We focus our attention to the Calorimeter, which we treat as a digital camera in cylindrical space.

Overview of M Learning for Partid

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US ATLAS ML **Training** July 26, 2023

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Particle Physics

Particle Physics + Machine Learning

Particle Physics + Machine Learning

5 Particle Physics + Machine Learning

One key challenge with images is that they have a fixed size.

In many contexts, this is ideal, because the data also have a fixed size. However, this is not always the case.

For example, events / jets have a variable number of particles.

One can represent these particles as a sequence in order to apply variable-length approaches that can access the full feature granularity.

Sequence learning with RNNs

Flavor tagging (classify jets from b-quark or not) has a long history of ML. Use features of the charged-particle tracks inside jets.

In the past, challenging to incorporate correlations between tracks.

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Plight

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 I Carried Sets anti-*k^t* **Sequences Fixed sets** *J* = *{pµ* \rightarrow *, pµ* γ *, ..., pµ* $\sum_{i=1}^{n}$ International Anti-Physics Previous work Previous wor $\sqrt{\frac{1}{\sqrt{2}}\left(\frac{3}{2}\right)}\left(\frac{3}{2}\right)$ Single \sum $\frac{1}{\sqrt{2}}$ \mathcal{L} $\overline{}$ 0.04 \mathbb{X} . \sim $\frac{1}{2}$ $\langle 0 \rangle_t$) (b) \mathcal{F} [Translated] \mathcal{F} 1 0.5 0 -0.5 -1 $\frac{1}{\sqrt{2}}$ **b b** [→] **1, 8** [→] **p p = 125 GeV 1,8 re-showered with Pythia 8, m** Normalized Pixel Energy \mathbf{r} -3 10 -1 10 1 1 0.5 0 -0.5 -1 [Translated] Azimuthal Angle (\overline{a} **b b** [→] **1** [→] **p p = 125 GeV** -8 10 -7 10 \mathbf{r} \mathbf{r} **Variable** / r
M -1 $\overline{}$ \setminus **b** $\frac{1}{2}$ **b** $\frac{1}{2}$ **b** $\frac{1}{2}$ **c ⁸ re-showered with Pythia 8, m** $\overline{}$ -1 10) (b) \mathcal{L} [Translated] \mathcal{L} [Translated] \mathcal{L} 1 0.5 0 -0.5 -1 $\frac{1}{2}$ **b** $\frac{1}{2}$ **¹ re-showered with Pythia 8, m** $\overline{}$ \mathbf{z} -2 10 1 0.5 0 -0.5 -1 $\overline{}$ -0.5 **sets Trees** Particle Strategy of the Contract of the Contr Personal Representation Event Representation Contract Property and ΦΦΦ人
人 \mathcal{L} Later Space Figure 1: A visualization of the decomposition of an observable via Eq. (1.1). Each particle in the event is mapped by to an internal (latent) particle representation, shown here as three abstract illustrations for a latent space of dimension three. The latent representation is $\begin{picture}(180,170) \put(0,0){\line(1,0){10}} \put(1,0){\line(1,0){10}} \put($ to the value of the observable. For the IRC-safe case of Eq. (1.2), takes in the angular $\left\langle \begin{array}{c} \end{array} \right\rangle$ competitive with existing techniques on key collider tasks, and provides a platform for visualizing the information learned by the model. Beyond this, we demonstrate how our framework unifies the existing event representations of calorimeter images and radiation moments, and we show the extraction of novel and One ever-present collider phenomenon that involves complicated multiparticle final states is the formation and observation of *jets*, sprays of color-neutral hadrons resulting from the fragmentation of high-energy quarks and gluons in quantum chromodynamics (QCD). Numerous individual observables have been proposed to study jets including the jets including multiplicity, image activity [66], the contraction of the contraction eralized angularities [71], (generalized) energy correlation functions [71], so ft drop multiplant and many more (see Refs. [51, 76] for reviews). Many more (see Refs. [51, 76] for reviews). Many more contract in the contract of the co have found to the transfer control to the transfer con vidual standard observables. Jet classification provides and case study for the Deep of th **Dense Networks Deep Sets Convolution Convolution Recursion NNS** Recursive NNs Graph CNNs **19** See 1709.04464 for image refs. Step 1: how to represent our data

A challenge with sequence learning is that thanks to quantum mechanics, there is often no unique order.

A common scenario is that we have a variable-length **SET** of particles and we would like to learn from them directly.

Solution: set learning / point cloud approaches

Factorize the problem into two networks: one that **embeds** the set into a fixed-length latent space and one that acts on a permutation invariant operation on that latent space:

$$
f(\{x_1, \ldots, x_M\}) = F\left(\sum_{i=1}^M \Phi(x_i)\right)
$$

Due to the sum, this structure can operate on any length set and the order of the inputs doesn't matter.

Factorize the problem into two networks: one that embeds

Solution 1: Deep sets **23**

Solution 1: Deep sets **24**

Latent space in IRC safe case is interpretable (and predictable!) *See also equivalent / covariant networks (e.g. 2203.06153)*

on input features to ∑ improve overall rn better $\frac{1}{2}$ Faster to train than RNN so can do R&D performance.

Latent space in IRC safe case is interpretable (and predictable!)

Classic CNNs operate on a fixed grid and are not invariant under the permutation of points

Can generalize CNNs to act on graphs

Need to define distances using particle properties

1801.07829 , 1902.08570

One way to categorize methods is based on their level of *supervision*

Unsupervised = no labels **Weakly-supervised** = noisy labels **Semi-supervised** = partial labels **Supervised** = full label information

This is 99% of the ML. We have labeled examples and we train a model to predict the labels from the examples.

Need to be careful about what loss function to pick (more on that in a little bit…)

Unsupervised = no labels

Typically, the goal of these methods is to implicitly or explicitly estimate p(x).

One strategy (autoencoders) is to try to compress events and then uncompress them. When x is far from

Talking point: anomaly detection!

Weakly-supervised = noisy labels

Typically, the goal of these methods is to estimate *p(possibly signal-enriched)/p(possibly signal-depleted)*

Semi-supervised = partial labels

Typically, these methods use some signal simulations to build signal sensitivity

How can we learn a classifier that does not sculpt a bump in the background?

How can we learn a classifier that does not sculpt a bump in the background?

**This is actually sufficient but unnecessary. There are many dependencies (e.g. linear) that would not sculpt bumps.*

Train e.g. a neural network

Train e.g. a neural network with a **custom loss functional**

 $\lambda \sum_{i \in b} L_{\text{decor}}(f(x_i), m_i)$ $\mathcal{L}[f(x)] = \sum_{i \in s} L_{\text{classification}}(f(x_i), 1)$ $+ \sum_{i \in b} L_{\text{classification}}(f(x_i), 0)$

> *Lclassifier* is the usual classifier loss, e.g. cross entropy or mean squared error.

37

Ldecor is large when *f(x)* and *m* are "correlated"

Recent proposals:

Adversaries: *Ldecor* is the loss of **a 2nd NN** (adversary) that tries to learn *m* from *f(x)*.

Distance Correlation: *Ldecor* is **distance correlation** (generalizes Pearson correlation) between *m* and *f(x).*

Mode Decorrelation: *Ldecor* is small when the **CDF** of *f(x)* is the same across different values of *m.*

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Enforcing Independence

Image credit: Denis Boigelot

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Adversaries: *Ldecor* is the loss of **a 2nd NN** (adversary) that tries to learn *m* from *f(x)*.

Pros: Very flexible and *m* can be multidimensional

Cons: Hard to train (minimax problem) & many parameters

Distance Correlation: L_{decor} is **distance correlation** (generalizes Pearson correlation) between *m* and *f(x).*

Pros: Convex (easier to train) and no free parameters

Cons: Memory intensive to compute distance correlation

Mode Decorrelation (MoDE): *L_{decor}* is small when the **CDF** of *f(x)* is the same across different values of *m.*

Pros: Cons: Readily generalizes beyond independence (can require linear, quadratic (+monotonic), … In its simplest form, need discrete bins in *m* (does not seem to be fundamental) No free parameters and small memory footprint

Overview **46**

Real world example: the search for Lorentzboosted *W* bosons at the Large Hadron Collider

MoDE[0] enforces independence, [1] is linear, [2] is monotonic quadratic, …

2010.09745

construction of the classifier sculpts a peak at the *classifier for upgestaintical* Case *N.B. think twice about using decorrelation for uncertainties! See 2109.08159.* Sometimes, we need a model (often for calibration) that does not depend on the training sample properties.

For example, a particle of a given energy hits our detector and registers measurements in a number of sensors

e.g. the particle energy is uniform during training, but exponential for certain running conditions.

(usually not an issue for classification)

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For example, a particle of a given energy hits our detector and registers measurements in a number of sensors

e. the particle energy is uniform during training,

Your first instinct here might have **b**. values using simulated data. *been to train a classifier to estimate the true value given measured values using simulated data.*

Claim: this is prior dependent !

For example, a particle of a given energy hits our detector and registers measurements in a number of sensors

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Suppose you have some features x and you want to predict y.

detector energy true energy

One way to do this is to find an f that minimizes the mean squared error (MSE):

$$
f = \operatorname{argmin}_g \sum_i (g(x_i) - y_i)^2
$$

Then*, $f(x) = E[y|x]$.

*If you have not seen this before, please let me know if you need help with the proof!

Suppose you have some features x and you want to predict y.

detector energy true energy

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$$
f(x) = E[y|x] = \int dy \, y \, p(y|x)
$$

 $E[f(x)|y] = \int dx dy' y' p_{\text{train}}(y'|x) p_{\text{test}}(x|y)$

this need not be y even if $p_{train} = p_{test}(!)$

2205.05084

2205.05084

Gaussian Example **64**

2205.05084

Gaussian Example: MLE instead!**55 Unbiased!** Average $(\mu, \sigma, \varepsilon) = (0, 1, 2)$ $\overline{4}$ Calibration Unbiased $\overline{2}$ $f(X)$ (calibrated) $\overline{2}$ Y (true) $\overline{0}$ $\overline{0}$ -2 $\overline{2}$ $(\mu, \sigma, \varepsilon) = (0, 1, 2)$ -4 $-4\frac{1}{2}$ -1 $\overline{2}$ 1 $\overline{2}$ $\overline{4}$ -4 -2 Ω Y (true) X (measured)

2205.05084, 2404.18992

Physics Example **1996 1997**

2205.05084; see also ATL-PHYS-PUB-2018-013 2205.05084
. FIG. 5. The *mjj* distributions for QCD (blue) and BSM (red) \mathcal{F} and \mathcal{F} are shaded histograms.

Particle Physics + Machine Learning

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Surrogate Models with ML **59**

Can we train a neural network to emulate the detector simulation?

Grayscale images: Pixel intensity = energy deposited

Introduction: generative models **60**

A **generator** is nothing other than a function that maps random numbers to structure.

Deep generative models: the map is a deep neural network.

Tools **⁶¹**

Deep generative models: the map is a deep neural network.

Introduction: GANs

Generative Adversarial Networks (GANs): *A two-network game where one maps noise to structure and one classifies images as fake or real.*

Introduction: VAEs

Variational Autoencoders (VAEs): *A pair of networks that embed the data into a latent space with a given prior and decode back to the data space.*

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Introduction: NFs **⁶⁴**

Normalizing Flows (NFs): *A series of invertible transformations mapping a known density into the data density.*

Optimize via maximum likelihood

latent space *Invertible transformations with tractable Jacobians*

Introduction: Score-based **⁶⁵**

Score-based *Learn the gradient of the density instead of the probability density itself.* ³

From 2206.11898

Calorimeter ML Surrogate Models **66** E stimation (KDE) E and sampling directly from the latent variables and sampling directly from the encoded eter MIL SUrrodate Models is mo the *Bu*↵*er-VAE* from Ref. [27].

therefore more accurate generative sampling from such a N(α) distribution; or (2) k

the already trained model but using a second density estimator — such as Kernel Density

FIG. 3. Comparison of the sum of all voxel energies (top) and number of hits (bottom) for datasets 1 (left), 2 (middle), and 3 See also <https://calochallenge.github.io/homepage/>and<https://calochallenge.github.io/homepage/>

CaloScore: VP CaloScore: subVP CaloScore: VE Geant4 2206.11898 \rightarrow + GFANT **GEANT GEANT** 10^{-5}

Many papers on this subject see the living [review](https://iml-wg.github.io/HEPML-LivingReview/) for all

Calorimeter ML Surrogate Models **⁶⁷**

Conditioning

Fix noise, scan latent variable corresponding to energy Fix noise scan latent variable corresponding to energy calorimeter.

Figure 2. Nearest GAN-generated neighbors (bottom) for seven random Geant4-generated

1711.08813

Fix noise, scan latent variable corresponding to x-position Fix Hoise, scall laterit variable corresportung to x-position

Our (ATLAS Collaboration) fast simulation (AF3) now includes a GAN at intermediate energies for pions

The GAN architecture is relatively simple, but it is able to match the energy scale and resolution well.

> There is one GAN per η slice

Integration into real detector sim. **⁷⁰**

Integration into real detector sim. **⁷¹**

The new fast simulation (**AF3**) significantly improves jet substructure with respect to the older one (**AF2**)

Ideally, the same calibrations derived for full sim. (Geant4-based) can be applied to the fast sim.

ATLAS Collaboration, 2109.02551

As expected, the fast sim. timing is independent of energy, while Geant4 requires more time for higher energy.
Common question: if we train on N events and sample M >> N events, do we have the statical power of M or N?

No free lunch - only win with **inductive bias**. Examples: factorization, symmetries, smoothness, …

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No free lunch - only win with **inductive bias**. Examples: factorization, symmetries, smoothness, ...

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Inverse Problems **76** Araa Drah **12**

Want this

perameters of the aenerative more (or the parameters of the generative model) **1** *Want this* **Measure this Measure this Measure this**

7

7

 \sim 1 iii \sim 1 iii 1 1 1 1 remove detector distortions (unfolding) or parameter estimation

 \mathcal{I}_1 , oddiad ad max 11 IV V 1 If you know *p(meas. | true)*, could do maximum likelihood, i.e.

7

77 ¹

7

1 1 1 *For parameter estimation, replace true with θ* If you know *p(meas. | true)*, could do maximum likelihood, i.e.

true unfolded = argmax p(measured | true)

Challenge: **measured** is hyperspectral and **true** is hypervariate … *p(meas. | true) is intractable !* **!**

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For parameter estimation, replace true with θ

If you know *p(meas. | true)*, could do maximum likelihood, i.e.

true unfolded = argmax p(measured | true)

Challenge: **measured** is hyperspectral and **true** is hypervariate … *p(meas. | true) is intractable !* **!**

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However: we have **simulators** that we can use to sample from *p(meas. | true)*

→ **Simulation-based** (**likelihood-free) inference**

For parameter estimation, replace true with θ

I'll briefly show you one solution to give you a sense of the power of likelihood-free inference.

Reweighting

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The solution will be built on *reweighting*

dataset 1: sampled from *p(x)* dataset 2: sampled from *q(x)*

Create weights *w(x) = q(x)/p(x)* so that when dataset 1 is weighted by *w*, it is statistically identical to dataset 2.

Reweighting

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dataset 1: sampled from *p(x)* dataset 2: sampled from *q(x)*

Create weights *w(x) = q(x)/p(x)* so that when dataset 1 is weighted by *w*, it is statistically identical to dataset 2.

What if we don't (and can't easily) know *q* and *p*?

Fact: Neutral networks learn to approximate the likelihood ratio = *q(x)/p(x)* (or something monotonically related to it in a known way)

> Solution: train a neural network to distinguish the two datasets!

This turns the problem of **density estimation** (**hard**) into a problem of **classification** (**easy**)

Proof of fact 84

$$
L[f] = \sum (f(x_i) - c)^2 \quad \text{Try yourself with BCE!}
$$
\n
$$
\approx \int dx \, p(x, c) \, (f(x) - c)^2
$$

δL[*f*, *f*′] *δf* = ∂*L* [∂]*^f* [−] *^d dx* ∂*L* ∂*f*′ Euler-Lagrange *Equation*

Proof of fact **85**

$$
L[f] = \sum (f(x_i) - c)^2
$$
 Try yourself with BCE!
\n
$$
\approx \int dx p(x, c) (f(x) - c)^2
$$
\n
$$
\frac{\delta L[f, f']}{\delta f} = \frac{\partial L}{\partial f} - \frac{\delta L}{\delta x} \frac{\delta L}{\delta f} = 0
$$
 Euler-Lagrange Equation

Basically just a regular derivative: $\int dc \, p(x, c)(f(x) - c) = 0 \implies f(x) = E[c \, | \, x]$

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Here, instead of emulating $p(x | \theta)$ directly, we learn $\frac{p(x | \theta)}{p(x | \theta)}$ $p(x | \theta_0)$

(turns the problem of generation into classifi

Example **88**

Here, instead of emulating $p(x | \theta)$ directly, we learn $\frac{p(x | \theta)}{p(x | \theta)}$ $p(x | \theta_0)$

(turns the problem of generation into classifi

Benefit: easy to integrate complex data structure (symmetries, etc.)

Downside: large weights when θ is far from θ_0

Classification for reweighting **1999**

Reweight the **full phase space** and then pin
as
ne check for various binned 1D-observables-

0*.*04

Æ*^s* = 0*.*1365

Æ*^s* = 0*.*1600

Æ*^s* = 0*.*1600 wgt.

Jets per bin (normalized)

Achieving precision **190**

Works also when the differences between the two simulations are **small** (left) or **localized** (right).

These are histogram ratios for a series of one-dimensional observables

Parameterized reweighting

2021 0*.*02 tii
--

What if we have a new simulation with

 ~ 1 $\frac{1}{2}$ ~ 0 multiple 0*.*4 0*.*5 0*.*6 0*.*7 0*.*8 0*.*9 multiple continuous parameters θ?

1
1
1

Jets per bin (normalized)

Example Fit Example Fit

Step 1: Differentiable Surrogate Model

$$
f(x,\theta) = \underset{f'}{\operatorname{argmax}} \sum_{i \in \theta_0} \log f'(x_i, \theta) + \sum_{i \in \theta} \log(1 - f'(x_i, \theta))
$$

network *f* is trained as described above. Such a function

Example Fit to the values that minimizes the nominal class*f*(*x,* ✓) = argmax Example Fit

will satisfy the control of the control of

sifier loss. In particular, suppose that a reweighter neural, supported that a reweighter neural control and t
In particular, supported that a reweighter neural control and the second control and the second control and th network *f* is trained as described above. Such a function (*xi,* ✓) +^X *i*2✓ log(1 *f*⁰ (*xi,* ✓))

Step 1: Differentiable Surrogate Model

*i*2✓⁰

$$
f(x,\theta) = \underset{f'}{\operatorname{argmax}} \sum_{i \in \theta_0} \log f'(x_i, \theta) + \sum_{i \in \theta} \log(1 - f'(x_i, \theta))
$$

where \tilde{U}_1 is unknown (for instance, \tilde{U}_1 are collider data). The collider data \tilde{U}_2

gant way of implementing this approach is to fit unknown the this approach is to fit unknown the \mathcal{L}

log *f*⁰

for all in the *formulation* stars and σ for σ in the first sum takes the first sum takes the first sum takes the first sum takes the σ Step 2: Gradient-based optimization

$$
\theta^* = \underset{\theta'}{\operatorname{argmax}} \sum_{i \in \theta_0} \log f(x_i, \theta') + \sum_{i \in \theta_1} \log(1 - f(x_i, \theta'))
$$

93

(2)

(3)

Example Fit

BlindedTimeShower:alphaSvalue 0.1700 ⁰*.*¹⁷⁰⁷ *[±]* ⁰*.*⁰⁰²²

StringFlav:probStoUD 0.1400 0*.*1422 *±* 0*.*0065

94

2203.16722

2203.16722

 $0.1, \ldots$ 10 events are sampled from the density for each event in 'data'. There are corresponding α

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Jet Image

Conclusions and Outl

AI/ML has a great potential to **enhance**, **accelerate**, and **empower** all areas of HEP

There are applications now that were unthinkable before ML and new ideas are incoming!

We need you to help develop, adapt, and deploy new methods

I've provided some specific examples today, but see the Living Review, 2102.02770, for more!

Γ 0.08 1 b
d
a
D
te Note that I could not cover everything! e.g. anomaly detection

Fin.