

3D Structure of the Nucleon, p_T 2

Transverse Momentum Distributions

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Physics 290E
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The big questions

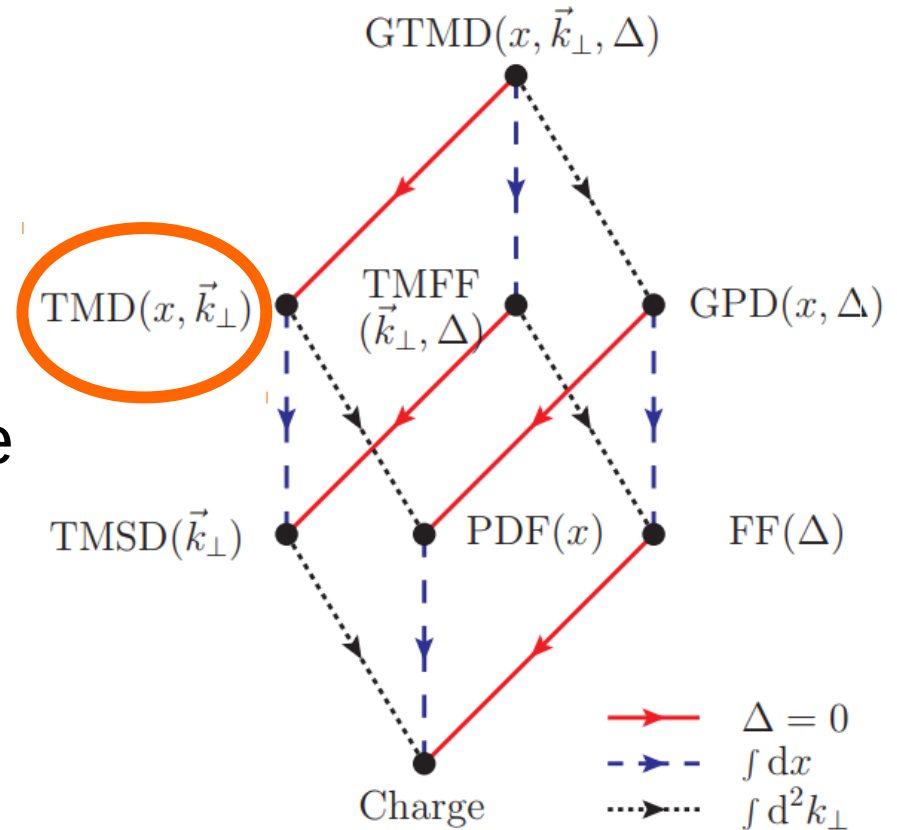
- What are TMDs?
- Why are they useful?
- How can they be measured?
- Status of existing measurements
- Prospects for future measurements

Background: Wigner distributions

- Holy grail: To measure/calculate the complete nucleon wavefunction $\psi(\mathbf{r}_g, \mathbf{r}_u, \mathbf{r}_{\bar{u}}, \mathbf{r}_d, \mathbf{r}_{\bar{d}}, \text{spins}, \dots)$
 - 3D (position or momentum), complex-valued
- ψ is mathematically equivalent to the Wigner “quasiprobability” distribution $W(\mathbf{r}_g, \mathbf{p}_g, \mathbf{r}_u, \mathbf{p}_u, \dots)$
 - 6D (position and momentum), real-valued
 - Not a true probability distribution (due to uncertainty principle), but similar in nature
- ψ/W encode *all* information on nucleon structure
- Unfortunately, we can’t measure them directly
 - Only lower-dimensional projections

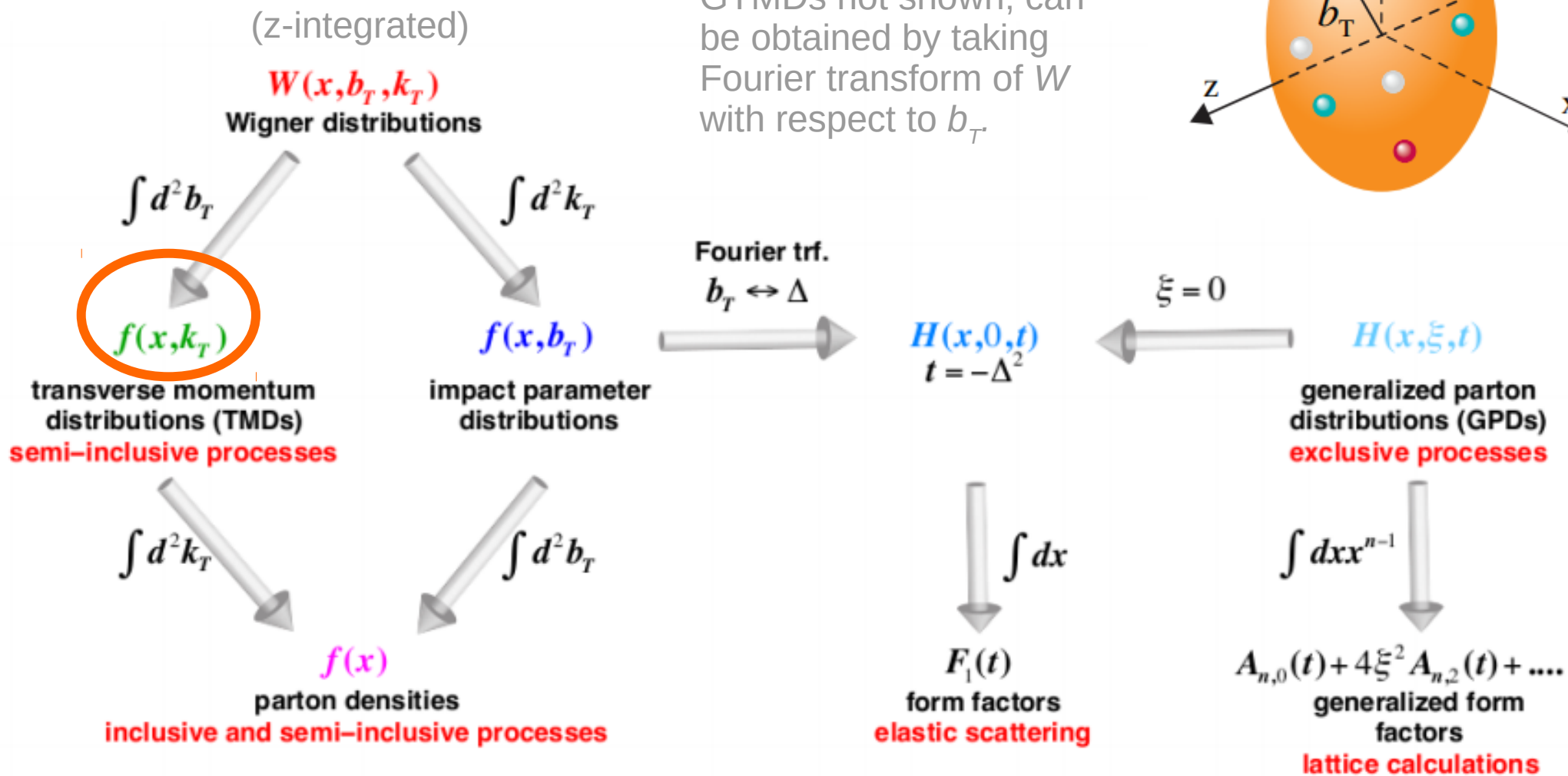
Nucleon structure “family tree”

- Integrate 6D W over longitudinal coordinate z to get 5D “GTMD”
 - Generalized TMD
 - Infinite-momentum frame: z is irrelevant
- Integrate GTMD over transverse coords, get 3D TMD
- Can further integrate TMD over transverse momenta to get familiar 1D PDF



For the pedantic: GTMD is actually Fourier transform of (z -integrated) W . Δ is “conjugate momenta” of transverse coordinates \mathbf{b}_T (*not the same as transverse momenta \mathbf{k}_T !*)

Family tree, again



Eight different TMDs

- Nucleon can be un-, longitudinally, or transversely polarized
- Likewise, our scattering process/measurement can be sensitive to different initial polarizations of the scattered parton
- Altogether, 8 TMDs per quark species, another 8 for gluons:

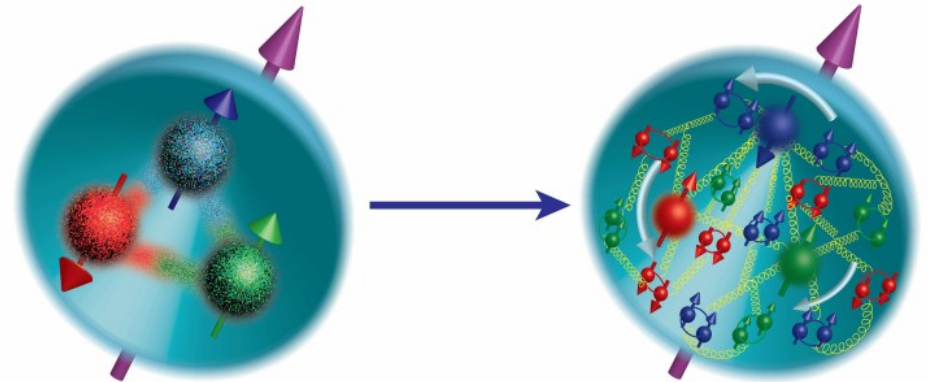
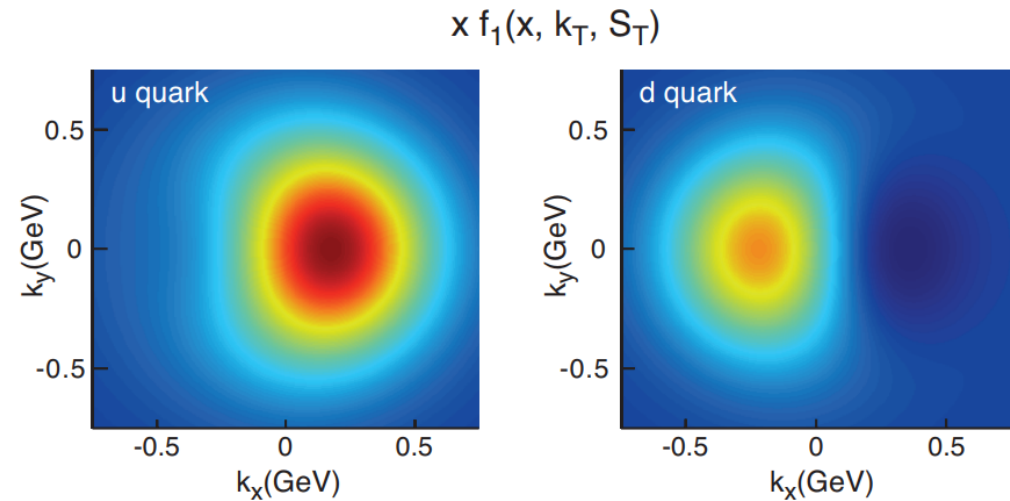
Leading Twist TMDs



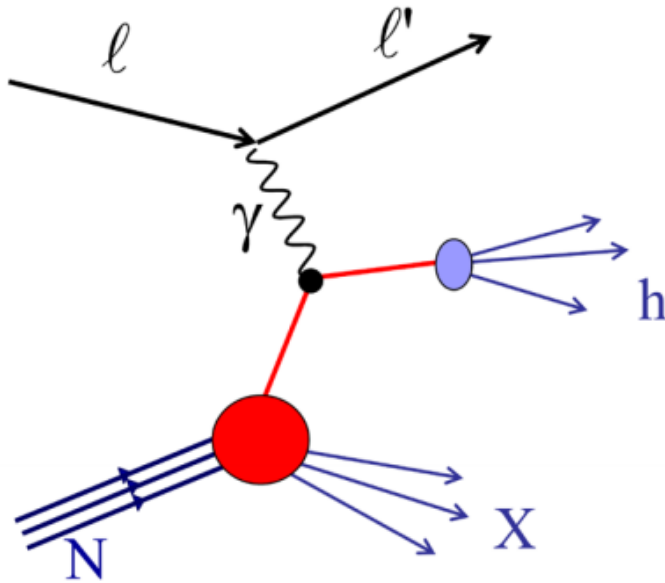
		Quark Polarization		
		Un-Polarized (U)	Longitudinally Polarized (L)	Transversely Polarized (T)
Nucleon Polarization	U	$f_1 =$		$h_1^\perp =$ — Boer-Mulders
	L		$g_{1L} =$ → — → Helicity	$h_{1L}^\perp =$ → — →
	T	$f_{1T}^\perp =$ — Sivers	$g_{1T}^\perp =$ — →	$h_1 =$ — Transversity $h_{1T}^\perp =$ — →

Why study TMDs?

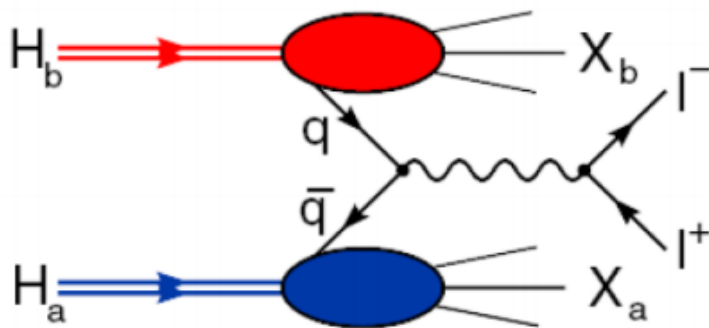
- Tomography: 3D imaging of nucleon in momentum space
 - Complimentary to GPDs: 3D in position space
- Orbital angular momentum's role in nucleon spin
 - k_T correlated w/ nucleon spin
- Correlation of parton spin with orbital ang. mom.
 - Contribution of sea quark, gluon polarization to nucleon spin
- Another handle on nucleon flavor structure



How to measure TMDs?



- Ordinary inclusive DIS won't work
 - Only measure outgoing lepton: not enough info
- Option 1: Semi-inclusive deep inelastic scattering (**SIDIS**)
 - Measure lepton + one outgoing hadron



- Option 2: Drell-Yan
 - E.g., $\pi p \rightarrow l+l-XX'$
- Need polarized beam/target to disentangle the 8 TMDs
- Today's focus is SIDIS

SIDIS kinematics

$$Q^2 = (k - k')^2 = 4E_e E_e' \sin^2 \left(\frac{\theta_e}{2} \right), \text{ Momentum transfer}$$

$$x = \frac{Q^2}{2M\nu}, \text{ quark momentum fraction}$$

$$\nu = \frac{P \cdot q}{M} = E_e - E_e', \text{ N rest frame } E_{loss}$$

$$y = \frac{P \cdot q}{P \cdot k} = \frac{\nu}{E_e}$$

$$W^2 = (P + q)^2 = M^2 + Q^2 \frac{1-x}{x}, \gamma^* N \text{ invariant mass}$$

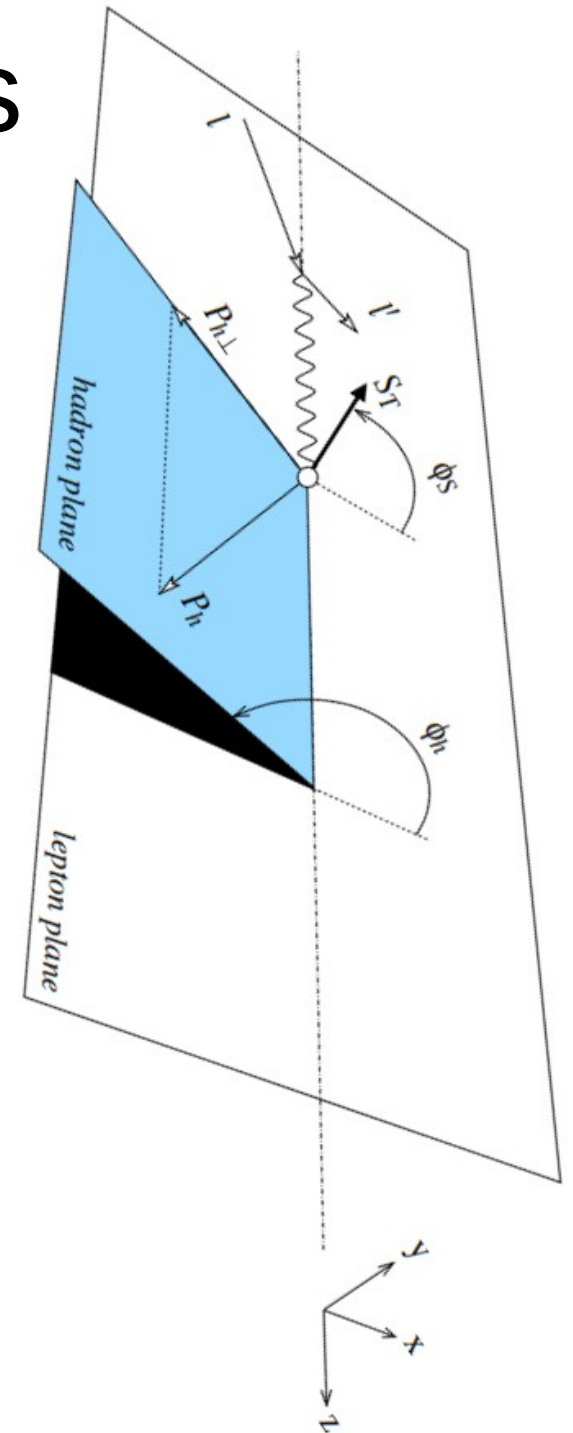
$$z = \frac{P \cdot P_h}{P \cdot q} = E_h / \nu, \text{ Hadron energy fraction}$$

$$p_T^h = \left| \mathbf{p}_h - \left(\frac{\mathbf{p}_h \cdot \mathbf{q}}{|\mathbf{q}|^2} \right) \mathbf{q} \right|, \text{ Hadron transverse momentum}$$

ϕ_h = Angle between lepton and hadron planes

ϕ_S = Angle between lepton plane and nucleon spin

$$W'^2 = M_X^2 = (P + q - P_h)^2, \text{ Missing mass}$$



SIDIS cross section

$$\frac{d\sigma}{dx dy d\psi dz d\phi_h dP_{h\perp}^2} =$$

$$\frac{\alpha^2}{xyQ^2} \frac{y^2}{2(1-\varepsilon)} \left(1 + \frac{\gamma^2}{2x}\right) \left\{ F_{UU,T} + \varepsilon F_{UU,L} + \sqrt{2\varepsilon(1+\varepsilon)} \cos\phi_h F_{UU}^{\cos\phi_h} \right. \quad \text{unpol target}$$

$$\left. + \varepsilon \cos(2\phi_h) F_{UU}^{\cos 2\phi_h} + \lambda_e \sqrt{2\varepsilon(1-\varepsilon)} \sin\phi_h F_{LU}^{\sin\phi_h} \right.$$

→ pol target

$$+ S_{\parallel} \left[\sqrt{2\varepsilon(1+\varepsilon)} \sin\phi_h F_{UL}^{\sin\phi_h} + \varepsilon \sin(2\phi_h) F_{UL}^{\sin 2\phi_h} \right] + S_{\parallel} \lambda_e \left[\sqrt{1-\varepsilon^2} F_{LL} + \sqrt{2\varepsilon(1-\varepsilon)} \cos\phi_h F_{LL}^{\cos\phi_h} \right]$$

$$+ |S_{\perp}| \left[\sin(\phi_h - \phi_S) \left(F_{UT,T}^{\sin(\phi_h - \phi_S)} + \varepsilon F_{UT,L}^{\sin(\phi_h - \phi_S)} \right) \right.$$

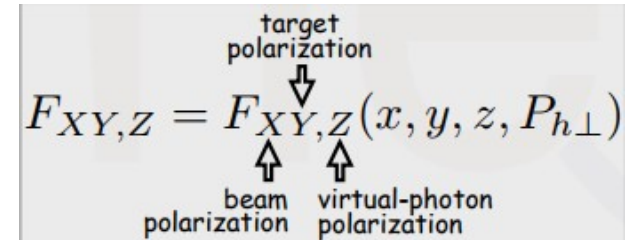
$$\left. + \varepsilon \sin(\phi_h + \phi_S) F_{UT}^{\sin(\phi_h + \phi_S)} + \varepsilon \sin(3\phi_h - \phi_S) F_{UT}^{\sin(3\phi_h - \phi_S)} \right.$$

$$\left. + \sqrt{2\varepsilon(1+\varepsilon)} \sin\phi_S F_{UT}^{\sin\phi_S} + \sqrt{2\varepsilon(1+\varepsilon)} \sin(2\phi_h - \phi_S) F_{UT}^{\sin(2\phi_h - \phi_S)} \right]$$

↑ pol target

$$+ |S_{\perp}| \lambda_e \left[\sqrt{1-\varepsilon^2} \cos(\phi_h - \phi_S) F_{LT}^{\cos(\phi_h - \phi_S)} + \sqrt{2\varepsilon(1-\varepsilon)} \cos\phi_S F_{LT}^{\cos\phi_S} \right.$$

$$\left. + \sqrt{2\varepsilon(1-\varepsilon)} \cos(2\phi_h - \phi_S) F_{LT}^{\cos(2\phi_h - \phi_S)} \right\},$$



18 structure functions

SIDIS cross section

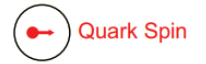
$$\begin{aligned}
 \frac{d\sigma}{dx dy d\psi dz d\phi_h dP_{h\perp}^2} = & \frac{\alpha^2}{xyQ^2} \frac{y^2}{2(1-\varepsilon)} \left(1 + \frac{\gamma^2}{2x}\right) \left\{ F_{UU,T} + \varepsilon F_{UU,L} + \sqrt{2\varepsilon(1+\varepsilon)} \cos\phi_h F_{UU}^{\cos\phi_h} \right. \\
 & + \varepsilon \cos(2\phi_h) F_{UU}^{\cos 2\phi_h} + \lambda_e \sqrt{2\varepsilon(1-\varepsilon)} \sin\phi_h F_{LU}^{\sin\phi_h} \\
 & + S_{\parallel} \left[\sqrt{2\varepsilon(1+\varepsilon)} \sin\phi_h F_{UL}^{\sin\phi_h} + \varepsilon \sin(2\phi_h) F_{UL}^{\sin 2\phi_h} \right] + S_{\parallel} \lambda_e \left[\sqrt{1-\varepsilon^2} \right. \\
 & + |S_{\perp}| \left[\sin(\phi_h - \phi_S) \left(F_{UT,T}^{\sin(\phi_h - \phi_S)} + \varepsilon F_{UT,L}^{\sin(\phi_h - \phi_S)} \right) \right. \\
 & + \varepsilon \sin(\phi_h + \phi_S) F_{UT}^{\sin(\phi_h + \phi_S)} + \varepsilon \sin(3\phi_h - \phi_S) F_{UT}^{\sin(3\phi_h - \phi_S)} \\
 & + \sqrt{2\varepsilon(1+\varepsilon)} \sin\phi_S F_{UT}^{\sin\phi_S} + \sqrt{2\varepsilon(1+\varepsilon)} \sin(2\phi_h - \phi_S) F_{UT}^{\sin(2\phi_h - \phi_S)} \left. \right] \\
 & + |S_{\perp}| \lambda_e \left[\sqrt{1-\varepsilon^2} \cos(\phi_h - \phi_S) F_{LT}^{\cos(\phi_h - \phi_S)} + \sqrt{2\varepsilon(1-\varepsilon)} \cos\phi_S F_{LT}^{\cos\phi_S} \right. \\
 & \left. \left. + \sqrt{2\varepsilon(1-\varepsilon)} \cos(2\phi_h - \phi_S) F_{LT}^{\cos(2\phi_h - \phi_S)} \right] \right\},
 \end{aligned}$$

14 independent azimuthal modulations

amplitudes of the modulations
→ TMD PDFs

SIDIS cross section

Leading Twist TMDs

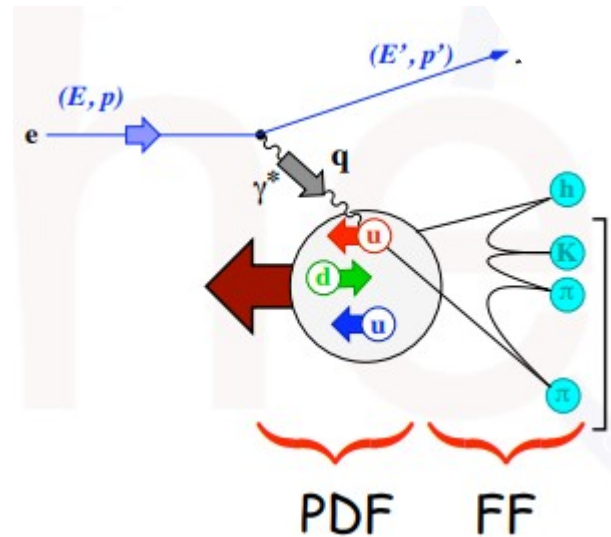


		Quark Polarization		
		Un-Polarized (U)	Longitudinally Polarized (L)	Transversely Polarized (T)
Nucleon Polarization	U	$f_1 = \odot$		$h_1^\perp = \uparrow - \downarrow$ Boer-Mulders
	L		$g_{1L} = \rightarrow - \leftarrow$ Helicity	$h_{1L}^\perp = \rightarrow - \leftarrow$
	T	$f_{1T}^\perp = \uparrow - \downarrow$ Sivers	$g_{1T}^\perp = \uparrow - \downarrow$	$h_1 = \uparrow - \downarrow$ Transversity $h_{1T}^\perp = \rightarrow - \leftarrow$

$$\begin{aligned}
 F_{UU,T} &\sim f_1 \otimes D_1 \\
 F_{UU}^{\cos 2\phi_h} &\sim h_1^\perp \otimes H_1^\perp \\
 F_{UL}^{\sin 2\phi_h} &\sim h_{1L}^\perp \otimes H_1^\perp \\
 F_{LL} &\sim g_1 \otimes D_1 \\
 F_{UT}^{\sin(\phi_h - \phi_S)} &\sim f_{1T}^\perp \otimes D_1 \\
 F_{UT}^{\sin(\phi_h + \phi_S)} &\sim h_1 \otimes H_1^\perp \\
 F_{UT}^{\sin(3\phi_h - \phi_S)} &\sim h_{1T}^\perp \otimes H_1^\perp \\
 F_{LT}^{\cos(\phi_h - \phi_S)} &\sim g_{1T} \otimes D_1
 \end{aligned}$$

$$F_{XY,Z} = F_{XY,Z}(x, y, z, P_{h\perp})$$

target polarization \downarrow
 beam polarization \uparrow virtual-photon polarization \uparrow



$$\begin{aligned}
 D_1(z, Q^2, p_\perp^2) &= \text{Unpolarized TMD FF} \\
 H_1^\perp(z, Q^2, p_\perp^2) &= \text{Collins TMD FF}
 \end{aligned}$$

TMD extraction

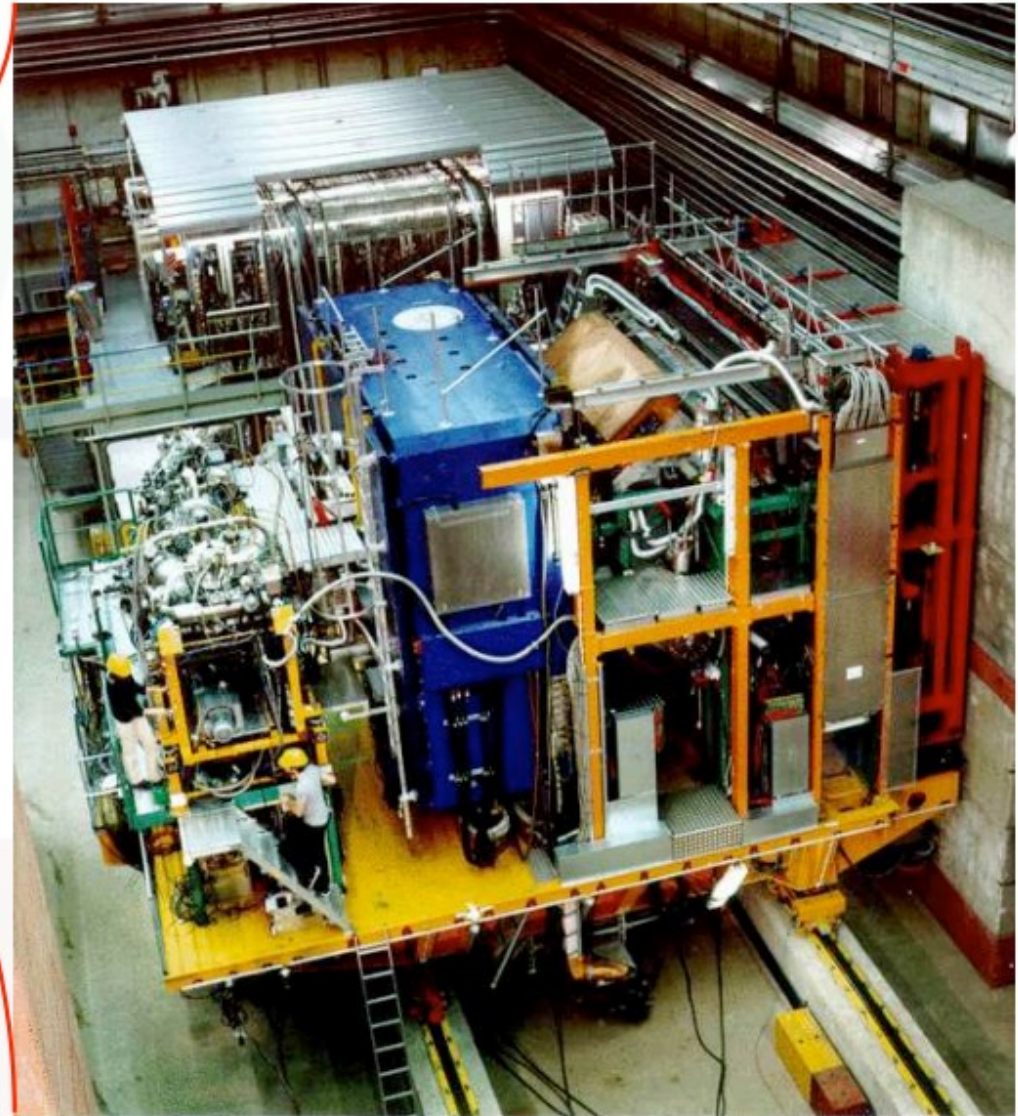
- For SIDIS, key is to measure azimuthal modulation
 - Angle between outgoing hadron \mathbf{p}_T and nucleon spin
- Different “harmonics” associated with different structure functions, e.g., $F_{UU}^{\cos(2\varphi)}$
- Each F is in turn a convolution of a TMD with a FF (previous slide)
- Take data at various energies and polarizations → disentangle and extract the TMDs
 - All 8 extractable with sufficient luminosity and kinematic reach (future electron-ion collider?)

Experimental landscape

- Modern (incomplete) TMD information from:
 - HERMES @ DESY (1995-2007)
 - COMPASS @ CERN-SPS (2002-present, SIDIS 2012)
 - 6GeV CEBAF @ Jlab (~2004 – 2012, all three halls)
- Under construction:
 - 12 GeV CEBAF
- The future: Electron-ion collider (all 8 TMDs!)
 - Either MEIC @ JLab or eRHIC @ BNL
 - Needed to extend to higher Q^2 , lower x → Probe sea quark and gluon TMDs

HERMES @ DESY

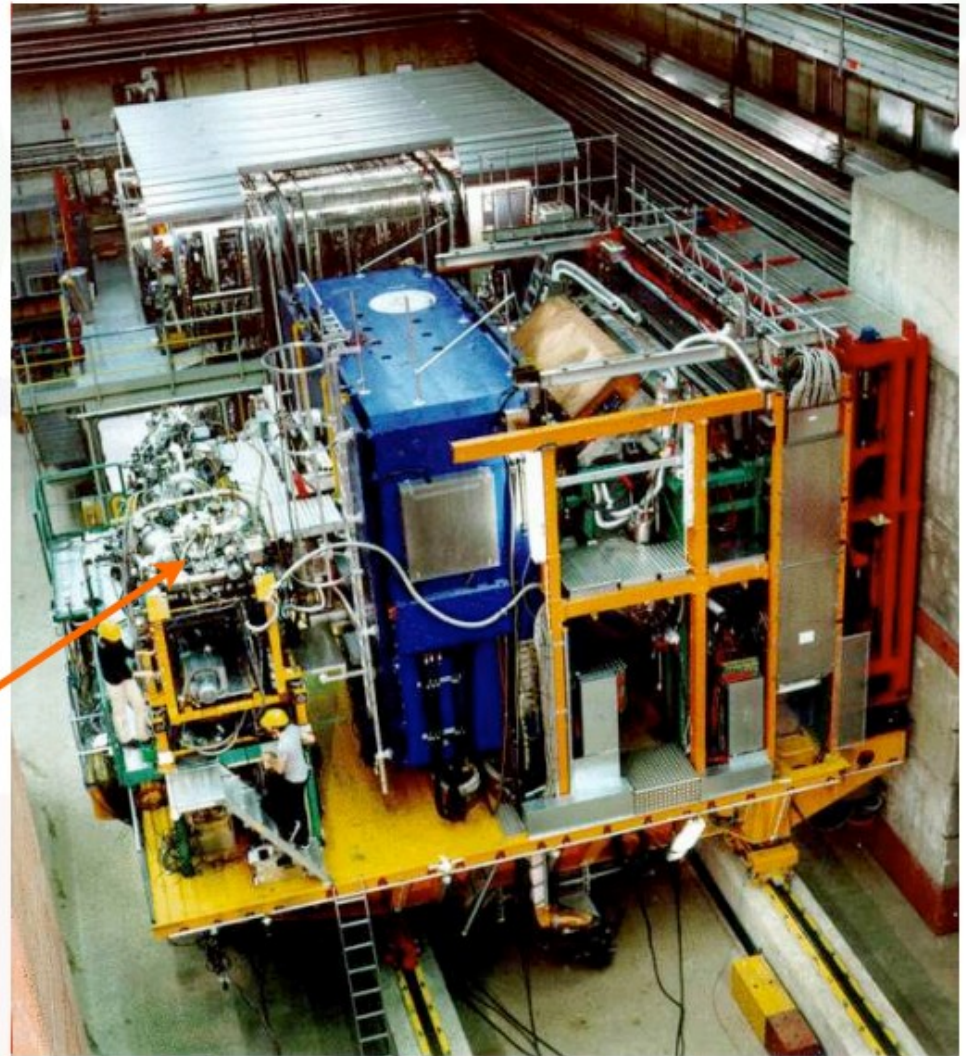
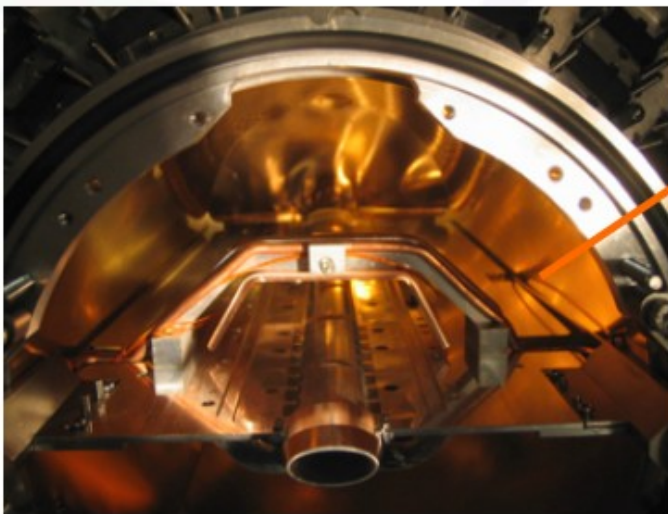
- 27.6 GeV HERA e^+/e^- beam



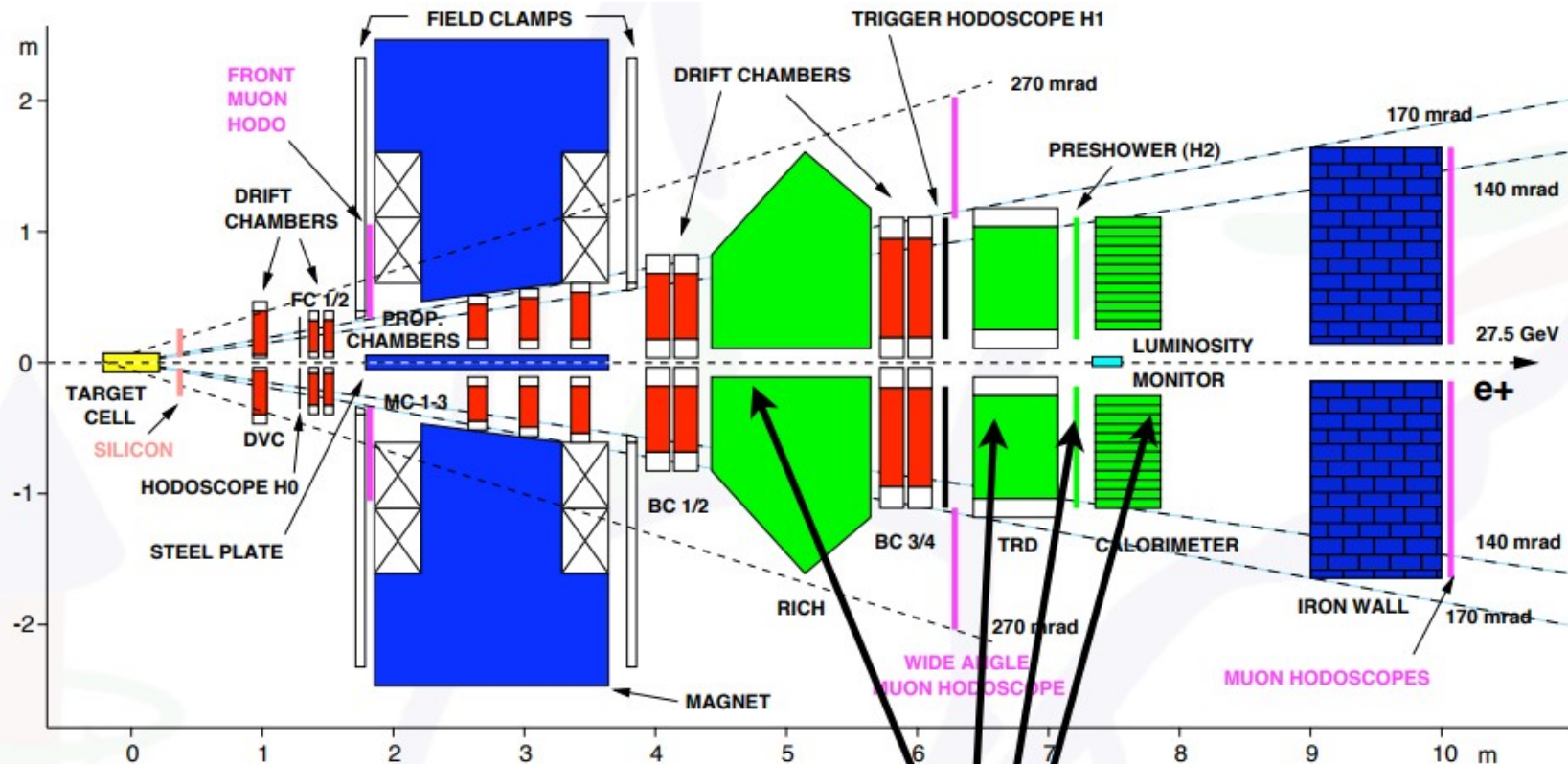
- longitudinally polarized

HERMES @ DESY

- pure gas targets
- internal to lepton ring
- unpolarized (^1H ... Xe)
- long. polarized: ^1H , ^2H , ^3He
- transversely polarized: ^1H



HERMES @ DESY



- pure gas targets internal to HERA 27.6 GeV lepton ring
- unpolarized (^1H ... Xe)
- long. polarized: ^1H , ^2H , ^3He
- transversely polarized: ^1H

Particle ID detectors allow for

- lepton/hadron separation
- RICH: pion/kaon/proton discrimination $2\text{GeV} < p < 15\text{GeV}$

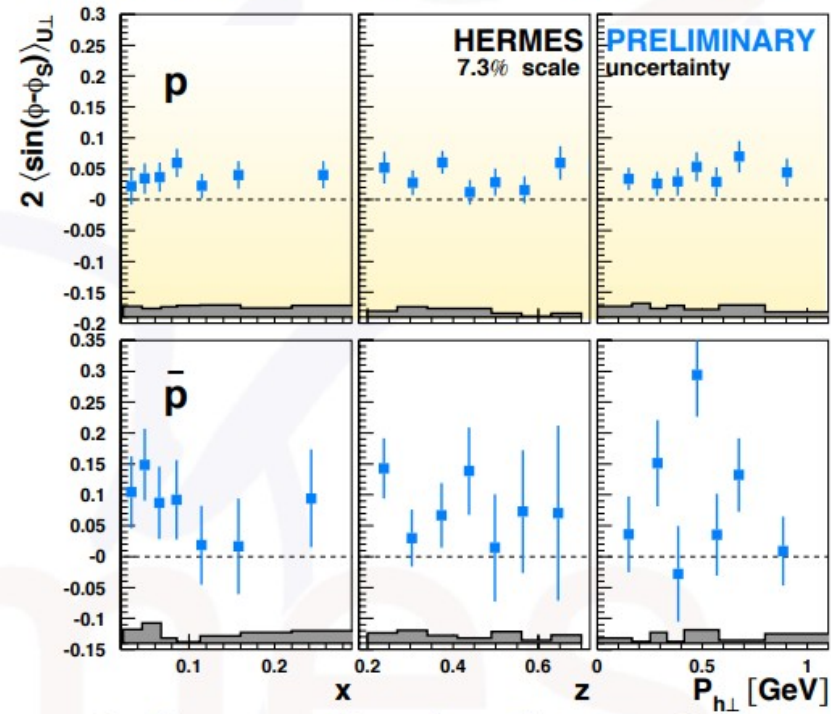
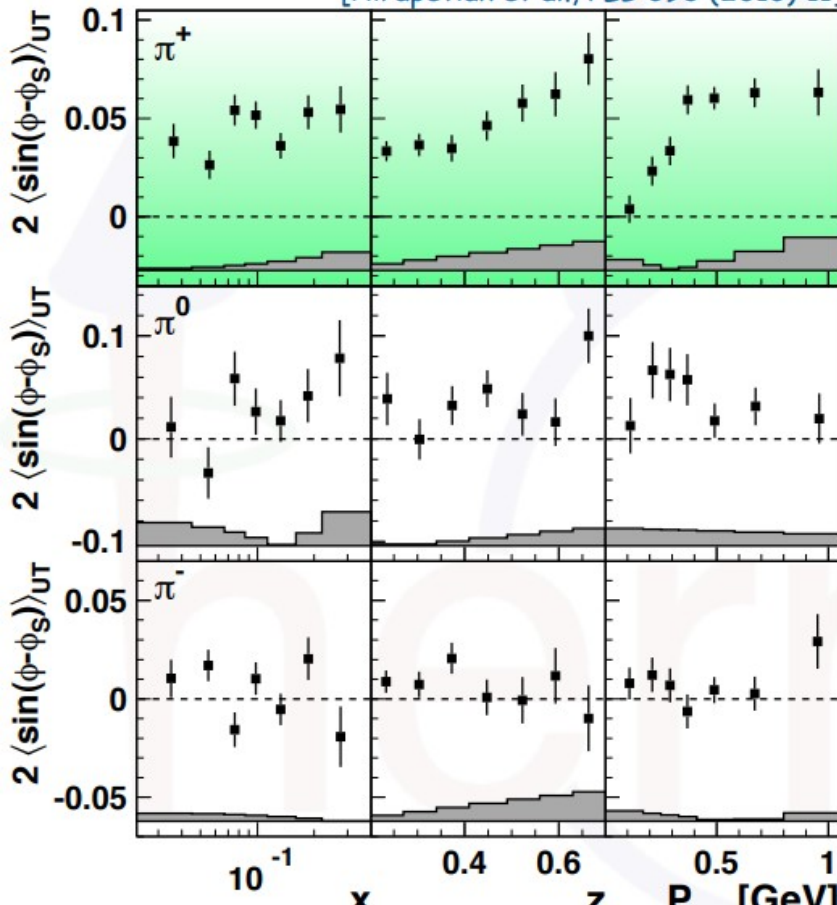
HERMES: Example data

	U	L	T
U	f_1		h_1^\perp
L		g_{1L}	h_{1L}^\perp
T	f_{1T}^\perp	g_{1T}	h_1, h_{1T}^\perp

Sivers amplitudes for baryons

$$2\langle \sin(\phi - \phi_S) \rangle_{UT} = - \frac{\sum_q e_q^2 f_{1T}^{\perp,q}(x, p_T^2) \otimes_W D_1^q(z, k_T^2)}{\sum_q e_q^2 f_1^q(x, p_T^2) \otimes D_1^q(z, k_T^2)}$$

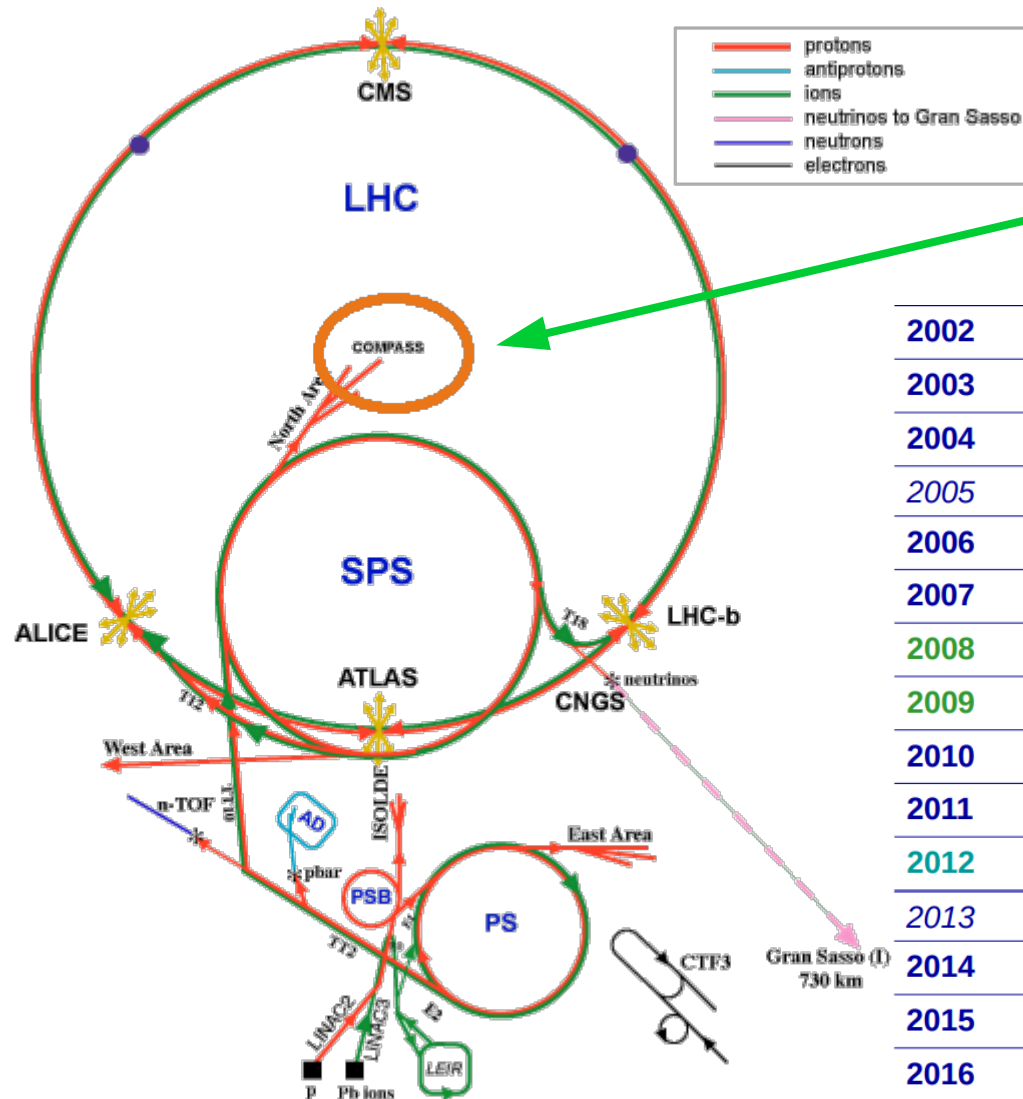
[Airapetian et al., PLB 693 (2010) 11]



similar amplitudes for positive pions and protons \rightarrow u-quark dominance (and not a FF effect)?

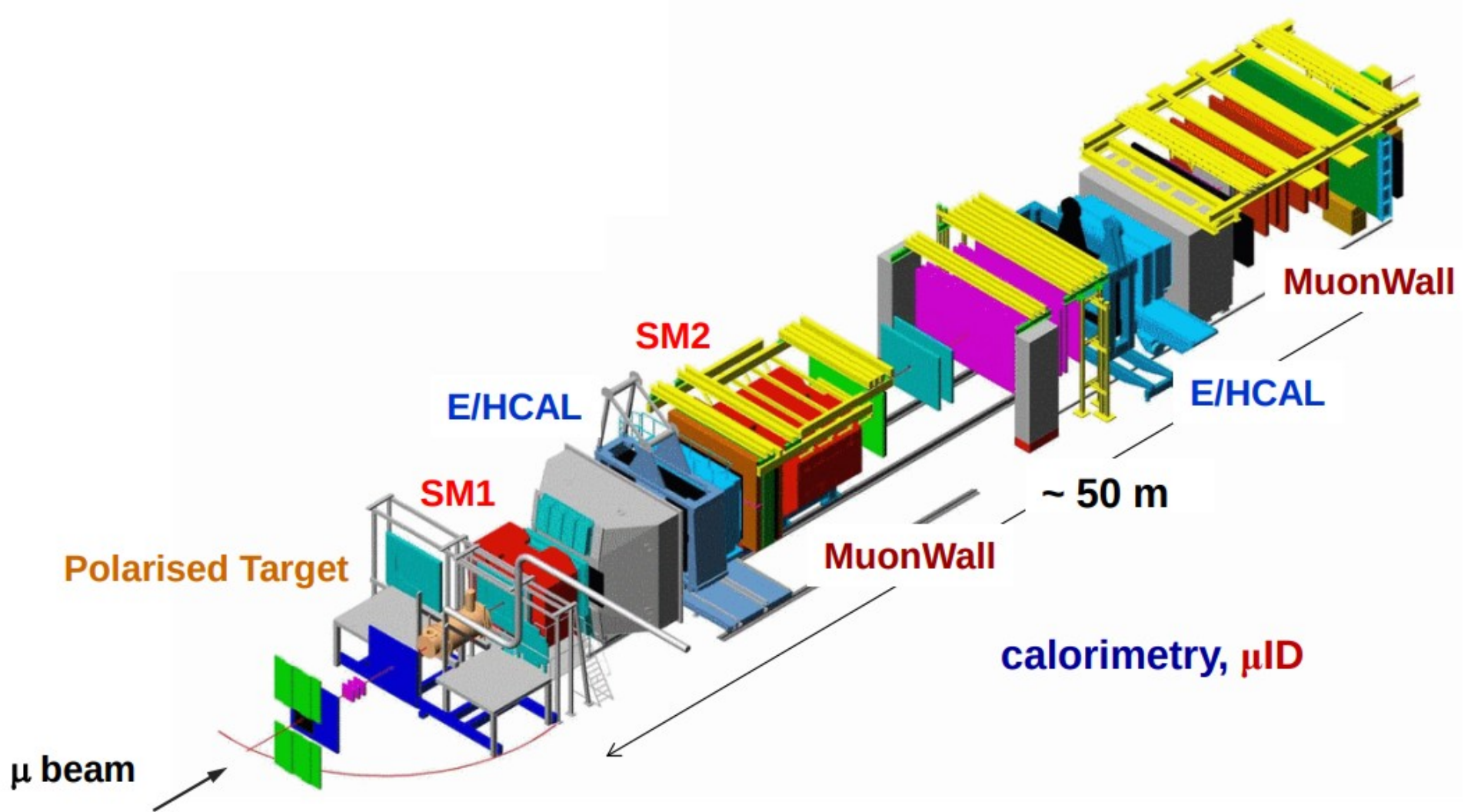
COMPASS @ CERN

Unpolarized muons/mesons on fixed target (proton or deuteron, possibly polarized)

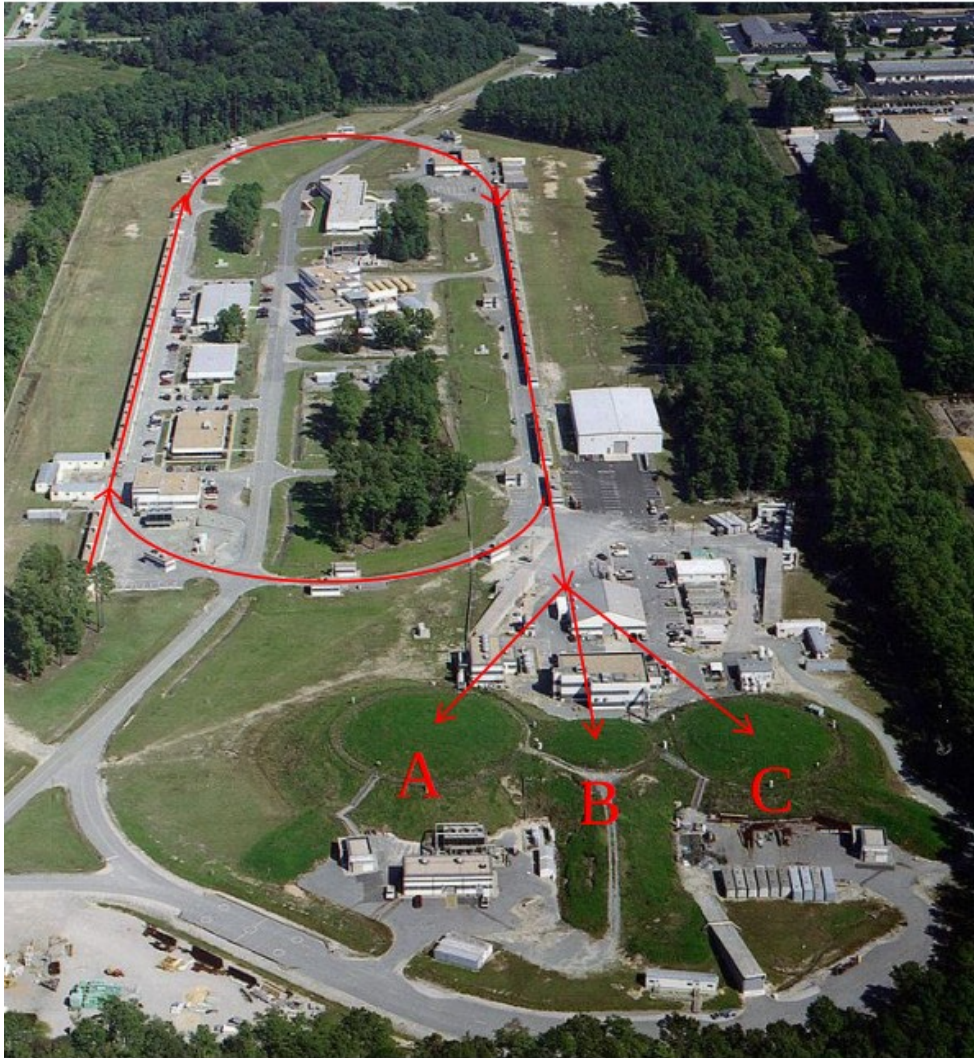


2002	nucleon structure with	160 GeV μ	L&T	polarised deuteron target
2003	nucleon structure with	160 GeV μ	L&T	polarised deuteron target
2004	nucleon structure with	160 GeV μ	L&T	polarised deuteron target
2005	CERN accelerators shut down			
2006	nucleon structure with	160 GeV μ	L	polarised deuteron target
2007	nucleon structure with	160 GeV μ	L&T	polarised proton target
2008	hadron spectroscopy			
2009	hadron spectroscopy			
2010	nucleon structure with	160 GeV μ	T	polarised proton target
2011	nucleon structure with	190 GeV μ	L	polarised proton target
2012	Primakoff & DVCS / SIDIS test			
2013	CERN accelerators shut down			
2014	Test beam Drell-Yan process with π beam and T polarised proton target			
2015	Drell-Yan process with π beam and T polarised proton target			
2016	DVCS / SIDIS with μ beam and unpolarised proton target			
2017	DVCS / SIDIS with μ beam and unpolarised proton target			
2018	Drell-Yan process with π beam and T polarised proton target			

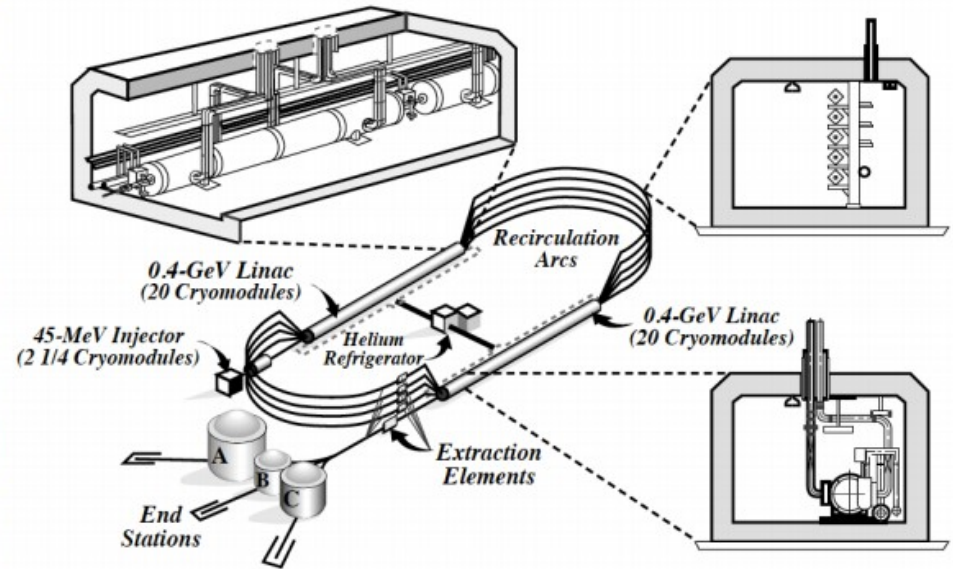
COMPASS @ CERN



CEBAF @ JLab



JLab Aerial View



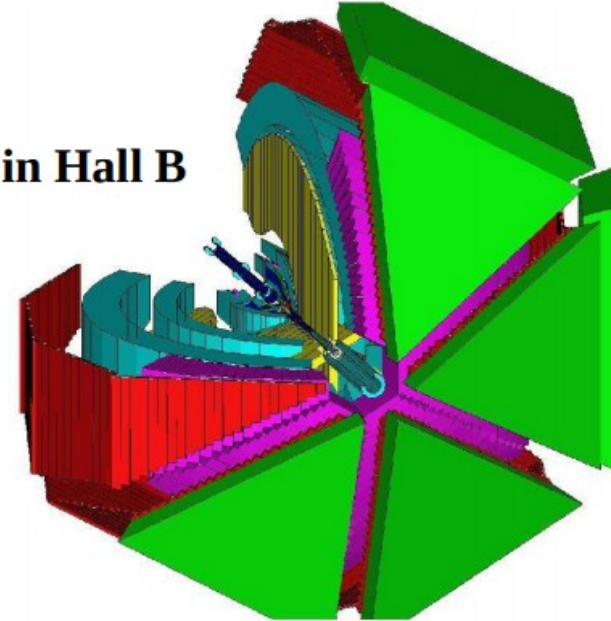
- Superconducting RF electron linacs with up to 5X recirculation
- CW (“100%” duty factor) operation (2 ns bunch period, ~0.3 ps bunch length)
- Polarized source: up to 85-90% polarization
- Three experimental Halls
- Energy up to 6 GeV (upgrade will increase to 11(12) GeV to Halls A/B/C (D))
- Current (up to 180 μA CW)

CEBAF @ JLab



Hall A: Two identical HRSs

CLAS in Hall B



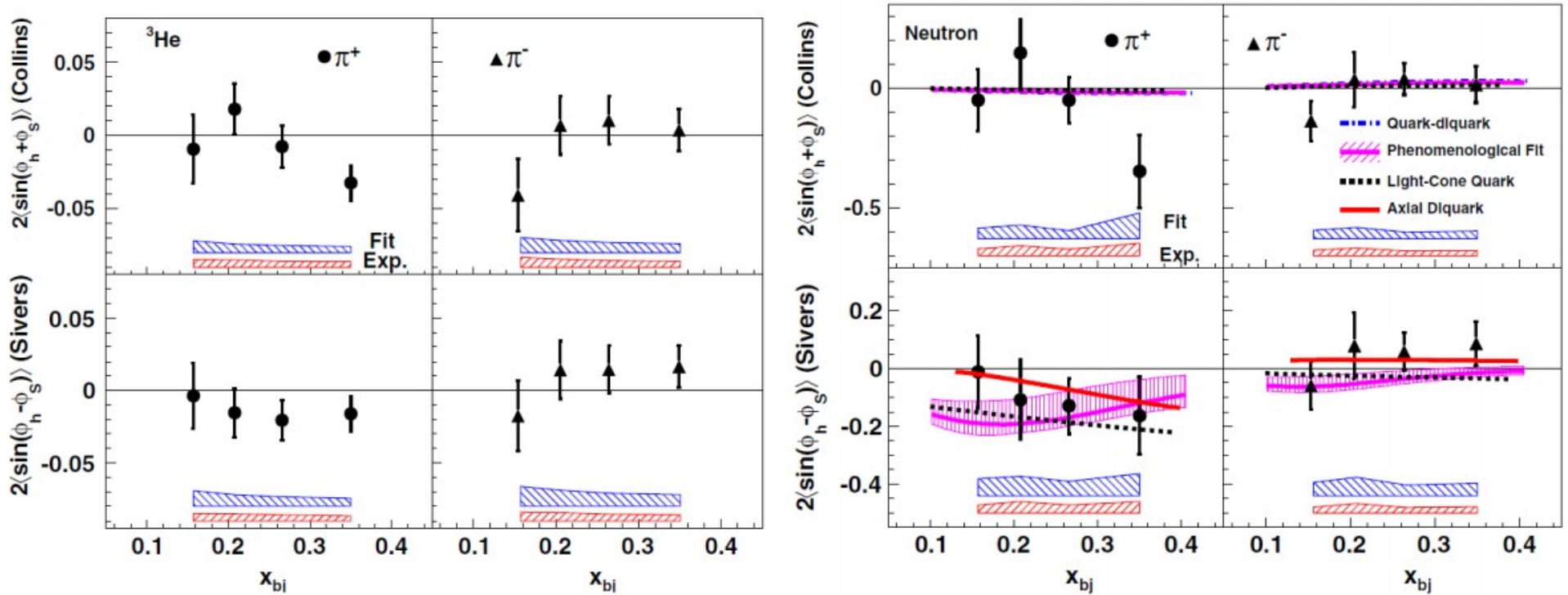
- **Hall A:** High resolution ($dp/p \sim 10^{-4}$) spectrometers, small acceptance for targeted measurements w/ well-controlled systematics, well-defined kinematics at high luminosities. *NIM A 522, 294 (2004)*
- **Hall B:** Large acceptance, moderate resolution/luminosity for measurement of multi-particle final states with broad kinematic coverage: *NIM A 503, 513 (2003)*
- **Hall C:** High momentum spectrometer and Short Orbit Spectrometer—well-controlled acceptance for precise cross section measurements: *PRC 78, 045202 (2008)*



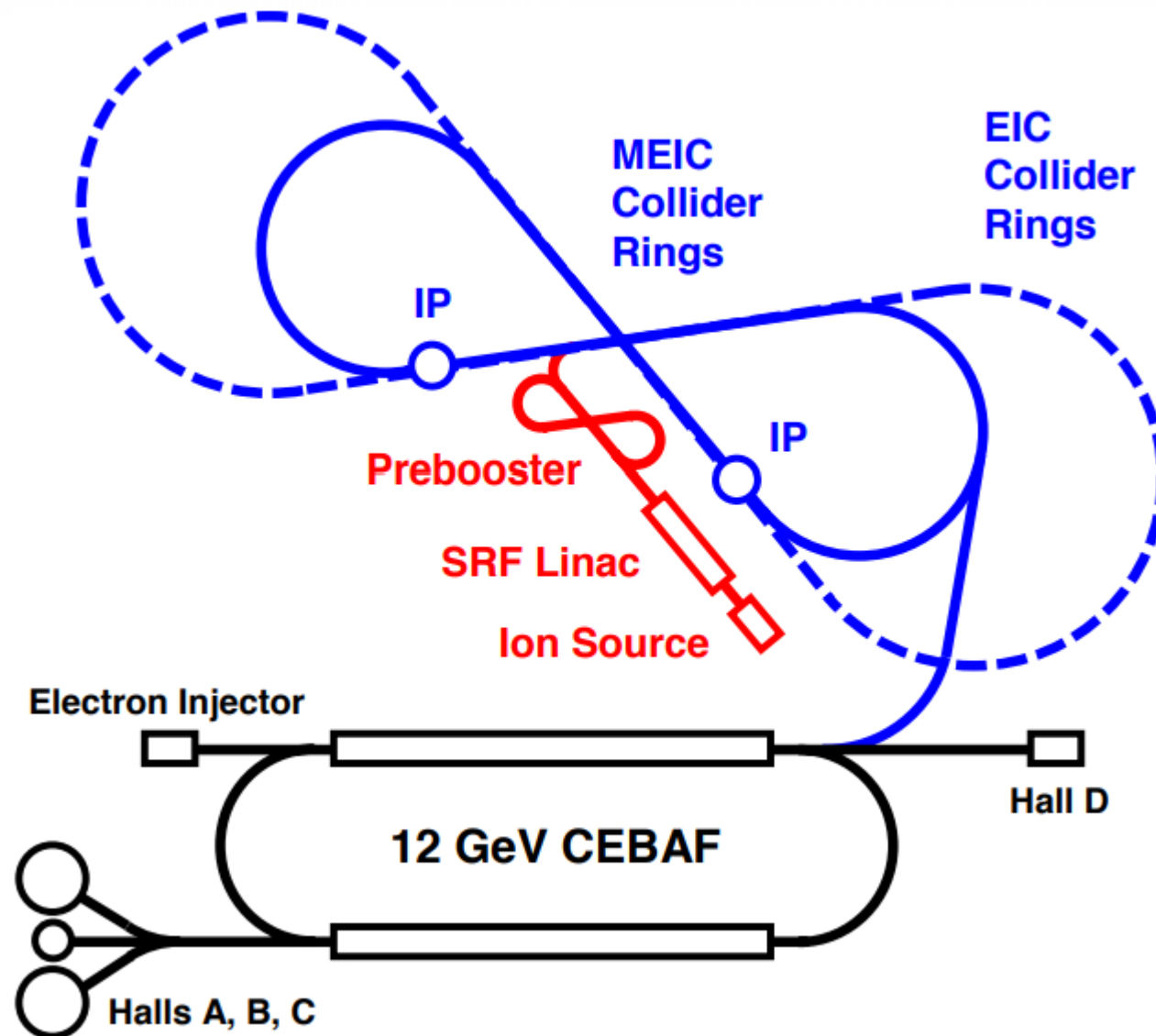
Hall C: HMS + SOS

CEBAF: Example data

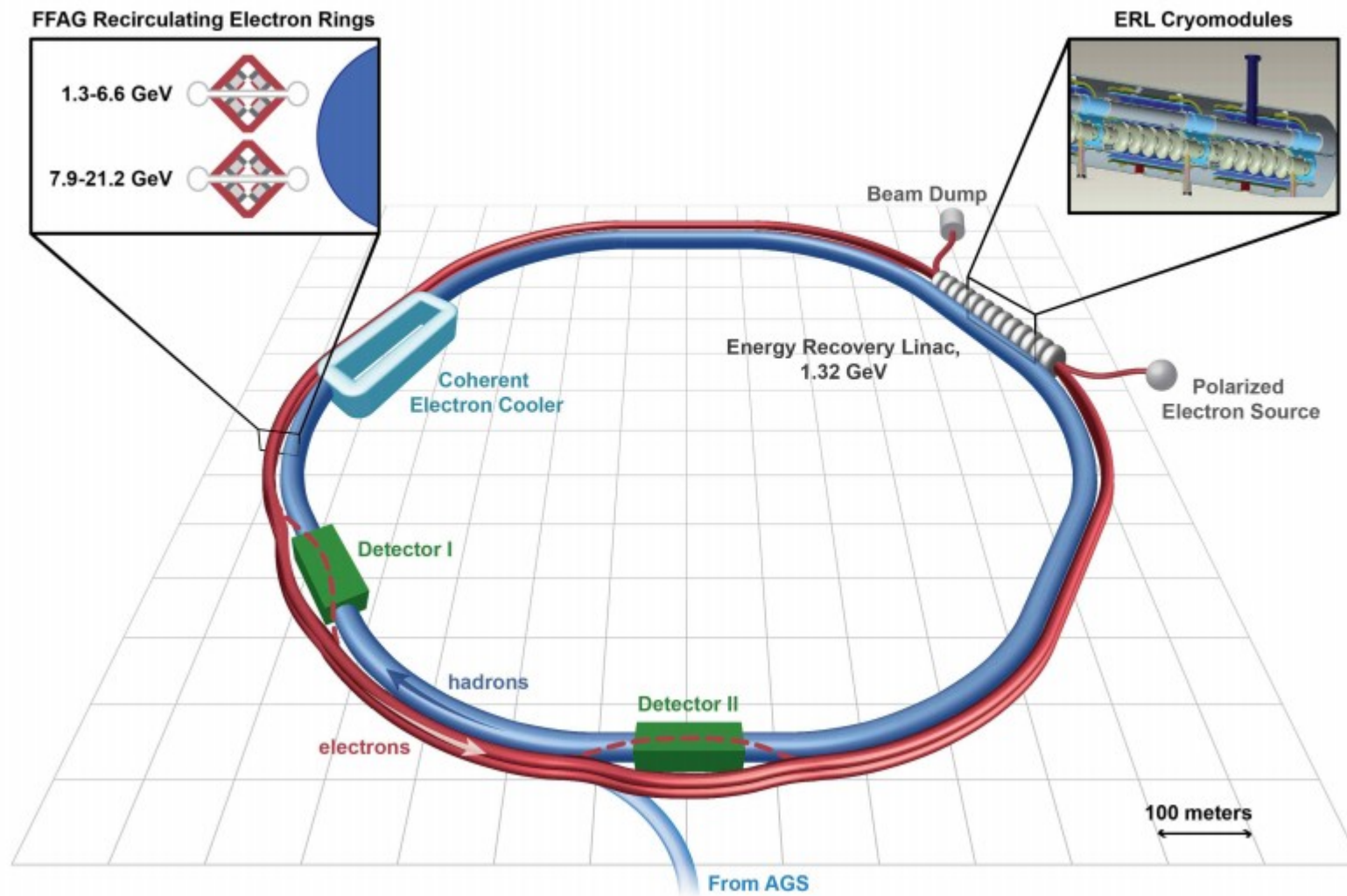
Collins and Sivers effects: *PRL 107, 072003 (2011)*



The future? MEIC @ JLab



The future? eRHIC @ BNL



Conclusions

- TMDs...
 - ...complement the 3D structure revealed by GPDs
 - ...provide unique insight into orbital angular momentum and spin-orbit coupling of partons
 - ...have been partially measured, but current fixed-target experiments are limited in reach
 - ...can be measured, at proposed EIC, to unprecedented precision, in all 8 forms, for all valence and sea quarks/gluons

References

- EIC whitepaper (very readable!): <https://arxiv.org/abs/1212.1701>
- HERMES:
<http://www-hermes.desy.de/notes/pub/TALK/gunar.3dpdfatlhc.pdf>
- COMPASS:
http://wwwcompass.cern.ch/compass/publications/talks/t2017/Bradamante_JLab2017.pdf
- CEBAF:
<https://www.jlab.org/conferences/qcd-evolution2015/talks/thursday/puckett.pdf>
- Theory (Alessandro Bacchetta):
 - Slides: https://www.jlab.org/div_dept/theory/talks/bacchetta08_eic.pdf
 - Notes:
https://www2.pv.infn.it/~bacchett/teaching/Bacchetta_Trento2012.pdf