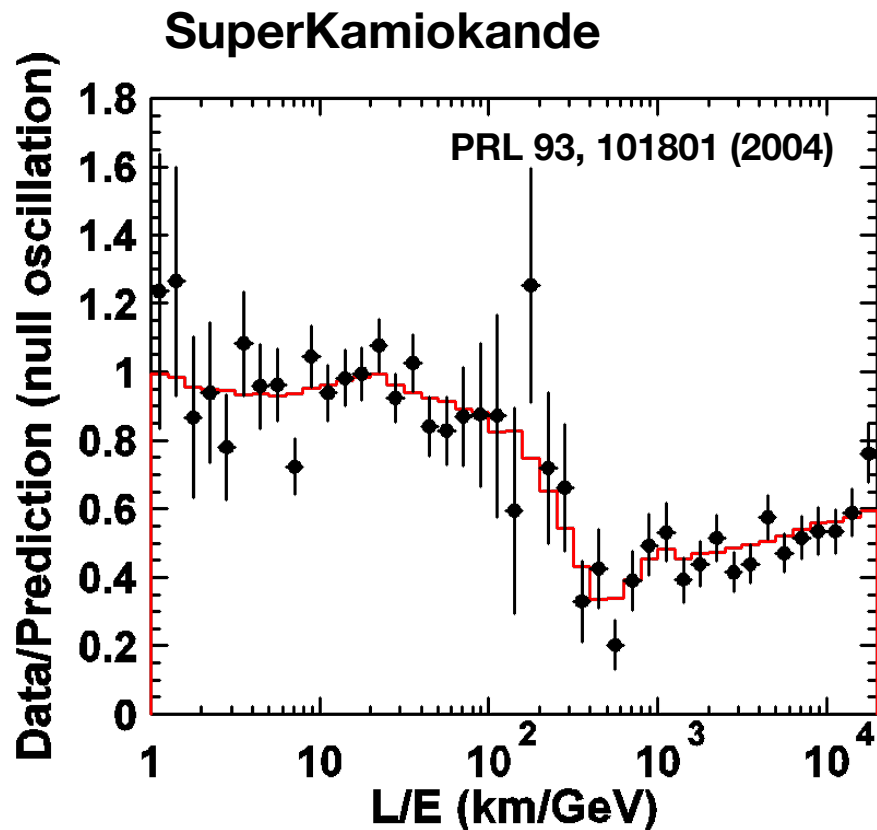
First demonstration of physics beyond the Standard Model (neutrino oscillations, hence neutrino mass)



Reminder:  
Segre Lecture - Kajita  
5:30pm, Oct 30, 2017

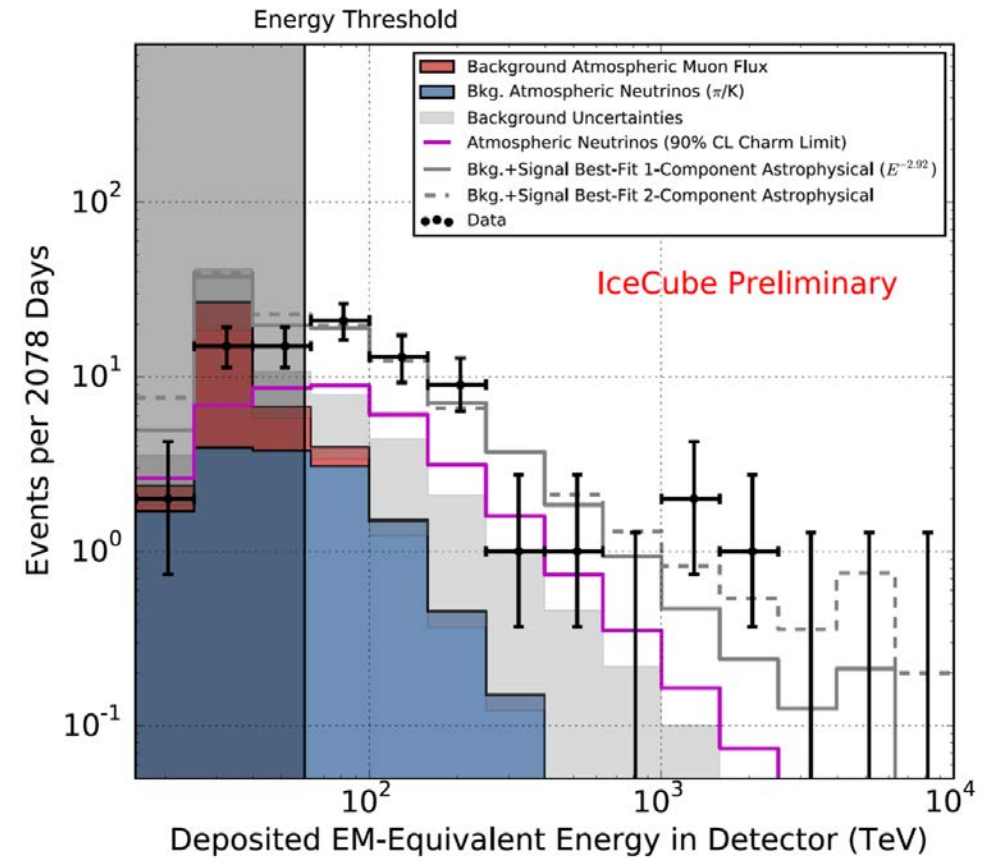
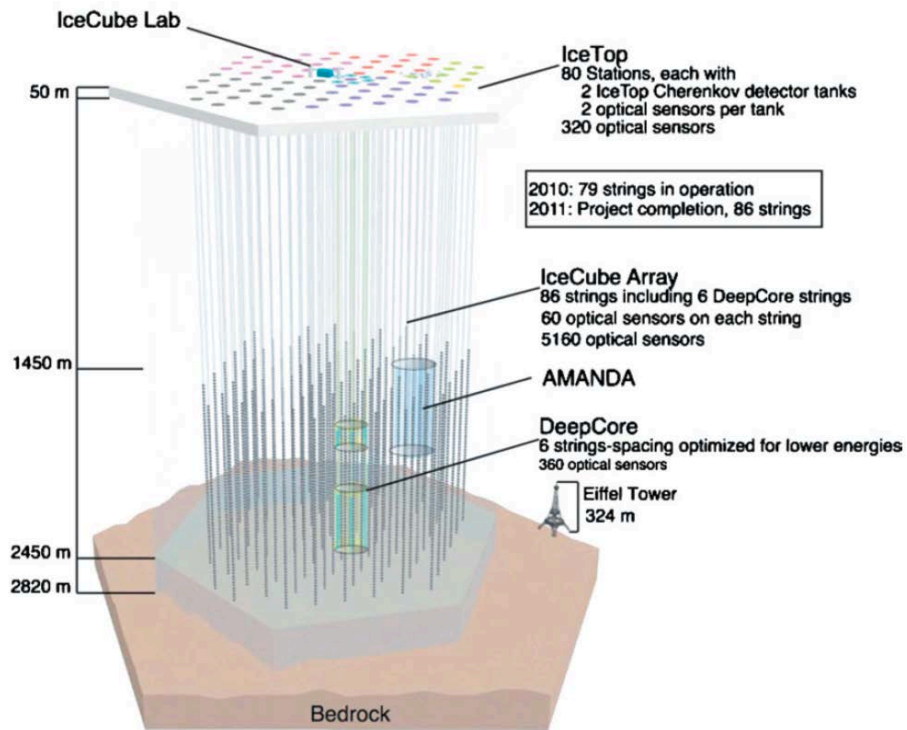
# L/E (Further evidence of neutrino oscillation)

$$P_{\nu_e \rightarrow \nu_e} = 1 - \sin^2 2\theta \sin^2 \left( 1.27 \frac{\Delta m^2 [\text{eV}^2] L [\text{m}]}{E [\text{MeV}]} \right)$$

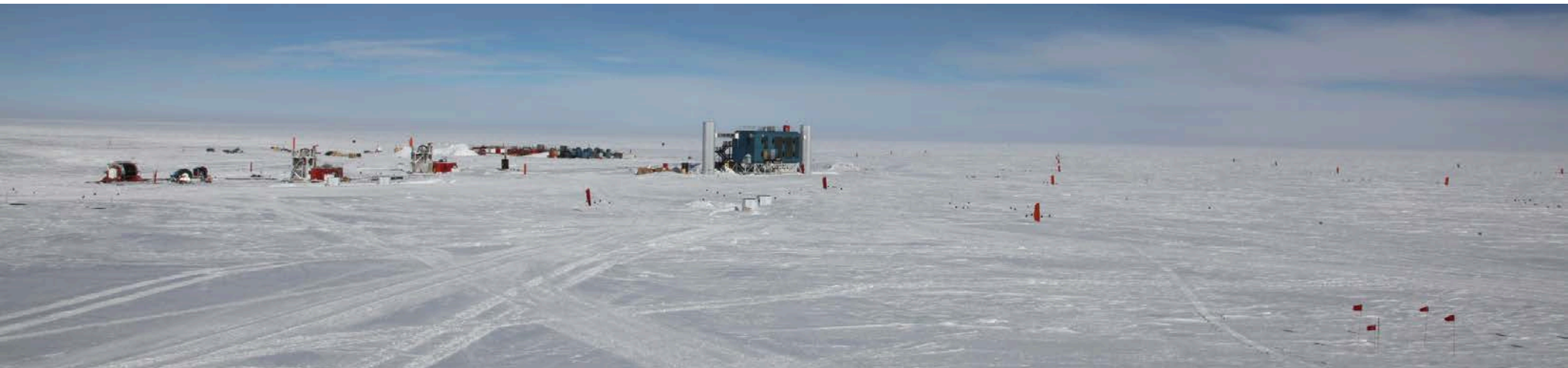


# Cosmic Messenger

## IceCube



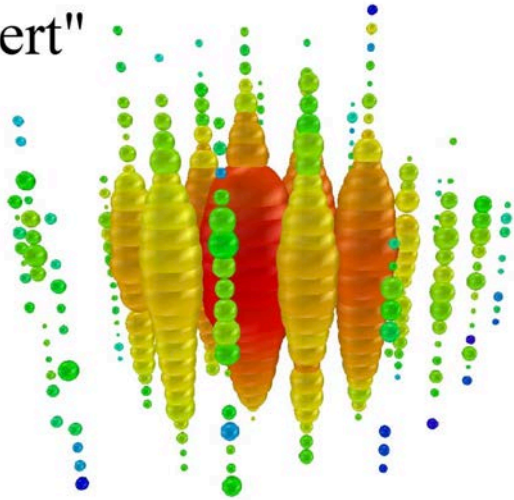
**80+2 events in 6 years (54 in 4 years)**





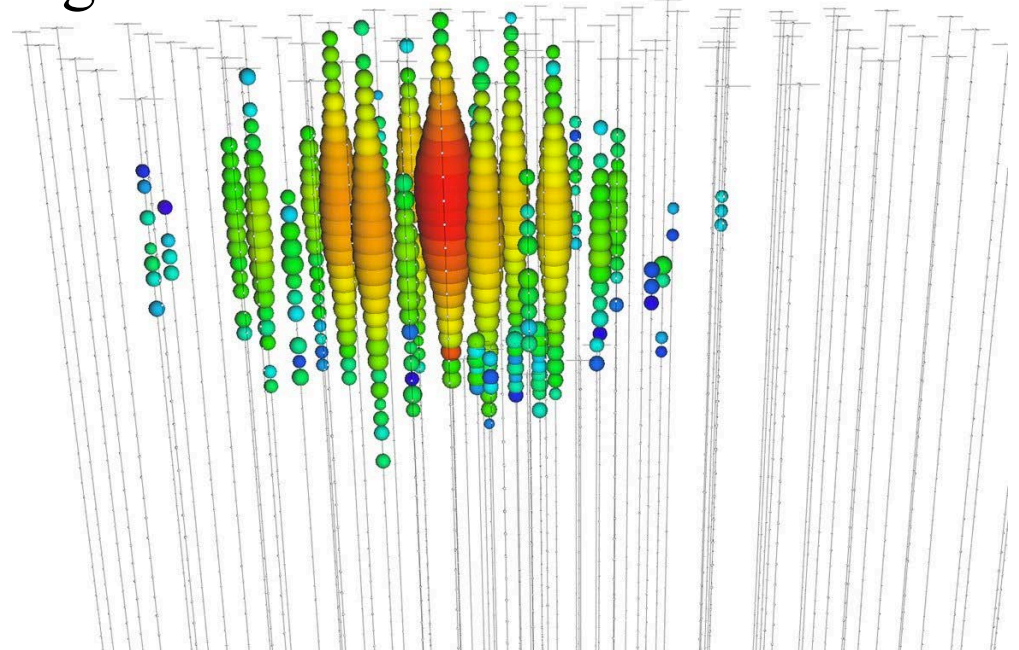
# Highest-energy neutrinos observed IceCube

"Bert"



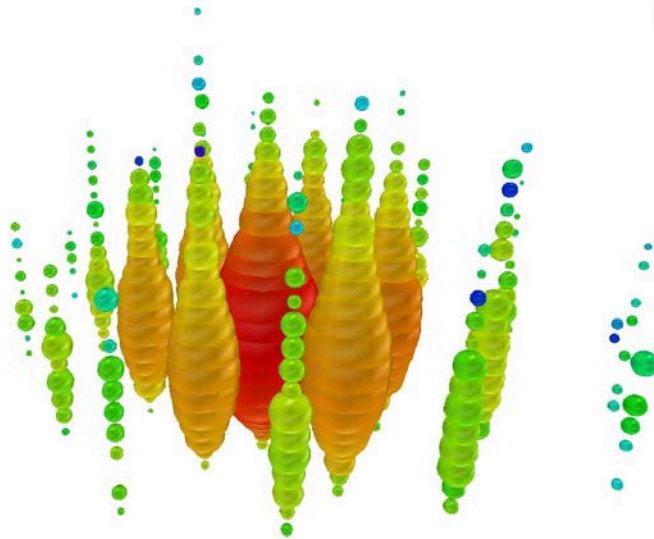
1.04 PeV

"Big Bird"



2 PeV

"Ernie"



1.14 PeV

1 PeV =  $10^{15}$  eV

**How to measure the neutrino mass?**

# How to measure the mass of the neutrino?

(in a model independent way)



$$\pi^+ \rightarrow \mu^+ + \nu_\mu$$

# How to measure the mass of the neutrino?

- Finding the missing mass at accelerator. For example:

$$\pi^+ \rightarrow \mu^+ + \nu_\mu$$

- Energy-momentum conservation says (for pion decay at rest):

$$m_{\nu_\mu}^2 = m_{\pi^+}^2 + m_{\mu^+}^2 - 2m_{\pi^+}(m_{\mu^+}^2 + p_{\mu^+}^2)^{1/2}$$

- How well can the momentum of the muon be measured?  
At an experiment at PSI [Phys. Rev. D53, 6065 (1996)], it was measured to  $\sim 4$  ppm:

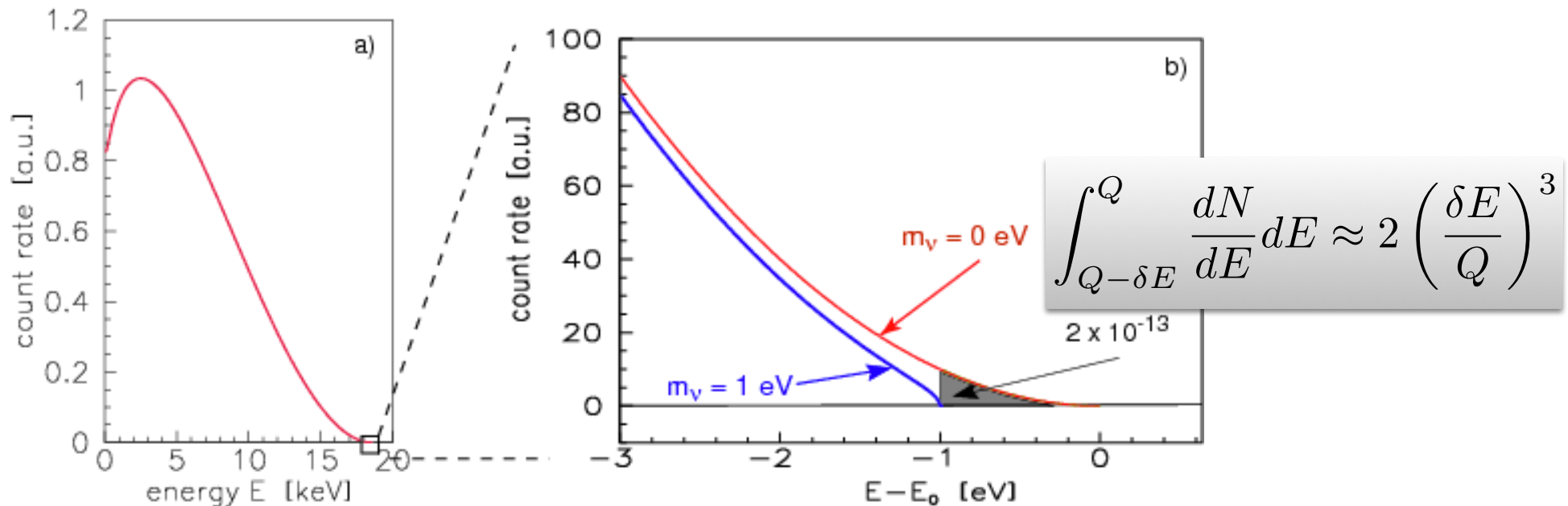
$$p_{\mu^+} = (29.79200 \pm 0.00011) \text{ MeV}/c$$

**Not good enough !**

(when you want to measure neutrino mass to sub-eV level) !

# Determining the neutrino mass from $\beta$ endpoint

$$\frac{dN}{dE} \propto F(E, Z)p(E + m_e)(Q - E) \sum_i |U_{ei}|^2 \sqrt{(Q - E)^2 - m_i^2}$$

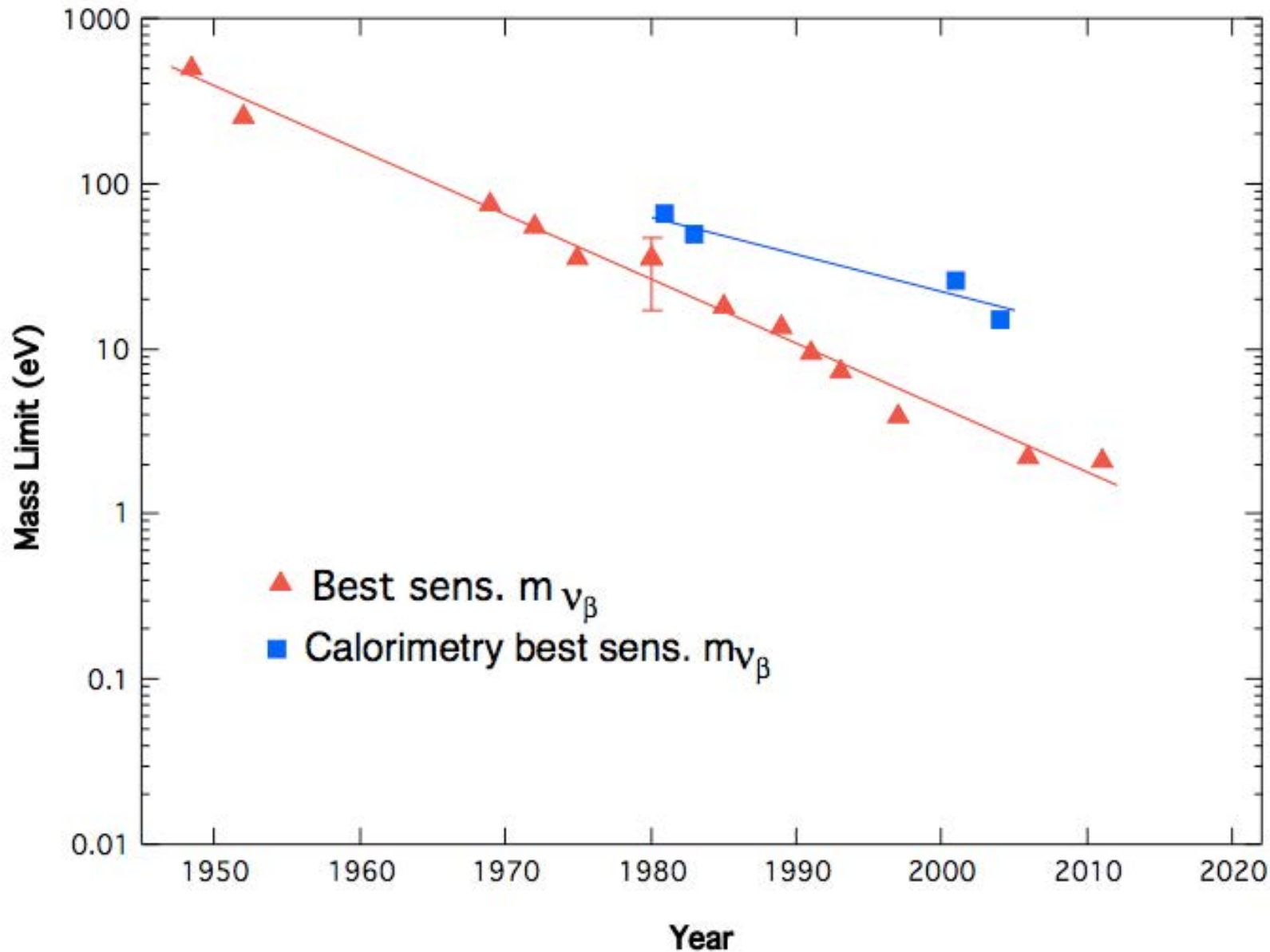


Only a tiny fraction of decays will end up near the endpoint

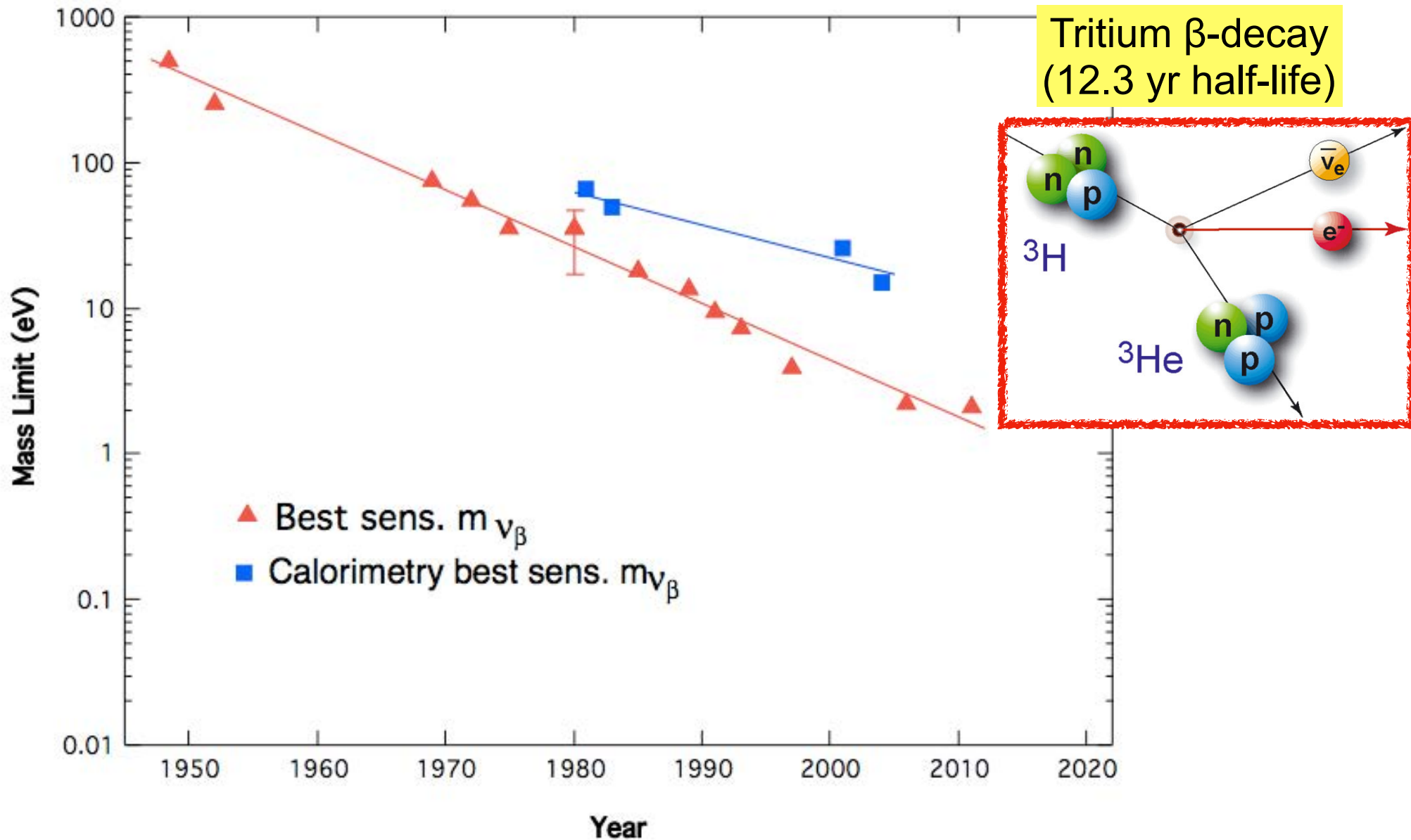
An ideal isotope would have very small  $Q$



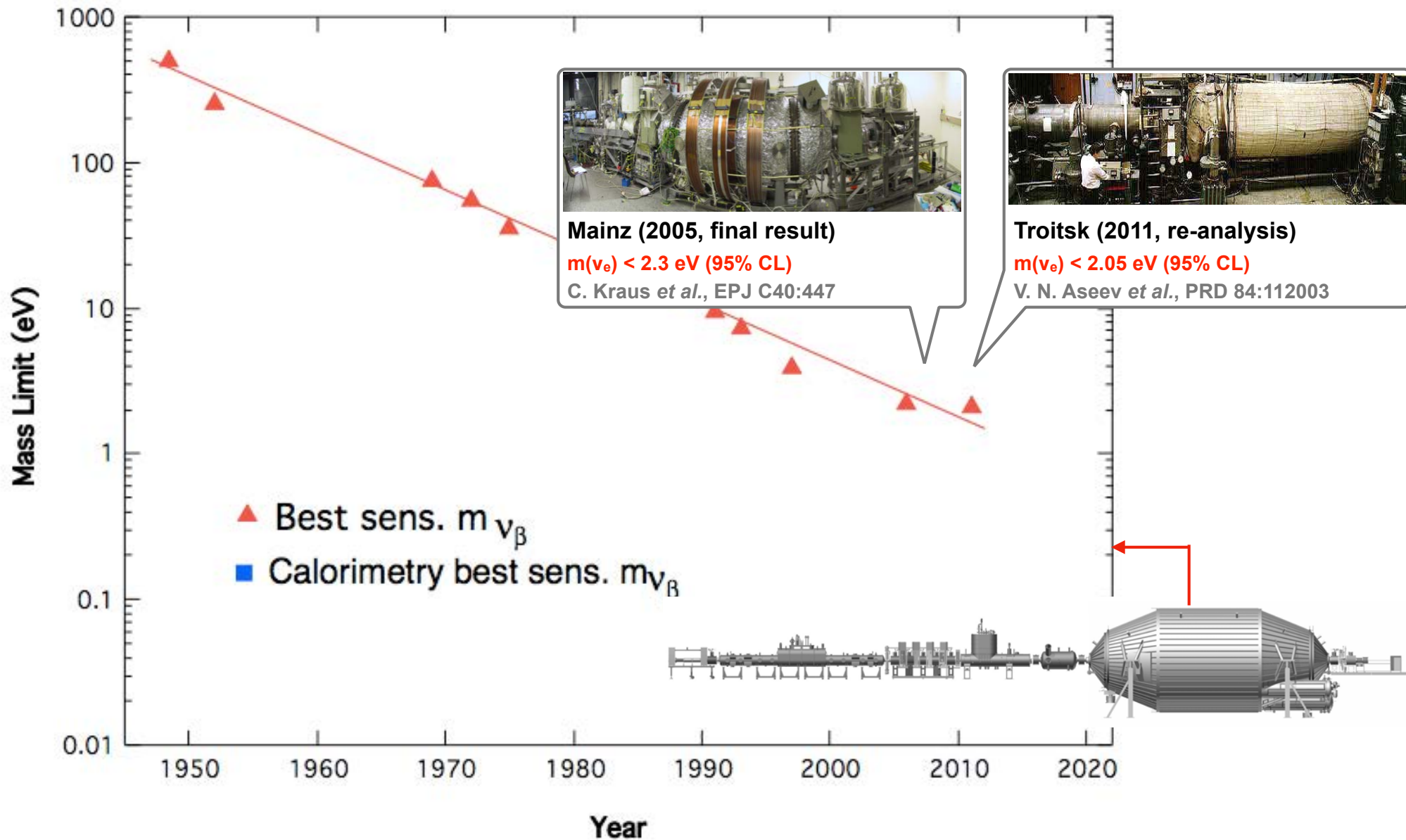
# Neutrino mass limit from beta-decays



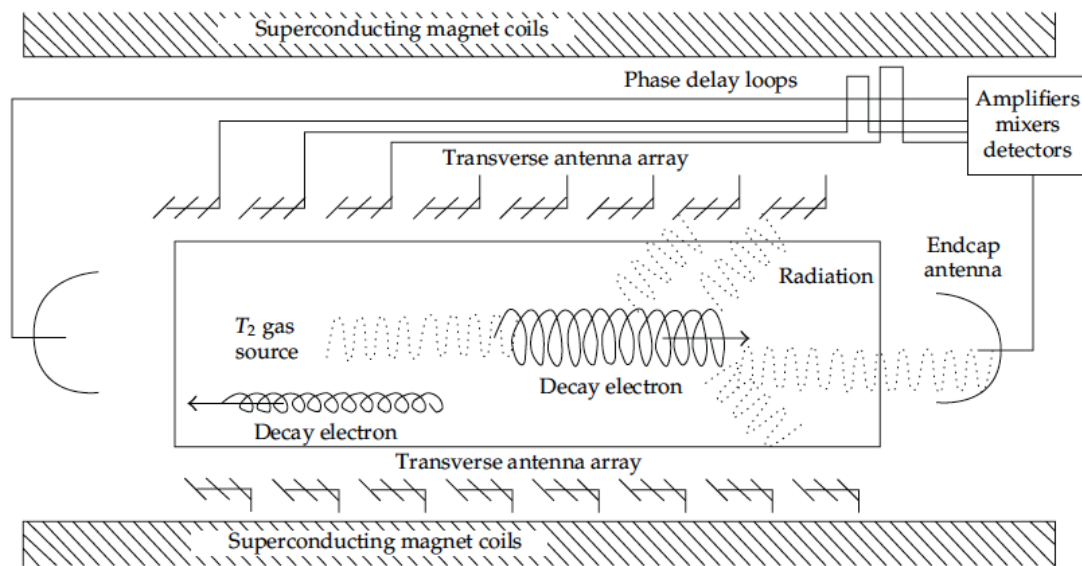
# Neutrino mass limit from beta-decays



# Neutrino mass limit from beta-decays



# Another way to “see” the beta-electrons

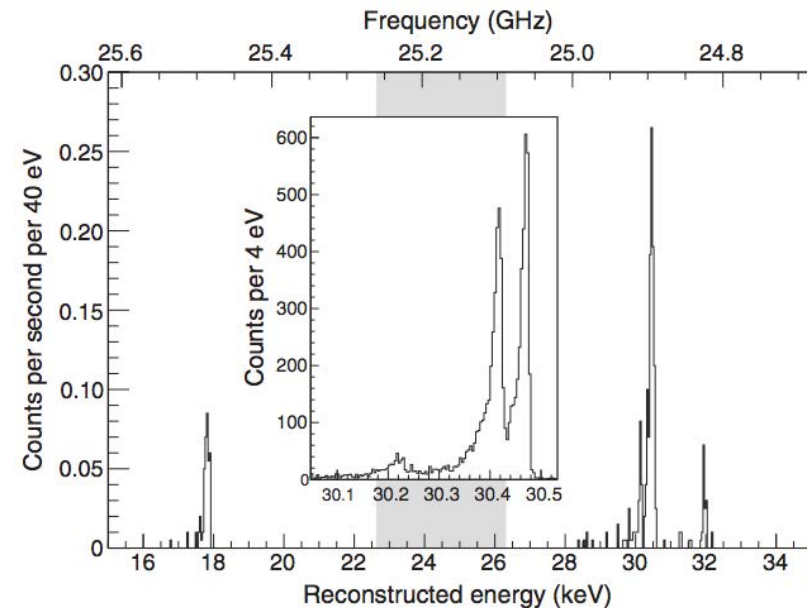
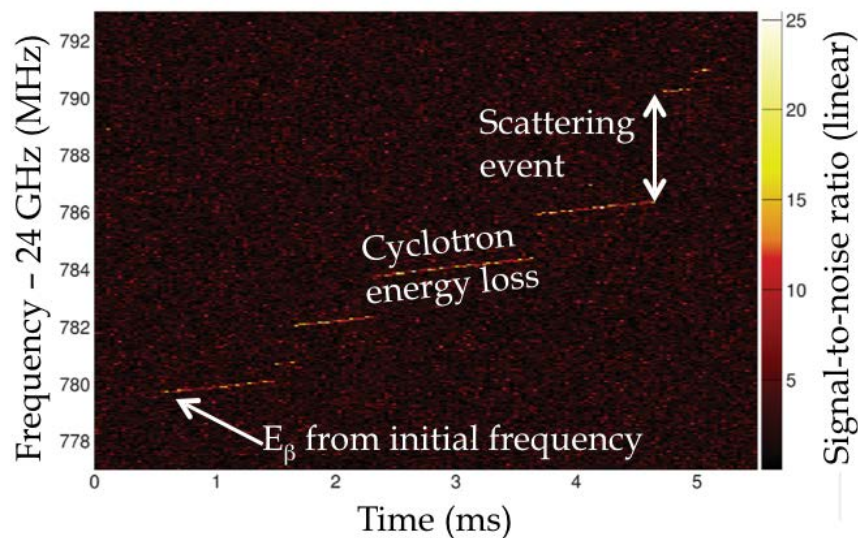


**coherent cyclotron radiation**

$$\omega = \frac{\omega_0}{\gamma} = \frac{qB}{m_e + E}$$



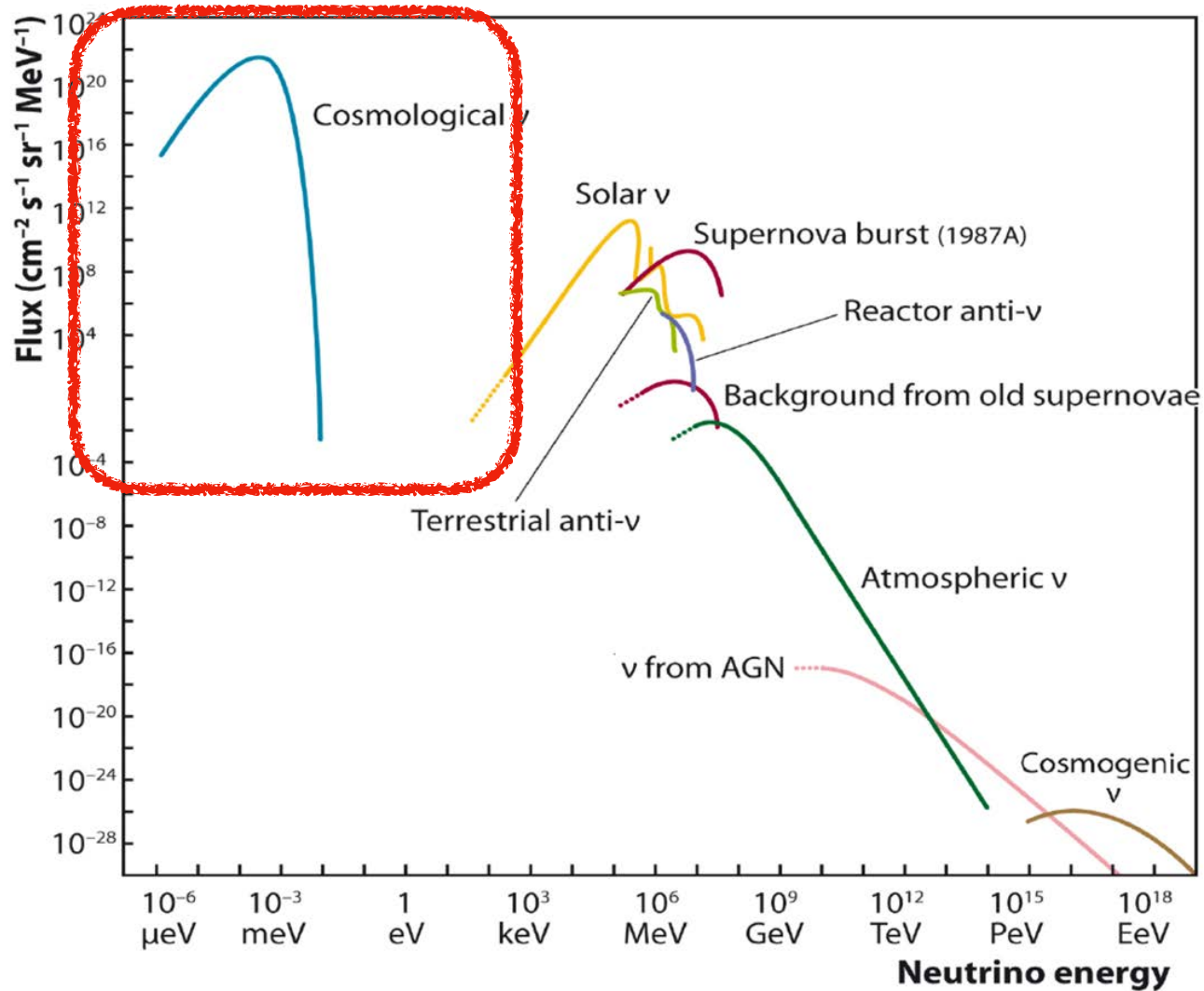
**<sup>83m</sup>Kr test**



**A Nobel idea....**



# Seeing the cosmic neutrino background



$$n_\nu = \left(\frac{3}{4}\right)\left(\frac{4}{11}\right)n_\gamma = 112/\text{cm}^3$$

per (neutrino+antineutrino) species

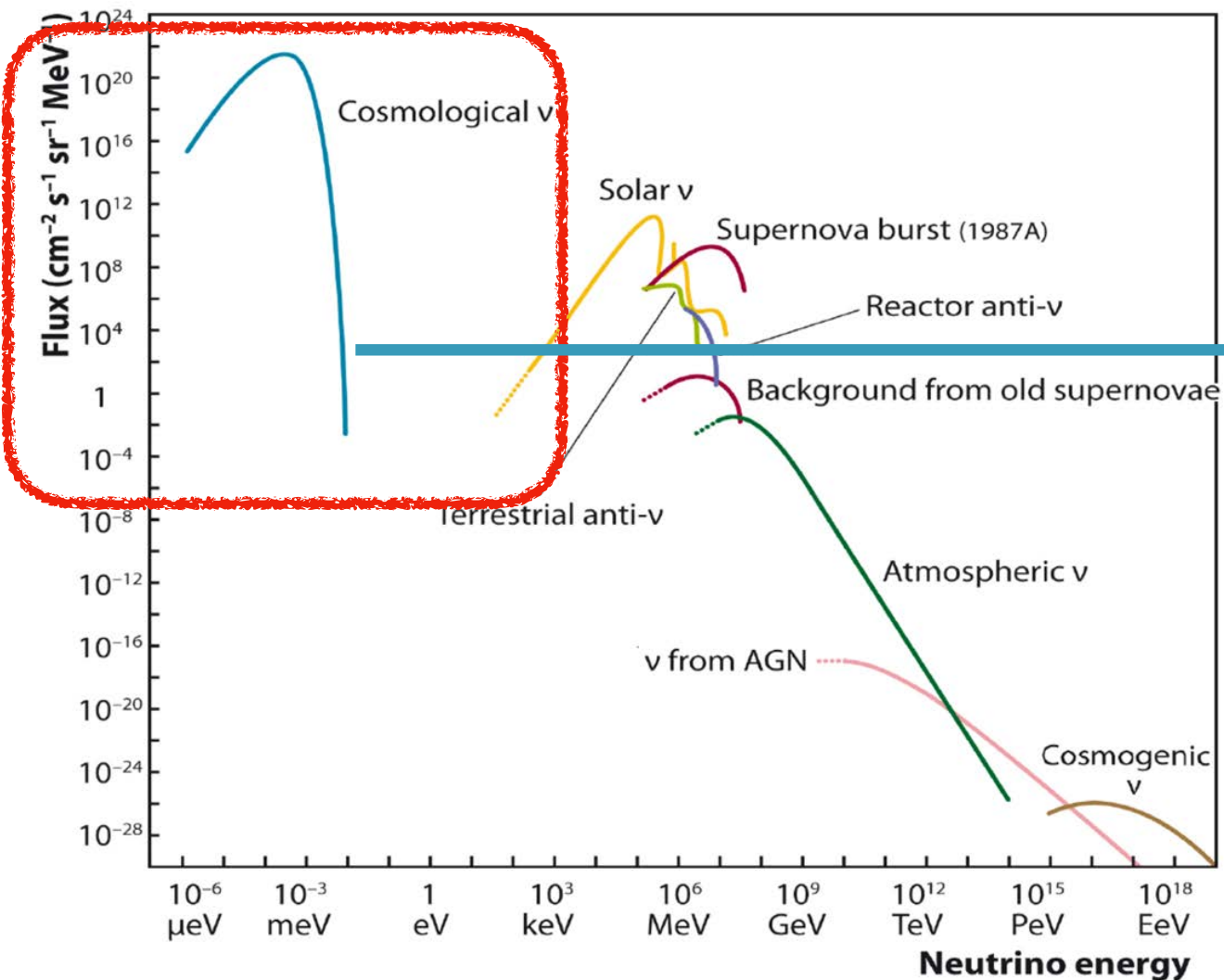
$$T_\nu = 1.95 \text{ K}$$

$$\text{cf } T_\gamma = 2.725 \text{ K}$$

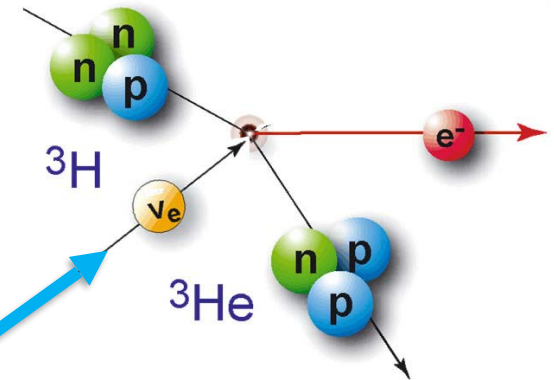
The energy is so low

HOW?

# Seeing the cosmic neutrino background



Neutrino capture on Tritium

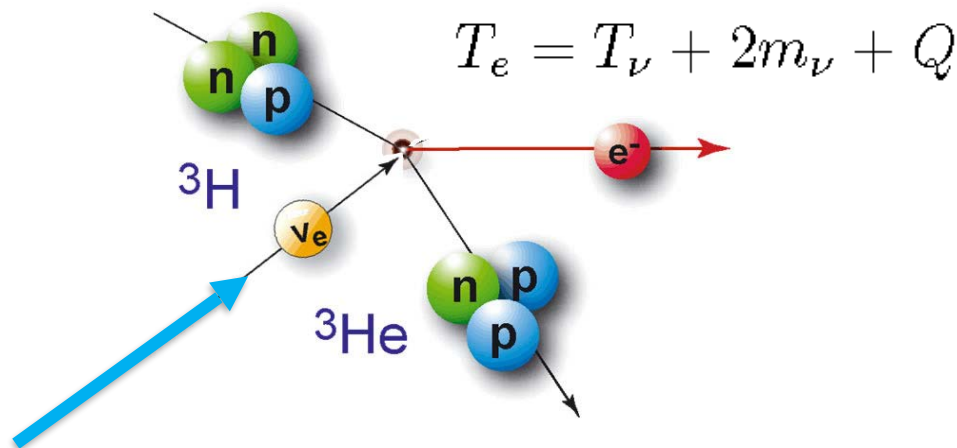


With 100 g of tritium, event rate is

$\sim O(10)$  per year

# Seeing the cosmic neutrino background

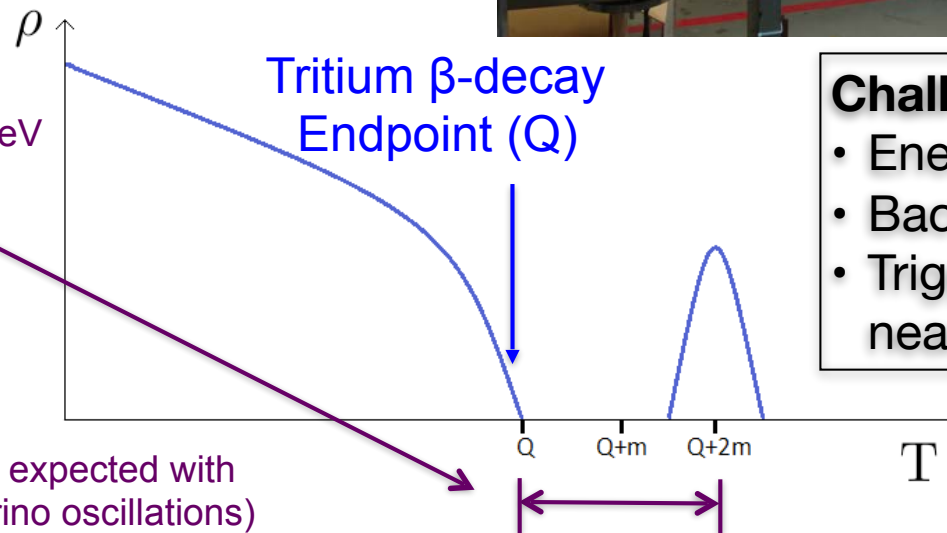
Neutrino capture on Tritium



**What do we know?**

Gap (2m) constrained to  $< \sim 0.6\text{eV}$   
from Cosmology

(some electron flavor expected with  
 $2m > 0.1\text{eV}$  from neutrino oscillations)



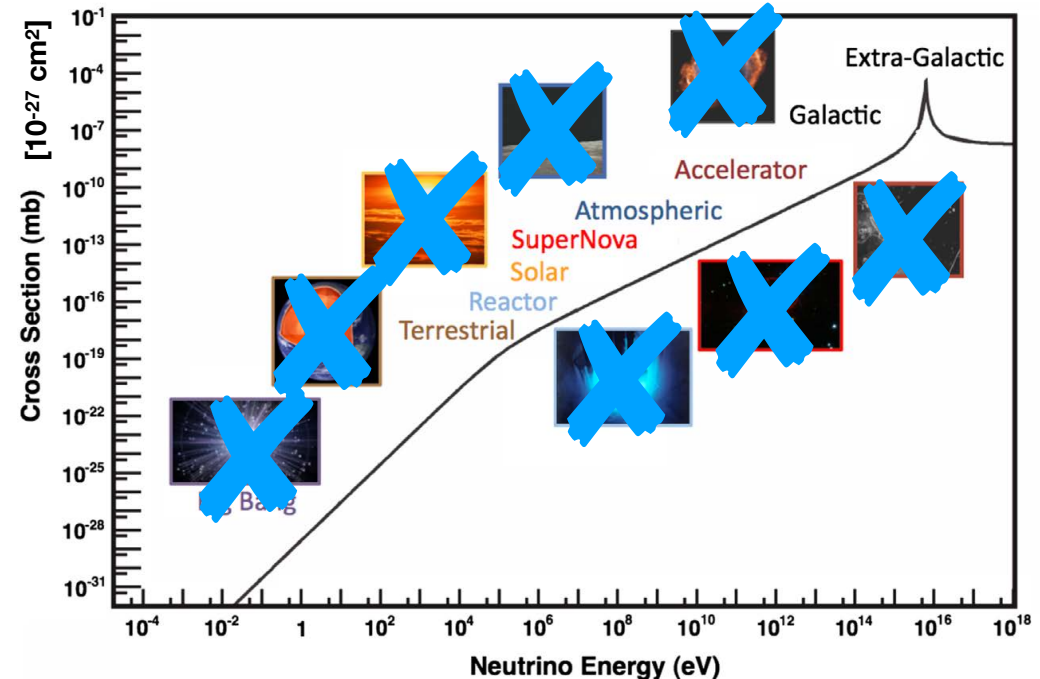
**Challenges:**

- Energy resolution
- Background
- Triggering on the electrons near endpoint

Figure 1: Emitted electron density of states vs kinetic energy for neutrino capture on beta decaying nuclei. The spike at  $Q + 2m$  is the CNB signal

## Neutrino topics that I didn't cover (many):

- Long baseline neutrino experiments (CP violation and neutrino mass hierarchy)
- Neutrino astronomy
- Neutrinoless double beta decays
- Sterile neutrinos (from reactor and beam experiments)
- Neutrinos in cosmology....



But I have covered how to “see” the neutrinos in the energy ranges of the sources in Slide 3, so you can explore these additional topics on your own.

# References

- Christine Sutton, *Spaceship Neutrinos*, Cambridge University Press (1992).
- H. Gallagher et al., *Neutrino-Nucleus Interactions*, Annu. Rev. Nucl. Part. Sci. 61, 355 (2011).
- J. A. Formaggio and G. P. Zeller, *From eV to EeV: Neutrino cross sections across energy scales*, Rev. Mod. Phys. 84, 1307 (2012).
- T. W. Donnelly et al., *Foundations of Nuclear and Particle Physics*, Cambridge University Press (2017).





# Neutrino interactions

## Useful Formulae

$$\begin{aligned}\hbar &= 6.58 \times 10^{-25} \text{ GeV sec} = 1 \\ \hbar c &= 0.197 \text{ GeV F} = 1 \\ (1 \text{ GeV})^{-2} &= 0.389 \text{ mb} \\ \alpha &= \frac{e^2}{4\pi} = \frac{1}{137}\end{aligned}$$

$$x^\mu = (t, \mathbf{x}), \quad p^\mu = (E, \mathbf{p}) = i\left(\frac{\partial}{\partial t}, -\nabla\right) = i\partial^\mu$$

$$p^2 = p^\mu p_\mu = E^2 - \mathbf{p}^2 = m^2$$

$$(\square^2 + m^2)\phi = 0, \quad (i\gamma^\mu \partial_\mu - m)\psi = 0.$$

In an electromagnetic field,  $i\partial^\mu \rightarrow i\partial^\mu + eA^\mu$  (charge  $-e$ )

$$j^\mu = -ie(\phi^* \partial^\mu \phi - \phi \partial^\mu \phi^*), \quad j^\mu = -e\bar{\psi}\gamma^\mu\psi$$

### $\gamma$ -Matrices

$$\begin{aligned}\gamma^\mu \gamma^\nu + \gamma^\nu \gamma^\mu &= 2g^{\mu\nu}, & \gamma^{\mu\dagger} &= \gamma^0 \gamma^\mu \gamma^0. \\ \gamma^{0\dagger} &= \gamma^0, & \gamma^0 \gamma^0 &= I; & \gamma^{k\dagger} &= -\gamma^k, & \gamma^k \gamma^k &= -I, & k &= 1, 2, 3. \\ \gamma^5 &= i\gamma^0 \gamma^1 \gamma^2 \gamma^3, & \gamma^\mu \gamma^5 + \gamma^5 \gamma^\mu &= 0, & \gamma^{5\dagger} &= \gamma^5.\end{aligned}$$

(Trace theorems on pages 123 and 261)

Standard representation:

$$\begin{aligned}\gamma^0 &= \beta = \begin{pmatrix} I & 0 \\ 0 & -I \end{pmatrix}, & \gamma &= \beta\alpha = \begin{pmatrix} 0 & \sigma \\ -\sigma & 0 \end{pmatrix}, & \gamma^5 &= \begin{pmatrix} 0 & I \\ I & 0 \end{pmatrix} \\ \sigma_1 &= \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}, & \sigma_2 &= \begin{pmatrix} 0 & -i \\ i & 0 \end{pmatrix}, & \sigma_3 &= \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}\end{aligned}$$

### Spinors

$$\begin{aligned}(\not{p} - m)u &= 0 & \begin{cases} \bar{u} &= u^\dagger \gamma^0 \\ \not{p} &= \gamma_\mu p^\mu \end{cases} \\ \bar{u}(\not{p} - m) &= 0\end{aligned}$$

$$u^{(r)\dagger} u^{(s)} = 2E\delta_{rs}, \quad \bar{u}^{(r)} u^{(s)} = 2m\delta_{rs}, \quad \sum_{s=1,2} u^{(s)} \bar{u}^{(s)} = \not{p} + m = 2m\Lambda_+$$

$$\frac{1}{2}(1 - \gamma^5)u = u_L, \quad \frac{1}{2}(1 + \gamma^5)u = u_R.$$

If  $m = 0$  or  $E \gg m$ , then  $u_L$  has helicity  $\lambda = -\frac{1}{2}$ ,  $u_R$  has  $\lambda = +\frac{1}{2}$ .

### Kinematics

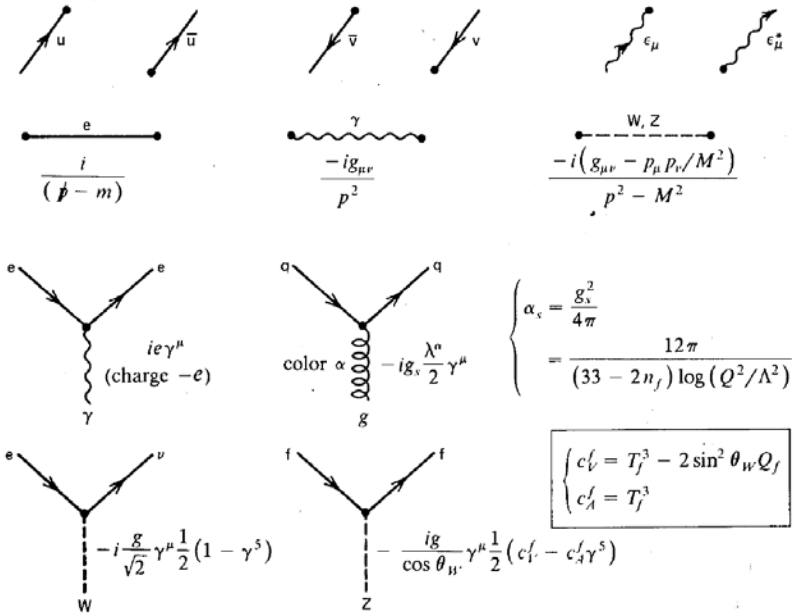
Lorentz invariant phase space ( $P \rightarrow p_1 + \dots + p_n$ )

$$dQ = (2\pi)^4 \delta^4(P - p_1 - \dots - p_n) \prod_{i=1}^n \frac{d^3 p_i}{(2\pi)^3 2E_i}$$

$$\text{Scattering: } \frac{d\sigma}{d\Omega} \Big|_{\text{cm}} = \frac{1}{64\pi^2 s} \frac{p_f}{p_i} |\mathcal{M}|^2$$

$$\text{Decay: } d\Gamma(A \rightarrow 1 + \dots + n) = \frac{|\mathcal{M}|^2}{2m_A} dQ.$$

### Feynman Rules for $-i\mathcal{M}$

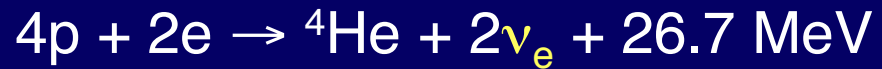


$f$	$Q_f$	$(T_f^3)_L$	$(T_f^3)_R$
u, c, t	$+\frac{2}{3}$	$\frac{1}{2}$	0
d, s, b	$-\frac{1}{3}$	$-\frac{1}{2}$	0
$\nu_e, \nu_\mu, \nu_\tau$	0	$\frac{1}{2}$	—
$e^-, \mu^-, \tau^-$	-1	$-\frac{1}{2}$	0

$$\sin^2\theta_W \approx 0.23, \quad g \sin\theta_W = e, \quad G = \frac{\sqrt{2}g^2}{8M_W^2} \approx 1.17 \times 10^{-5} \text{ GeV}^{-2}$$

# Solar Neutrinos

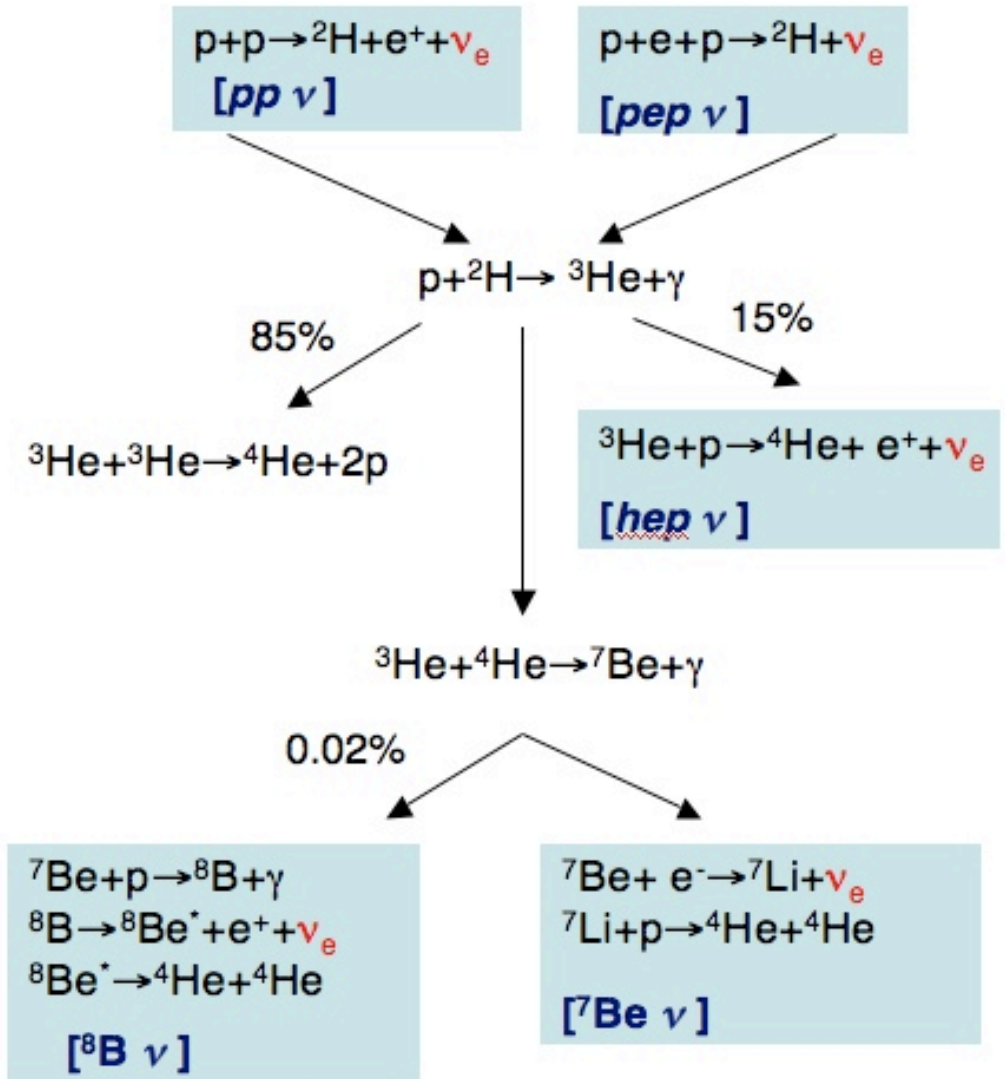
*pp* chain:



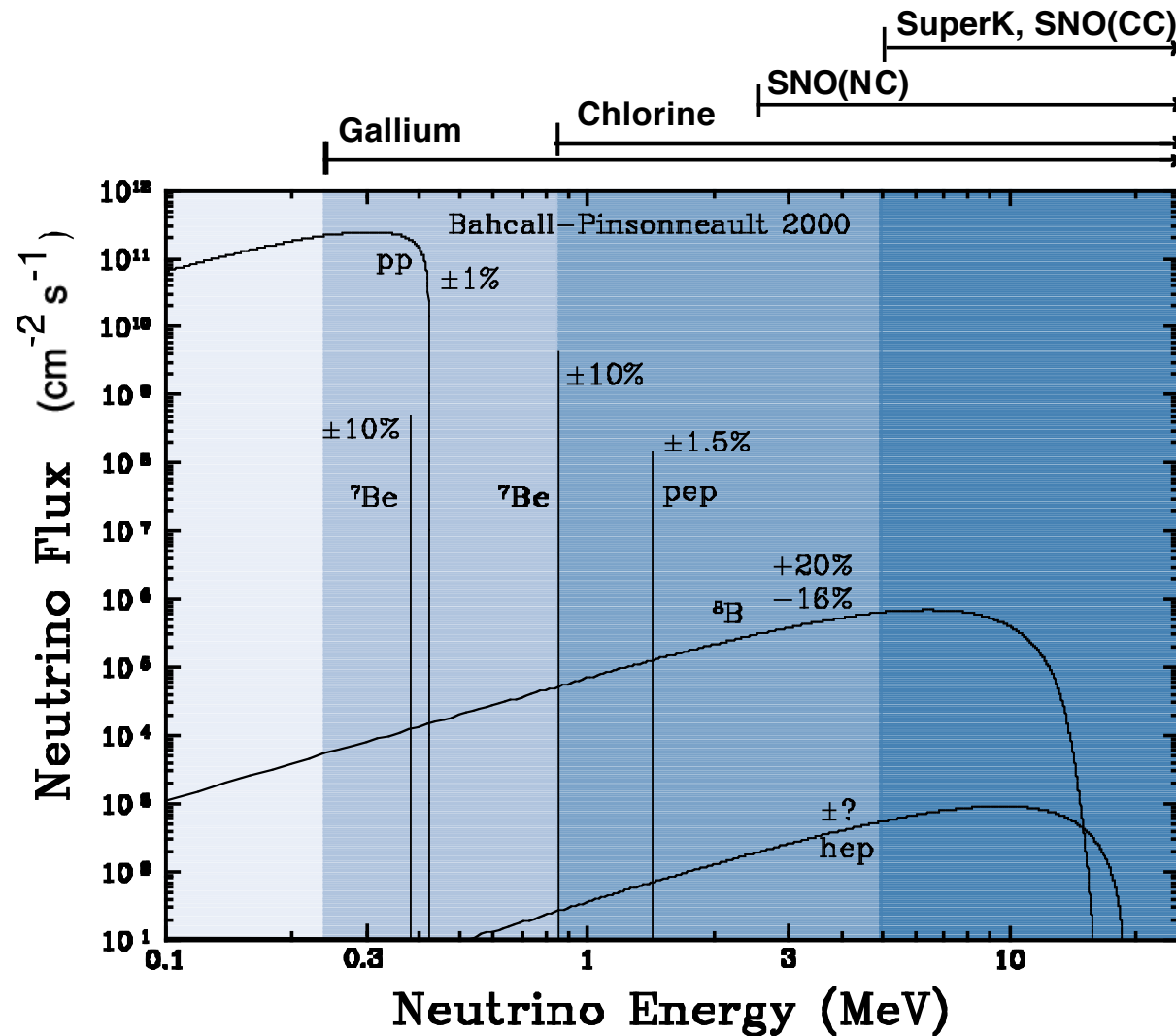
Detailed computer  
model of solar  
evolution



Standard  
Solar  
Model



# Standard Solar Model



pp chain should only produce  $\nu_e$

# Aside: Neutrino Oscillations

Standard Parameterization of Mixing Matrix (as CKM)

$$U = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & s_{13}e^{-i\delta_{13}} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta_{13}} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 1 & 0 & 0 \\ 0 & e^{i\lambda_{21}} & 0 \\ 0 & 0 & e^{i\lambda_{31}} \end{pmatrix}$$

$$= \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta_{13}} \\ -s_{12}c_{23}-c_{12}s_{23}s_{13}e^{i\delta_{13}} & c_{12}c_{23}-s_{12}s_{23}s_{13}e^{i\delta_{13}} & s_{23}c_{13} \\ s_{12}s_{23}-c_{12}c_{23}s_{13}e^{i\delta_{13}} & -c_{12}s_{23}-s_{12}c_{23}s_{13}e^{i\delta_{13}} & c_{23}c_{13} \end{pmatrix} \begin{pmatrix} 1 & 0 & 0 \\ 0 & e^{i\lambda_{21}} & 0 \\ 0 & 0 & e^{i\lambda_{31}} \end{pmatrix}$$

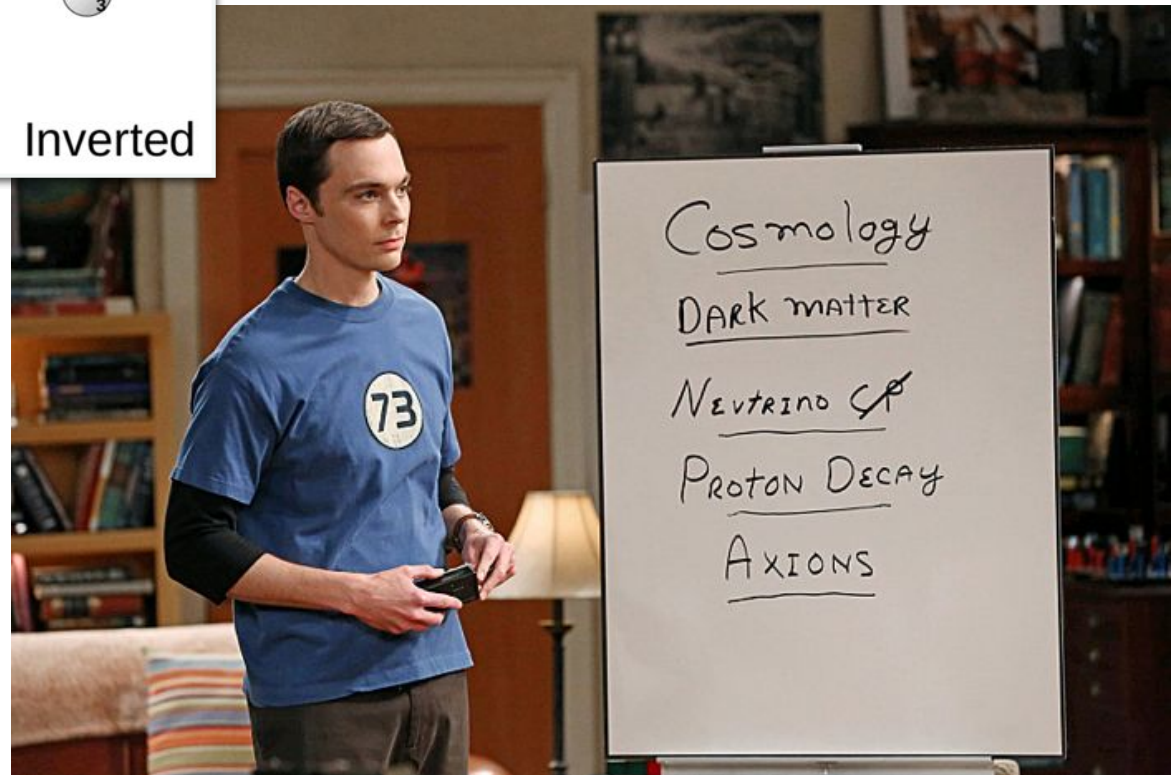
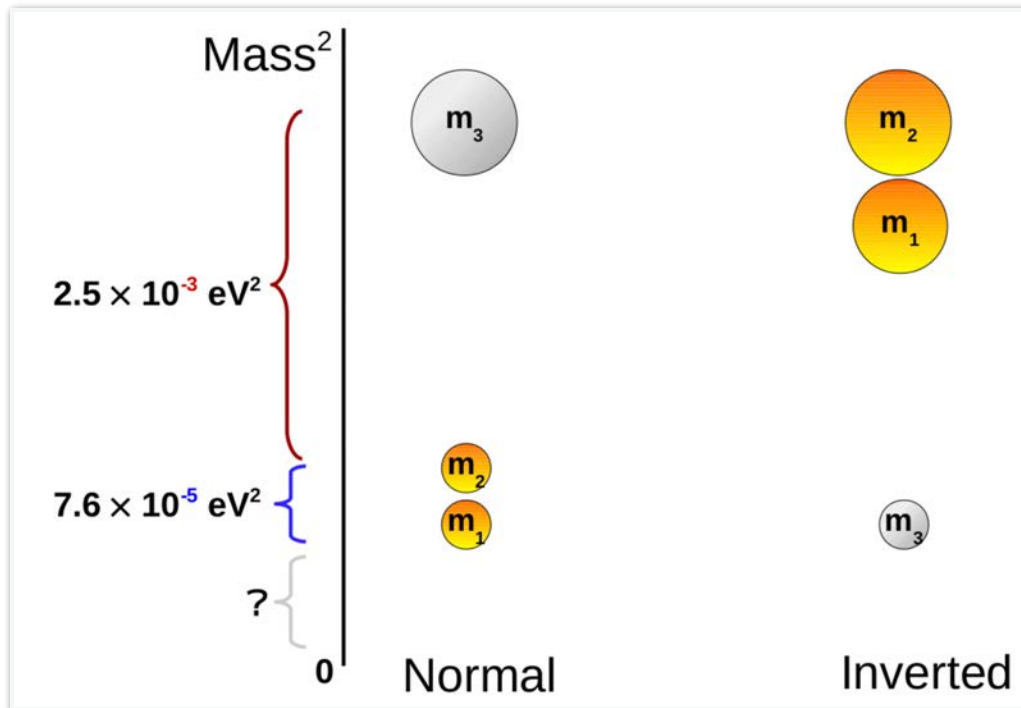
$$c_{ab} \equiv \cos \vartheta_{ab} \quad s_{ab} \equiv \sin \vartheta_{ab} \quad 0 \leq \vartheta_{ab} \leq \frac{\pi}{2} \quad 0 \leq \delta_{13}, \lambda_{21}, \lambda_{31} < 2\pi$$

$$\text{OSCILLATION PARAMETERS} \quad \left\{ \begin{array}{l} 3 \text{ Mixing Angles: } \vartheta_{12}, \vartheta_{23}, \vartheta_{13} \\ 1 \text{ CPV Dirac Phase: } \delta_{13} \\ 2 \text{ independent } \Delta m_{kj}^2 \equiv m_k^2 - m_j^2: \Delta m_{21}^2, \Delta m_{31}^2 \end{array} \right.$$

2 CPV Majorana Phases:  $\lambda_{21}, \lambda_{31} \iff |\Delta L| = 2$  processes



# Mass Hierarchy & CPV - Future

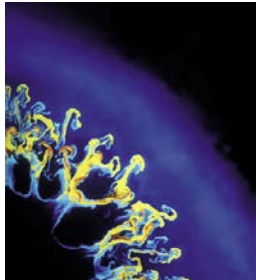


# CPV & MH - Future

Now

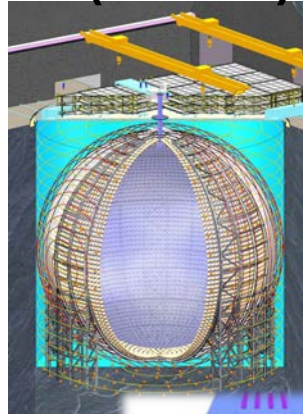
2026

Supernovae

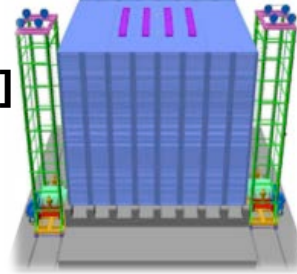


[Scholberg]

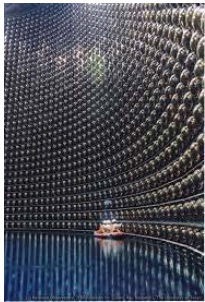
JUNO (20kt LS) [Gu]



INO  
[Singh]



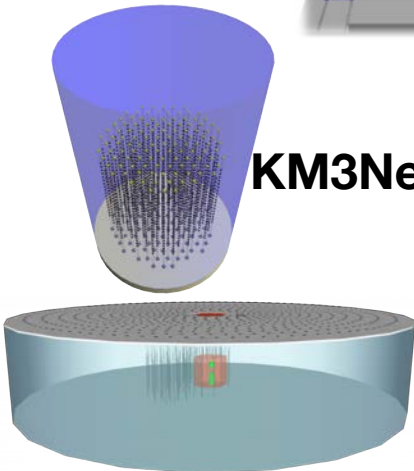
SuperK  
[Mine]



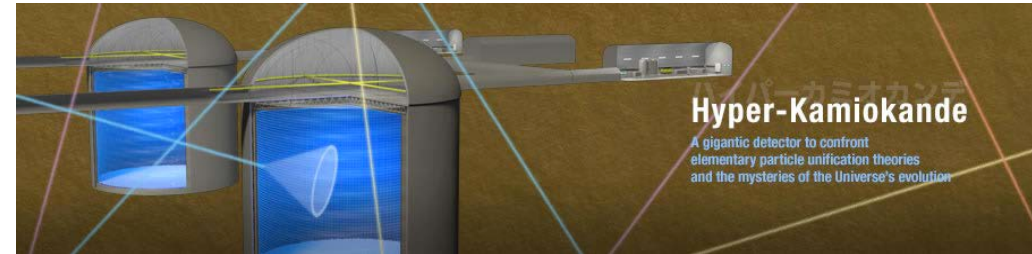
CHIPS  
[Thomas]



KM3Net-ORCA  
[Coelho]



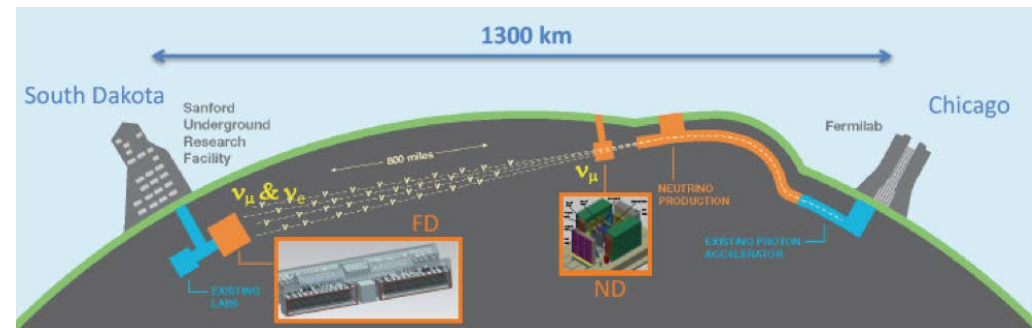
IceCube/DeepCore/PINGU [DeYoung]



Hyper-Kamiokande

A gigantic detector to confront elementary particle unification theories and the mysteries of the Universe's evolution

Hyper-K (187 kt H<sub>2</sub>O FV) [Takeuchi]



DUNE (40 kt LAr) [Ji]

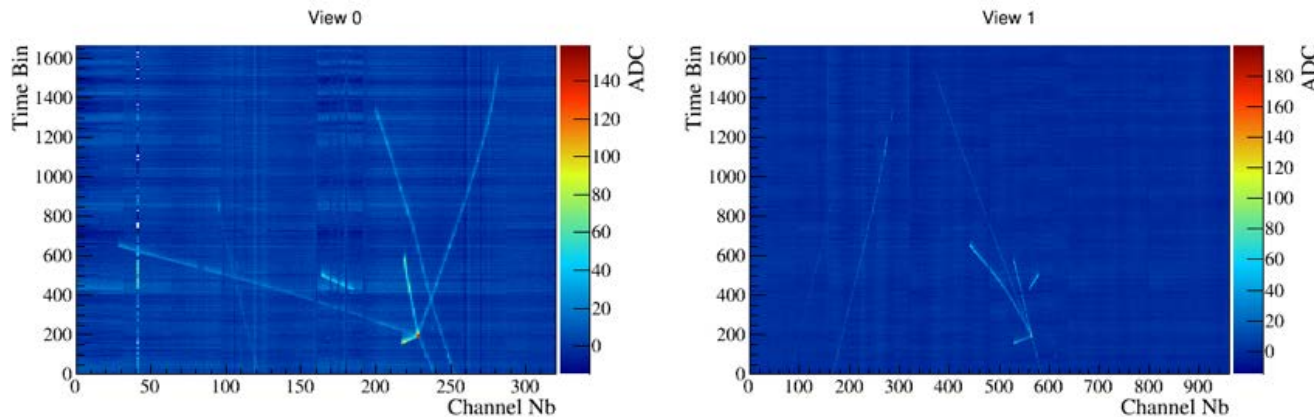
# CPV & MH - Future

## Hyper-K

- Current performance of new 50 cm PMT
  - SK-PMT x2 photon detection
  - SK-PMT x2 timing resolution ( $\sim 1.1\text{ns}$ )
  - Higher pressure tolerance ( $> 80\text{ m}$ )
  - Dark rate: 7.5 kHz (as of 2016)
    - $\rightarrow$  trying to reduce to SK-PMT level ( $< 4\text{kHz}$ )



[Takeuchi]

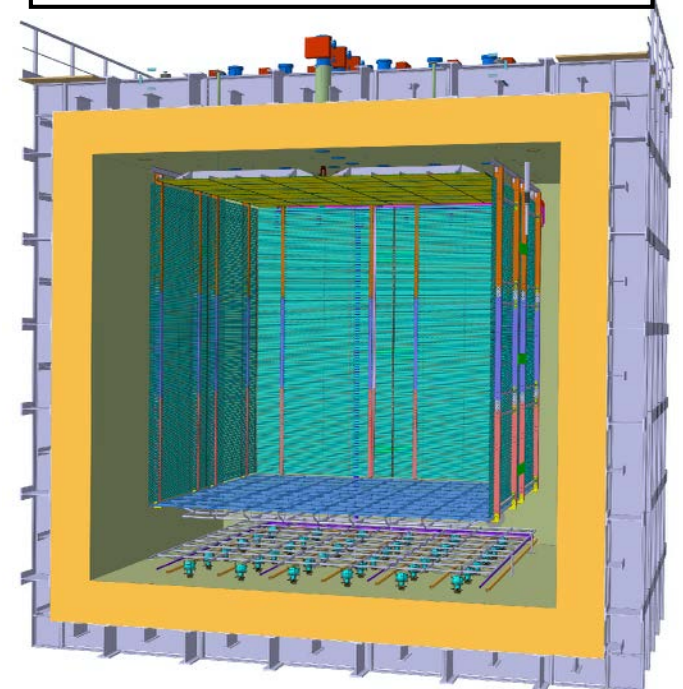


Reached design spec of 2.5 kV/cm extraction field

[Zambelli]

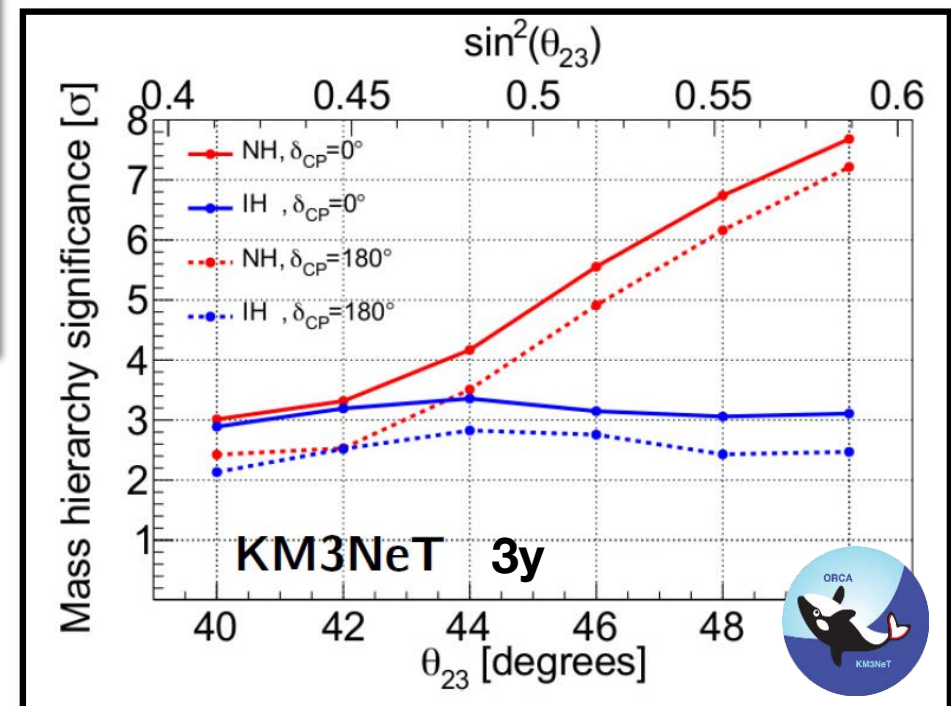
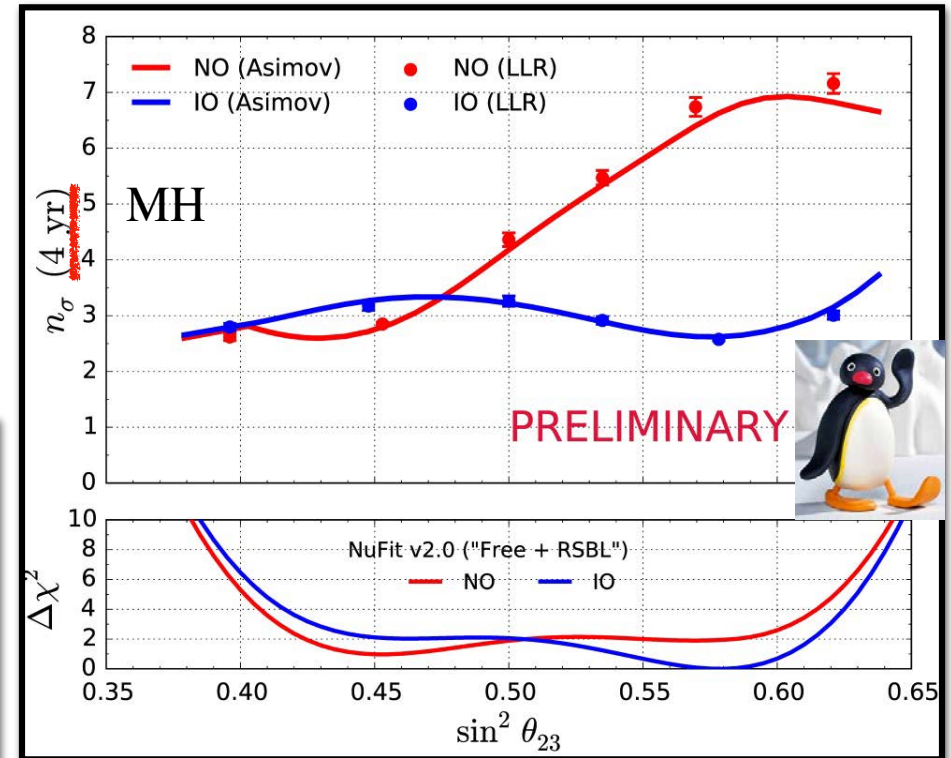
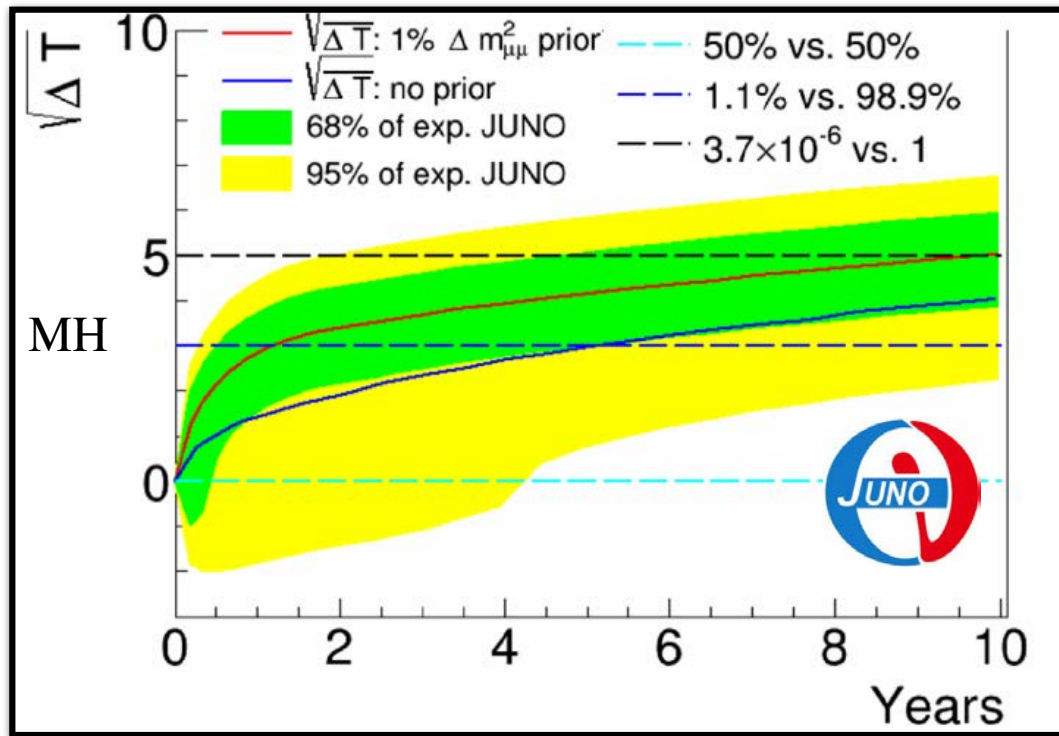
Technologies that I found impressive

protoDUNE dual-phase  
LAr TPC R&D

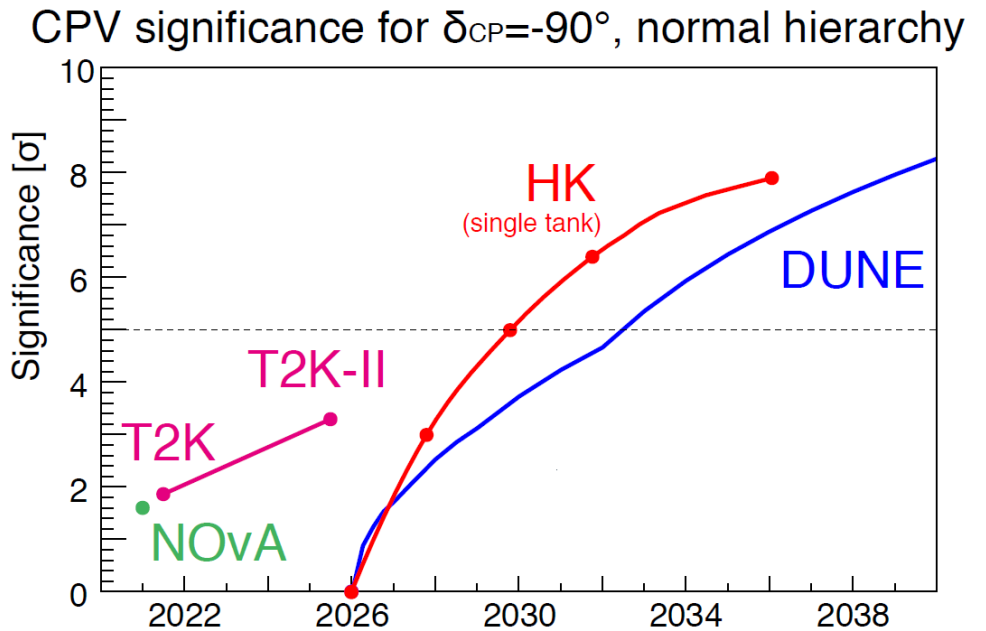
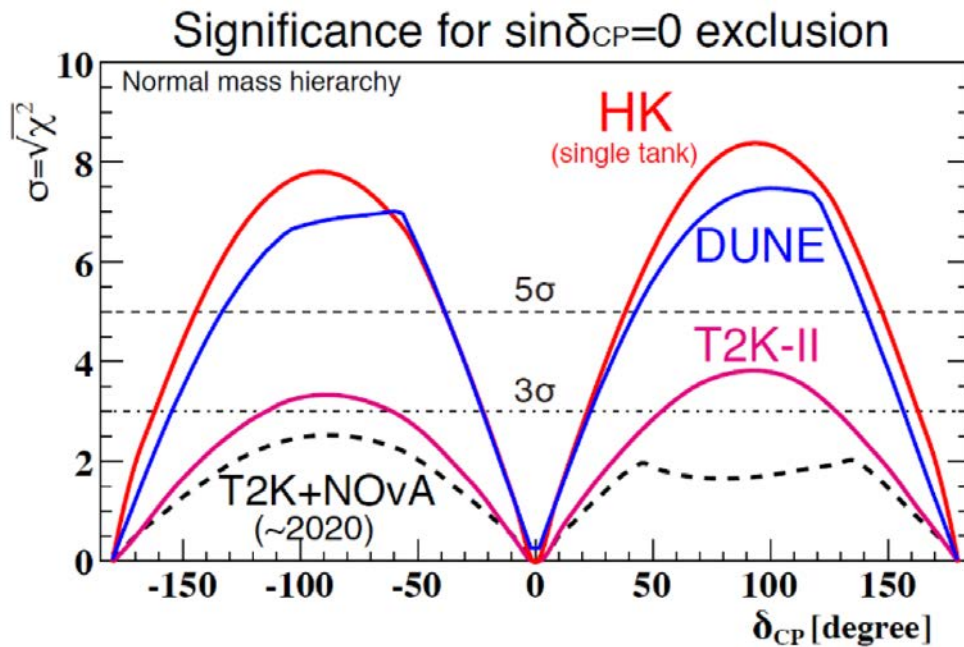




# CPV & MH - Future



# CPV & MH - Future



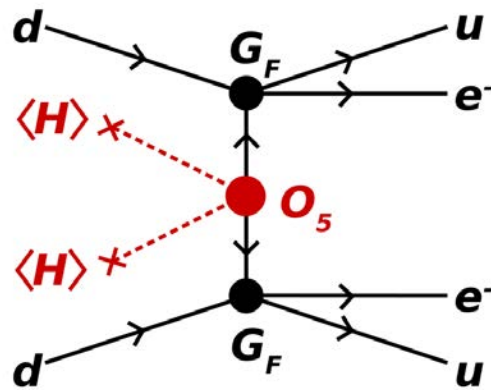
1.3 MW  $\times$  10 years ( $10^8$  sec),  $\nu:\bar{\nu} = 1:3$

- $\sim 8\sigma$  exclusion if  $\delta_{CP} = \pm 90^\circ$
- $\sim 6\sigma$  exclusion if  $\delta_{CP} = \pm 45^\circ$
- Observe CPV for 60% of  $\delta_{CP}$  with  $>5\sigma$  significance

- T2K favors  $\delta_{CP} = -90^\circ$ 
  - PRL 118, 151801 (2017)
  - Super-K atmospheric  $\nu$  data also
- It could be possible that ongoing experiments discover CPV ( $\sim 3\sigma$ )
- T2K  $\rightarrow$  T2K-II  $\rightarrow$  Hyper-K
- Seamless program to get timely results



# “Vanilla” mass mechanism



Halflife

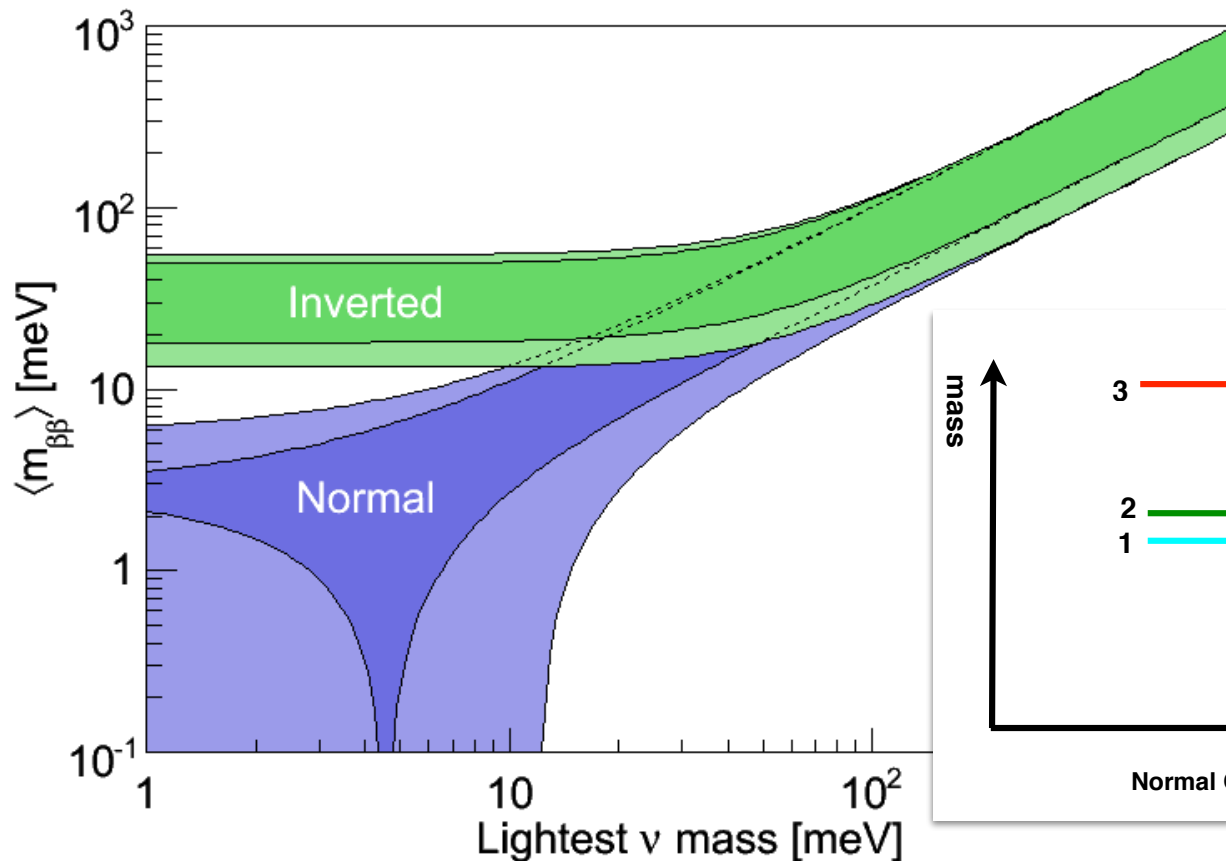
mass scale

$$(T_{1/2}^{0\nu})^{-1} = G_{0\nu}(Q_{\beta\beta}, Z) |M_{0\nu}|^2 \langle m_{\beta\beta} \rangle^2$$

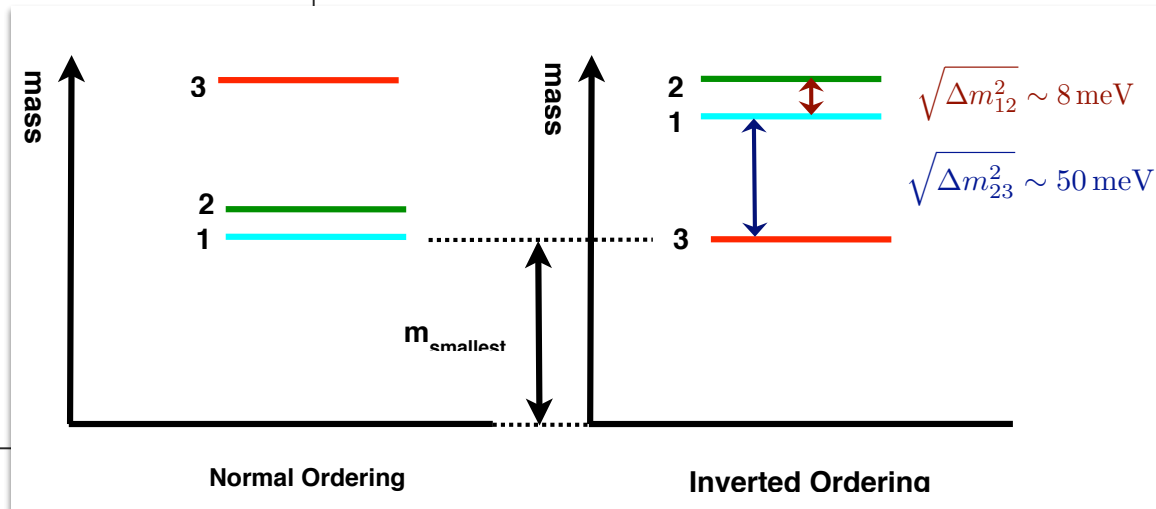
form  
factor

nuclear  
matrix  
element

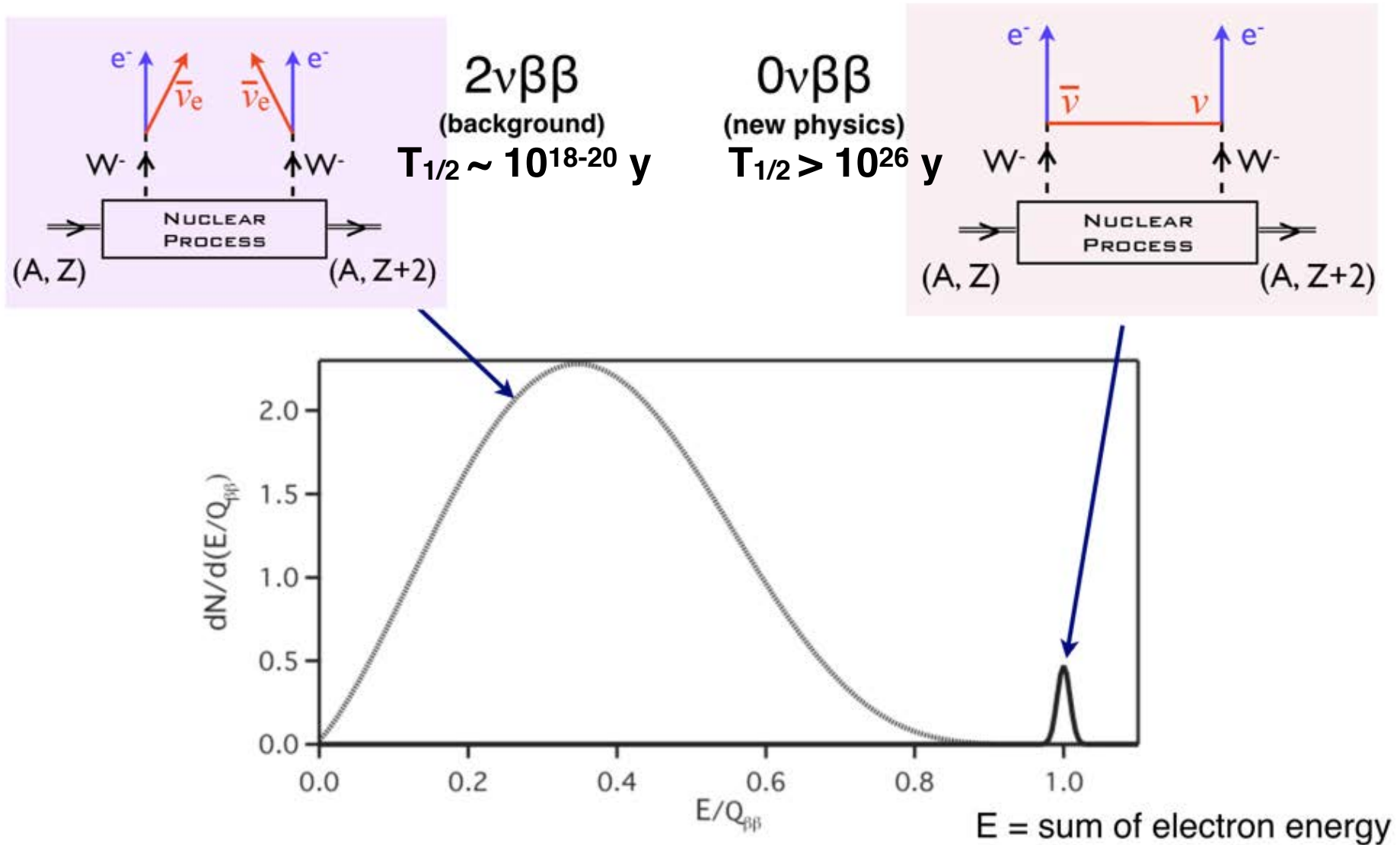
effective  
Majorana  
mass



$$\langle m_{\beta\beta} \rangle = \left| \sum_{i=1}^3 U_{ei}^2 m_i \right|$$



# Signal



Energy resolution and low backgrounds are keys!

# Considerations

$$T_{1/2}^{0\nu}(\text{FOM}) \propto a \cdot \epsilon \cdot \sqrt{\frac{M \cdot t}{b \cdot \delta E}}$$

- Preferably:
  - high isotopic abundance
  - high efficiency
  - large mass
  - long exposure
  - low background
  - good energy resolution

**There is not an obvious choice of isotope or detector technology**

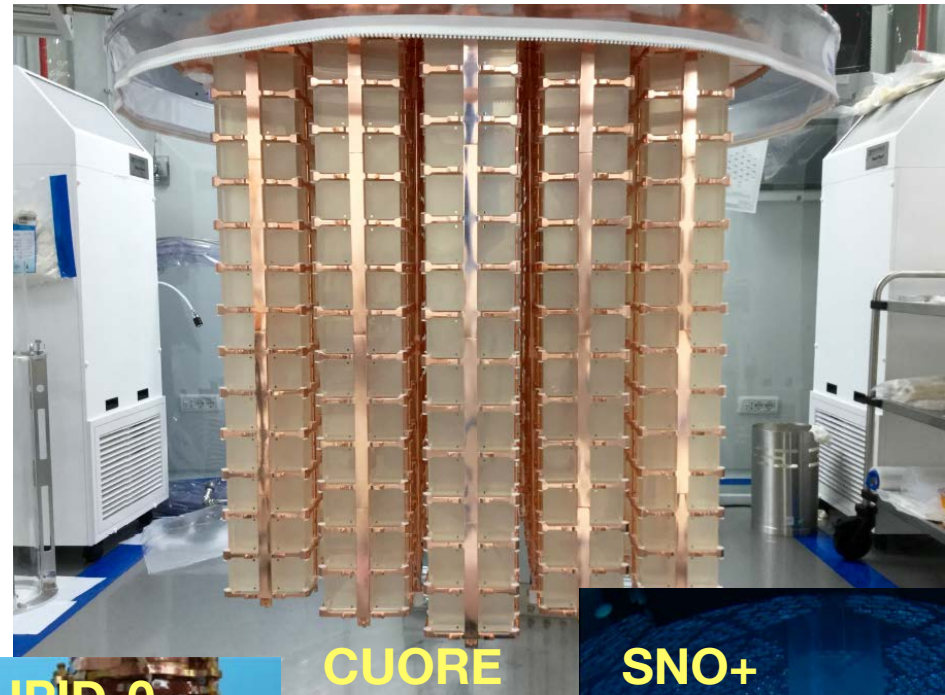
# Many experimental ideas...presented here

**Table 1.** Overview of present and future  $0\nu\beta\beta$  decay experiments, their energy resolution and sensitivity to event topology (i.e. the individual energy of the electrons and/or their angular correlation, useful to distinguish mechanisms). Timescales, references and details can be found in [7, 14, 16].

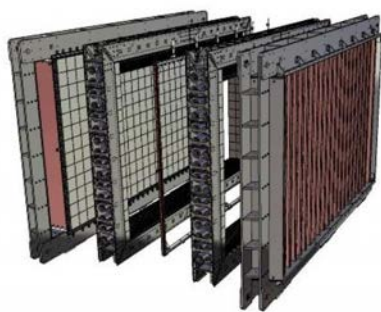
Name	Isotope	Source = detector			Source $\neq$ detector
		$\Delta E$ high	$\Delta E$ low	Topology	Topology
AMoRE	$^{100}\text{Mo}$	✓	—	—	—
CANDLES	$^{48}\text{Ca}$	—	✓	—	—
COBRA	$^{116}\text{Cd}$ (and $^{130}\text{Te}$ )	—	—	✓	—
CUORE	$^{130}\text{Te}$	✓	—	—	—
CUPID	$^{82}\text{Se} / ^{100}\text{Mo} / ^{116}\text{Cd} / ^{130}\text{Te}$	✓	—	—	—
DCBA/MTD	$^{82}\text{Se} / ^{150}\text{Nd}$	—	—	—	✓
EXO	$^{136}\text{Xe}$	—	—	✓	—
GERDA	$^{76}\text{Ge}$	✓	—	—	—
KamLAND-Zen	$^{136}\text{Xe}$	—	✓	—	—
LUCIFER	$^{82}\text{Se} / ^{100}\text{Mo} / ^{130}\text{Te}$	✓	—	—	—
LUMINEU	$^{100}\text{Mo}$	✓	—	—	—
MAJORANA	$^{76}\text{Ge}$	✓	—	—	—
MOON	$^{82}\text{Se} / ^{100}\text{Mo} / ^{150}\text{Nd}$	—	—	—	✓
NEXT	$^{136}\text{Xe}$	—	—	✓	—
SNO+	$^{130}\text{Te}$	—	✓	—	—
SuperNEMO	$^{82}\text{Se} / ^{150}\text{Nd}$	—	—	—	✓
XMASS	$^{136}\text{Xe}$	—	✓	—	—



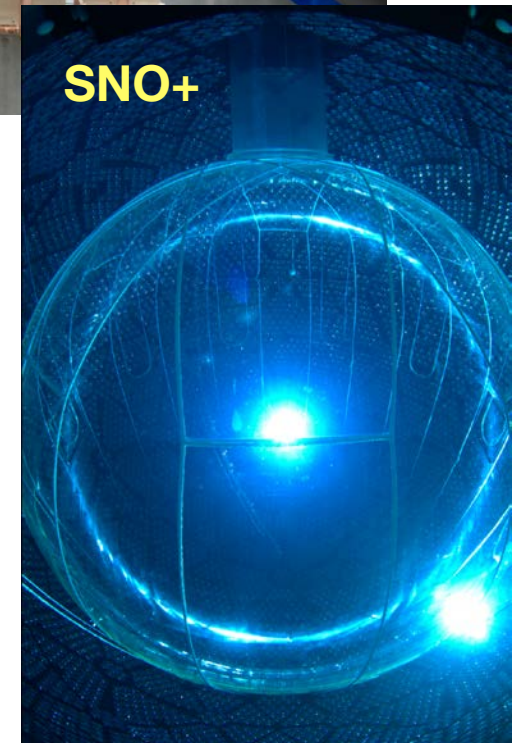
# Many experimental ideas...presented here



NEMO-3 (2003 - 2011)



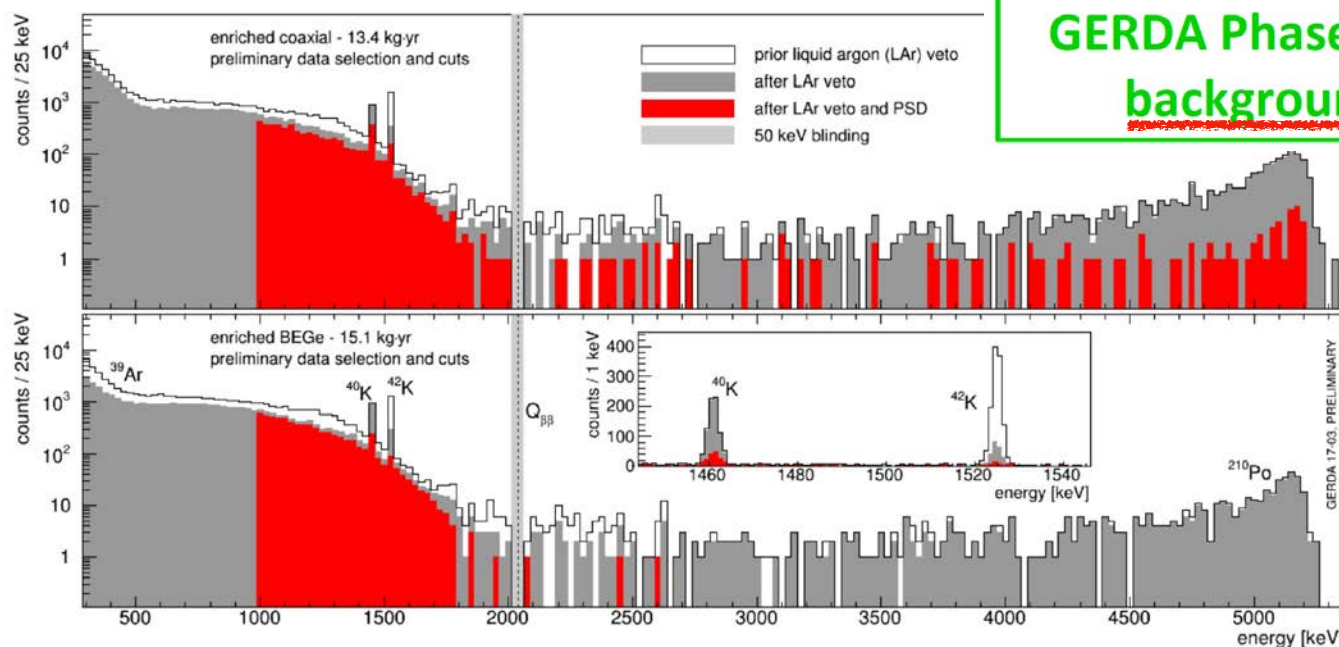
SuperNEMO  
démonstrateur ( $\geq 2016$ )





# $0\nu\beta\beta$ news - GERDA ( $^{76}\text{Ge}$ )

GERDA Phase II is the high-resolution and background-free  $0\nu\beta\beta$  experiment

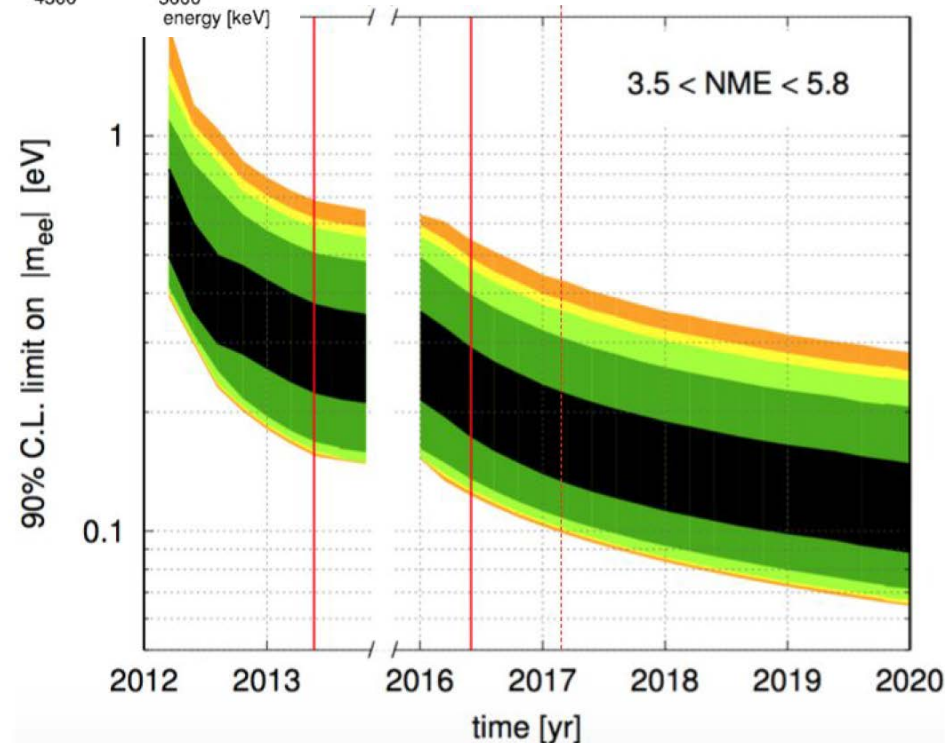


## Phase IIa achievements

background	$\sim 10^{-3}$ cts/(keV·kg·yr)
exposure	10.8 kg·yr
limit	$T_{1/2}^{0\nu} > 5.3 \cdot 10^{25}$ yr (90%CL)
	$m_{\beta\beta} < (0.15-0.33)$ eV (90%CL)

## Phase II goals

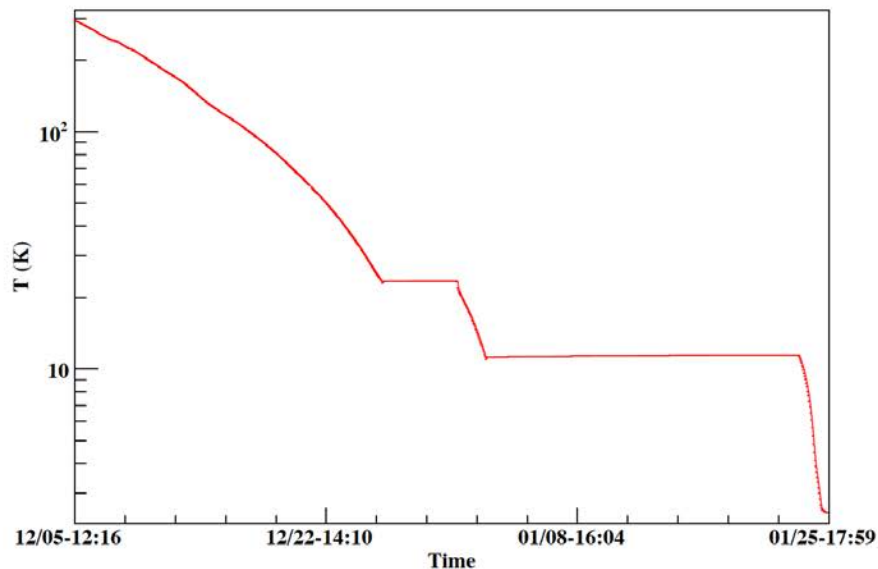
background	$\sim 10^{-3}$ cts/(keV·kg·yr) ✓
exposure	$\geq 100$ kg·yr
limit	$T_{1/2}^{0\nu} > 10^{26}$ yr



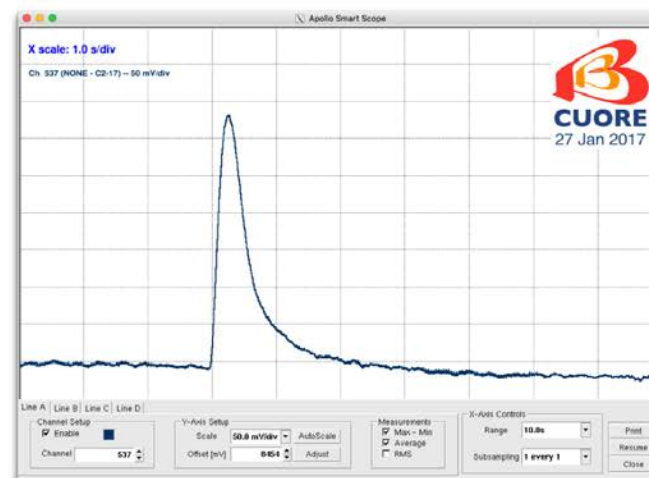
# $0\nu\beta\beta$ news - CUORE ( $^{130}\text{Te}$ )

CUORE is cold and running!

Diode thermometer at 10mK plate



Reached 8 mK: 26 Jan 2017



First pulse: 27 Jan 2017

## **Current status of CUORE:**

- End of commissioning and beginning of data-taking: April 2017
- Blind analysis currently in progress
- Expect first results within the next few months



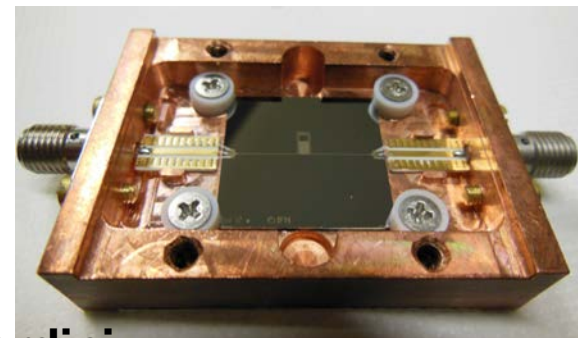
# 0νββ trailers - CUPIDs

## Problem: alpha background

Nucleus	I. A. [%]	Q-value [keV]	Materials successfully tested as bolometers in crystalline form ( <u>underlined compounds</u> : scintillators)
<sup>76</sup> Ge	7.8	2039	<u>Ge</u>
<sup>136</sup> Xe	8.9	2479	NONE
<sup>130</sup> Te	33.8	2527	<u>TeO<sub>2</sub></u> ← Cherenkov + scintillation TeO <sub>2</sub> is a very weak scintillator
<sup>116</sup> Cd	7.5	2802	<u>CdWO<sub>4</sub></u> , <u>CdMoO<sub>4</sub></u>
<sup>82</sup> Se	9.2	2995	<u>ZnSe</u> , <u>LiInSe<sub>2</sub></u>
<sup>100</sup> Mo	9.6	3034	<u>PbMoO<sub>4</sub></u> , <u>CaMoO<sub>4</sub></u> , <u>SrMoO<sub>4</sub></u> , <u>CdMoO<sub>4</sub></u> , <u>SrMoO<sub>4</sub></u> , <u>ZnMoO<sub>4</sub></u> , <u>Li<sub>2</sub>MoO<sub>4</sub></u> , <u>MgMoO<sub>4</sub></u>
<sup>96</sup> Zr	2.8	3350	<u>ZrO<sub>2</sub></u>
<sup>150</sup> Nd	5.6	3367	NONE → many attempts
<sup>48</sup> Ca	0.187	4270	<u>CaF<sub>2</sub></u> , <u>CaMoO<sub>4</sub></u>

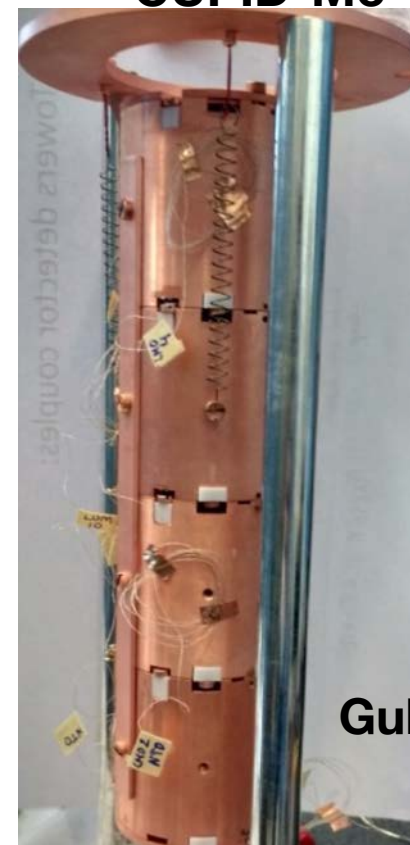
Nones

## Kinetic Inductance Detectors

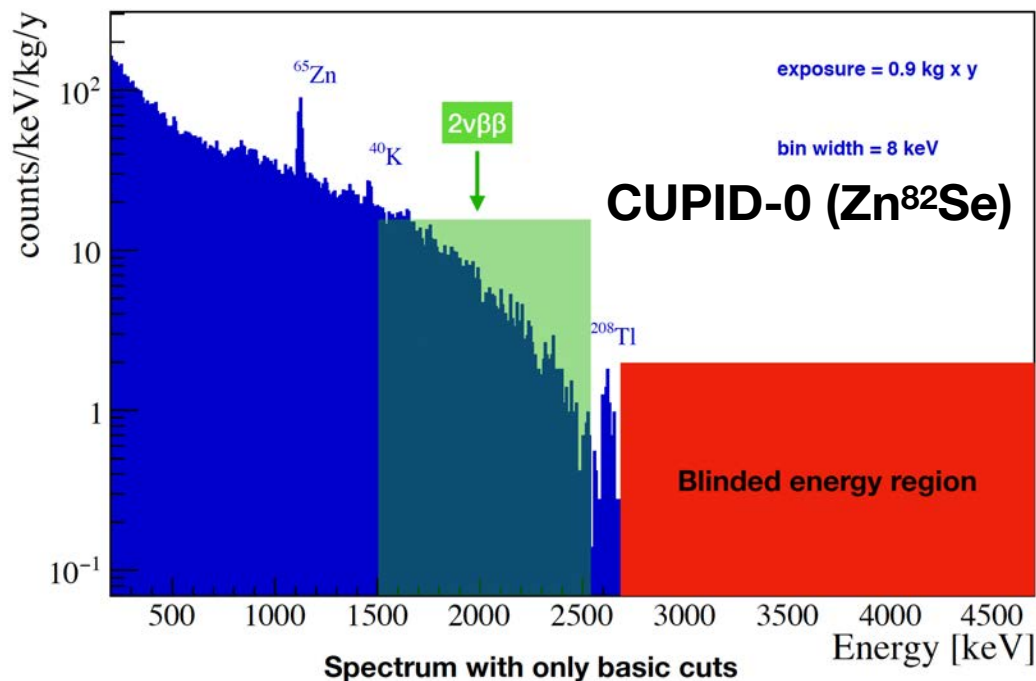


Cardini

## CUPID-Mo



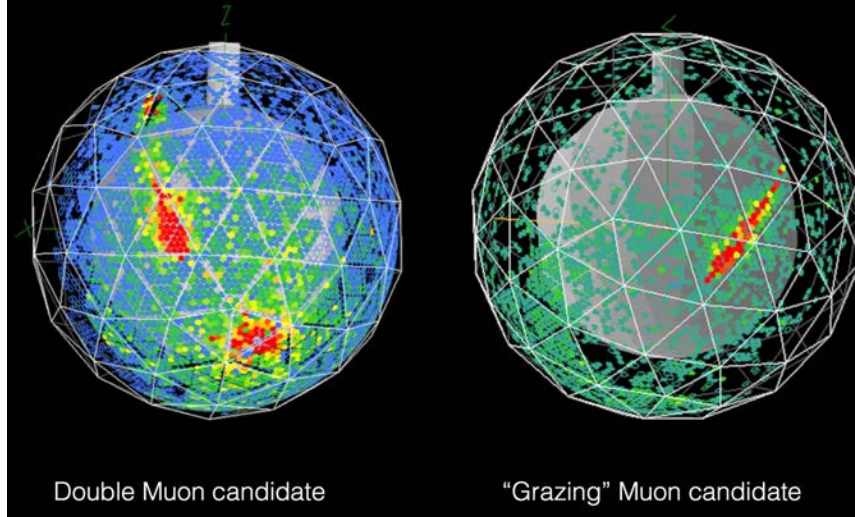
Guliani



# $0\nu\beta\beta$ trailers

**SNO+**

First water data



• **Loading method: Te acid + butanediol (TeBD)**

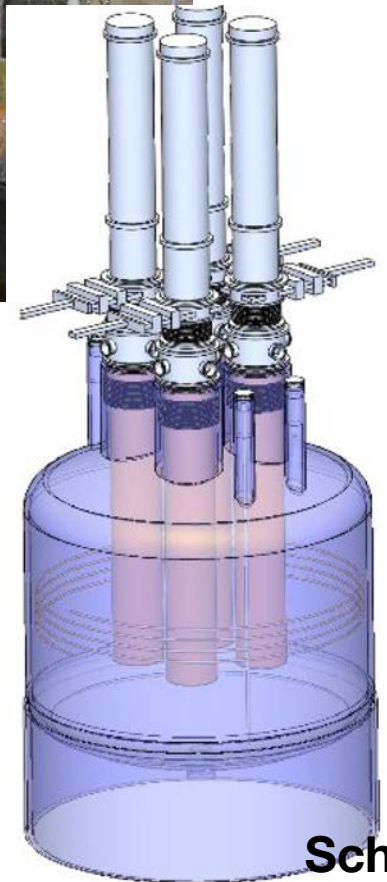
• Initially loading 0.5% (funding secured)

• ~1330 kg of  $^{130}\text{Te}$

**Barros**

↑  
"ton-scale"

**SuperNEMO**



# Mass sensitivity

