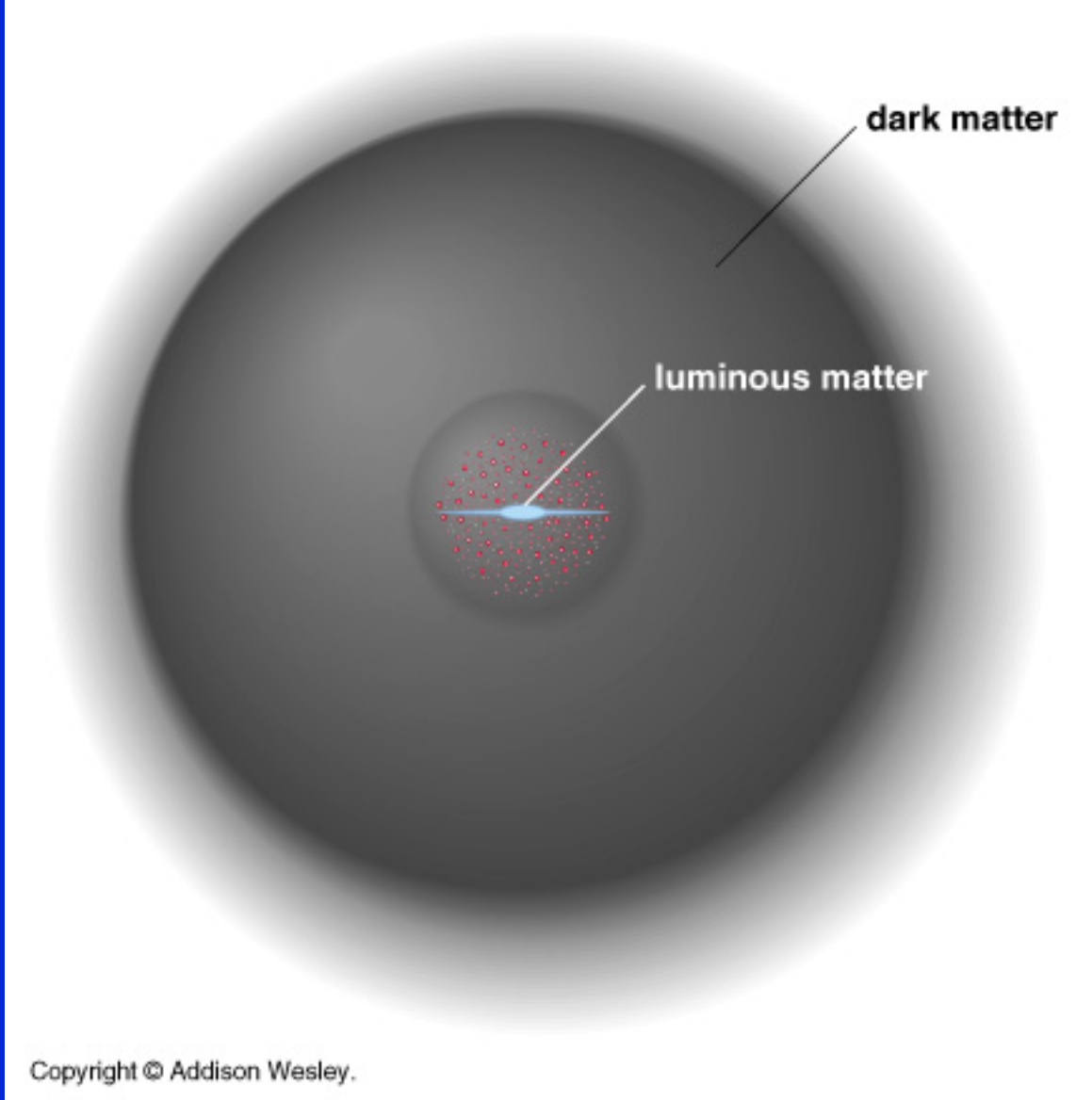


Dark matter: astrophysical evidence

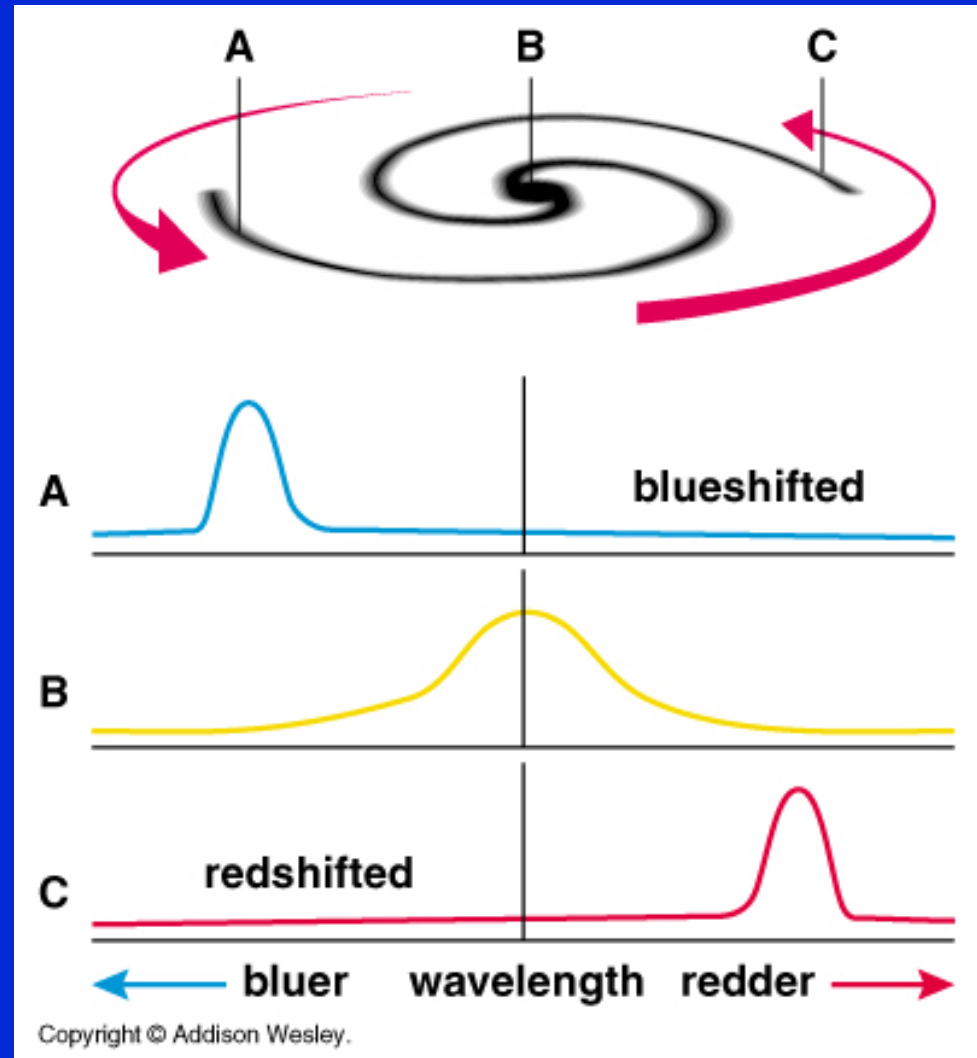
Uros Seljak

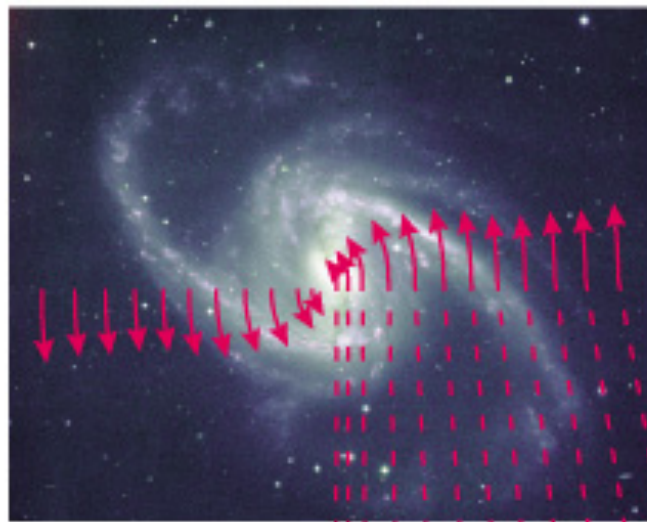
dark matter: do we need it?

- motions of stars/gas within galaxies show that there is 'dark matter' *within galaxies*
- motions of galaxies within groups and clusters show that there is dark matter *between galaxies* as well
- *gravitational lensing* also provides a different sort of evidence for the existence of dark matter
- CMB+BAO: best constraints

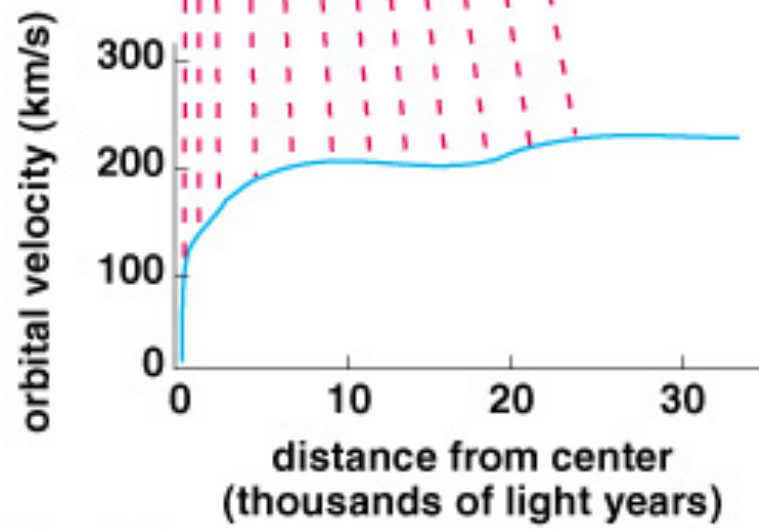


Evidence for dark matter in galaxies



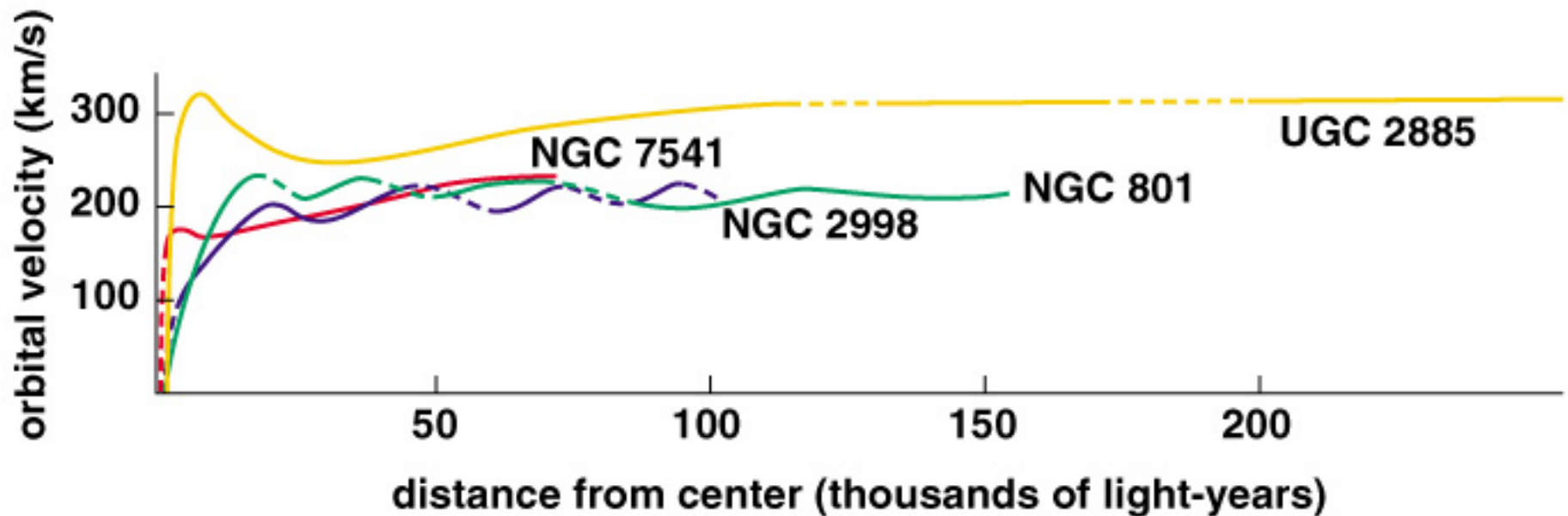


Longer arrows represent larger orbital velocities.

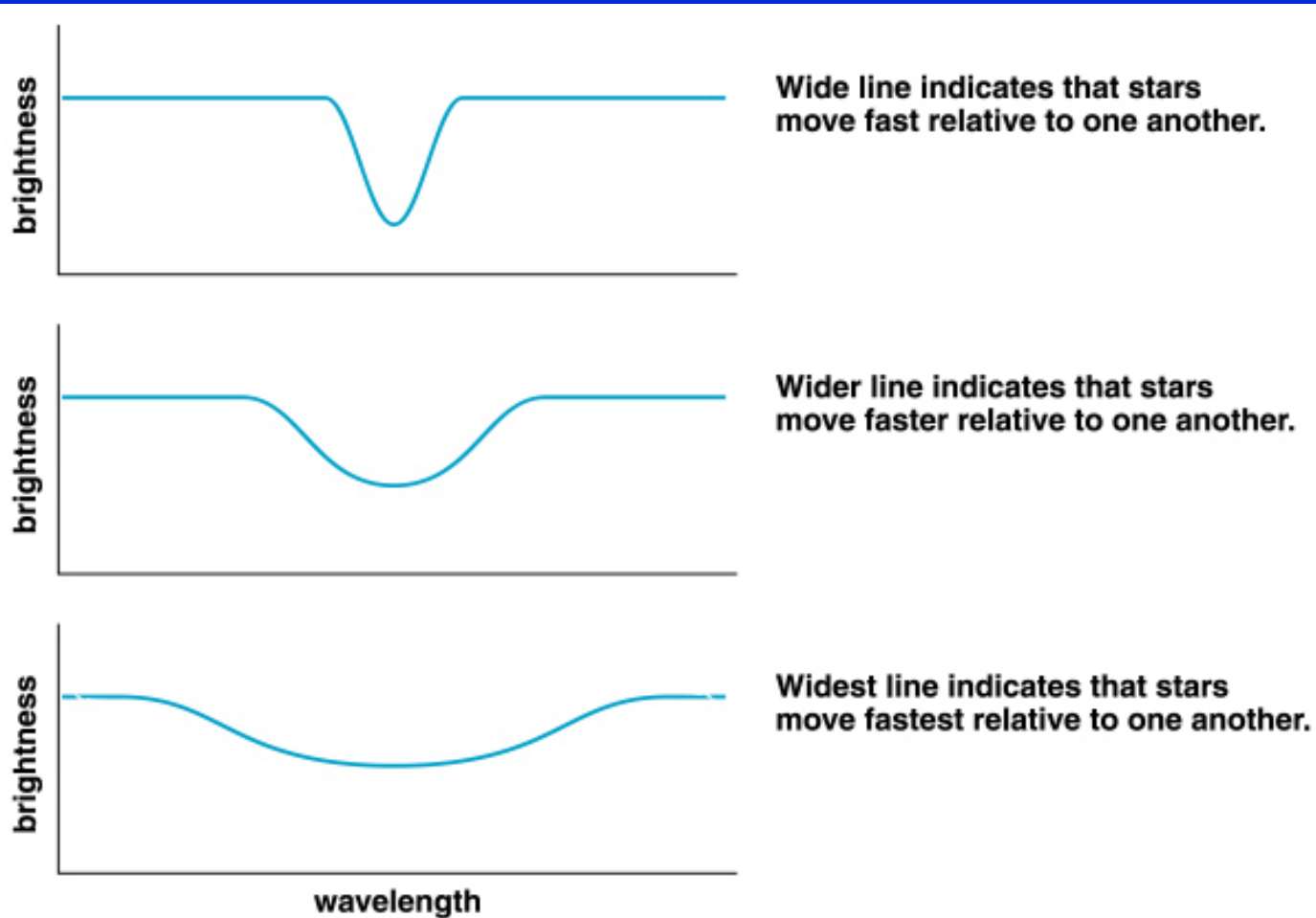


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rotation curves of four typical spiral galaxies



elliptical galaxies: absorption line broadening



mass-to-light ratio

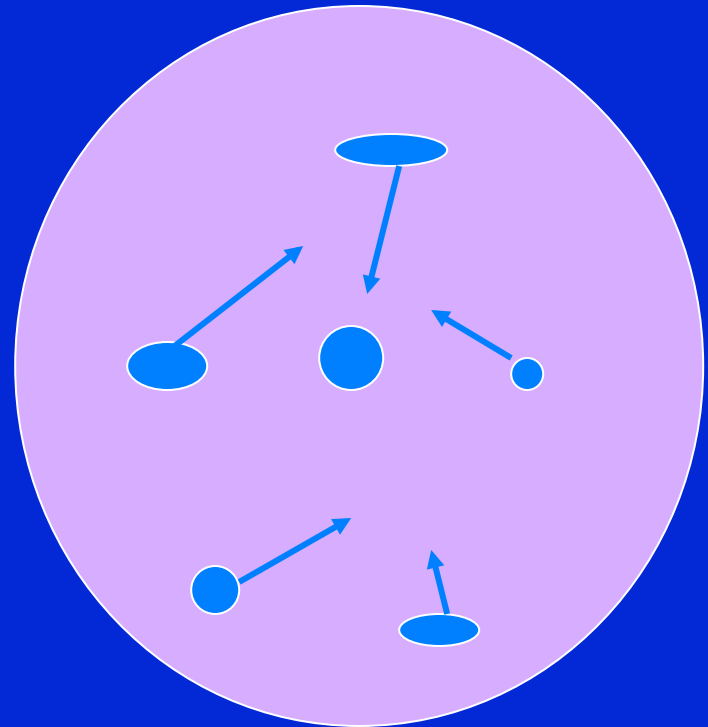
- the mass-to-light ratio is defined as the total mass in solar masses divided by the luminosity in solar luminosities
- for example: the mass of the Milky Way within the Solar radius is about $9 \times 10^{10} M_{\text{sun}}$, and the luminosity is $1.5 \times 10^{10} L_{\text{sun}}$
 - the mass-to-light ratio is $6 M_{\text{sun}}/L_{\text{sun}}$.

mass-to-light ratio depends on radius

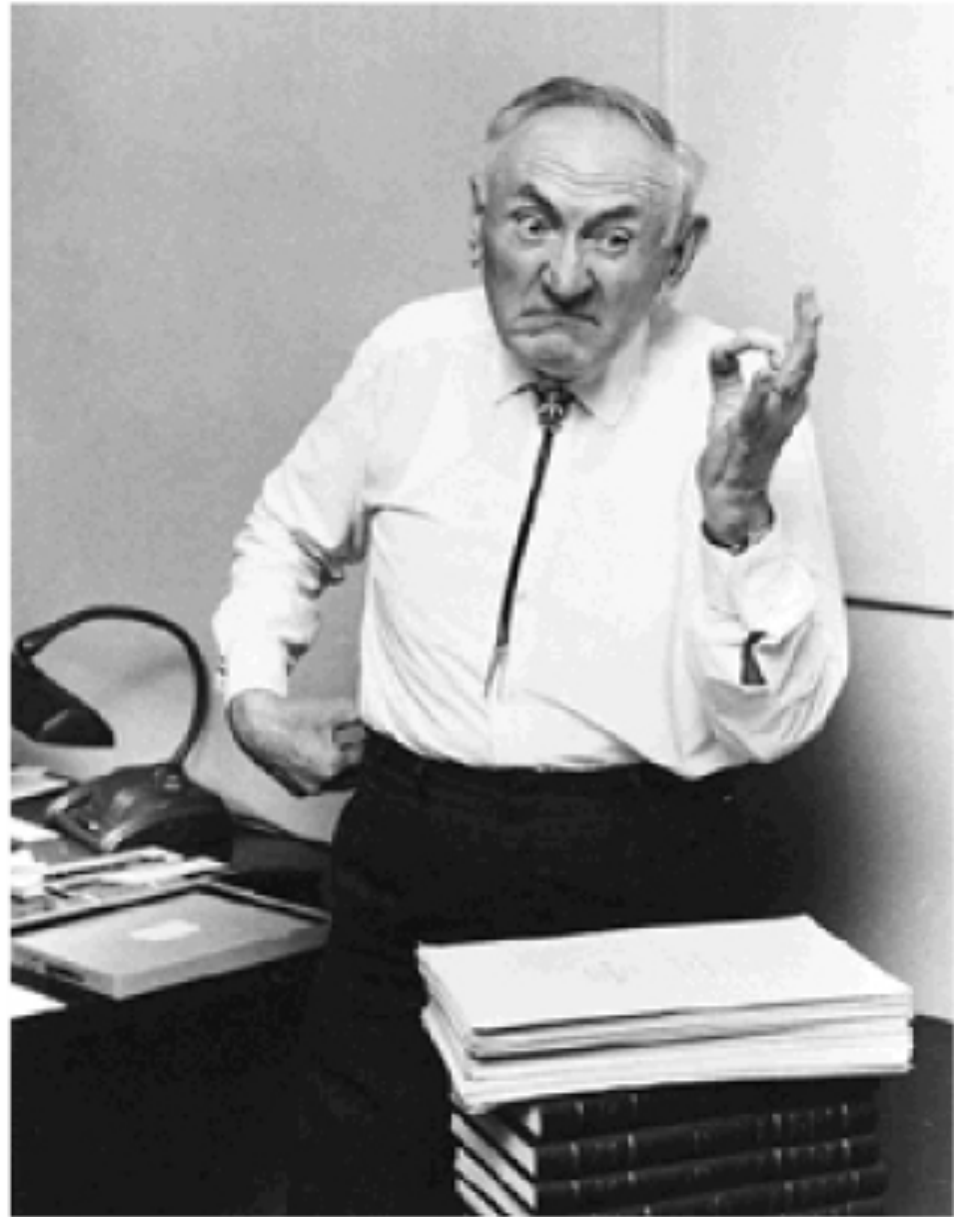
- the motions of satellite galaxies around the Milky Way show that the mass within 100 kpc is about $10^{12} M_{\text{sun}}$.
- the total luminosity within this radius is about $2 \times 10^{10} L_{\text{sun}}$, so the mass-to-light ratio is about $50 M_{\text{sun}}/L_{\text{sun}}$!
- about 90% of the mass within 100 kpc is dark matter.

dark matter in clusters

- we can find the mass of a cluster using the velocities of galaxies relative to the central galaxy

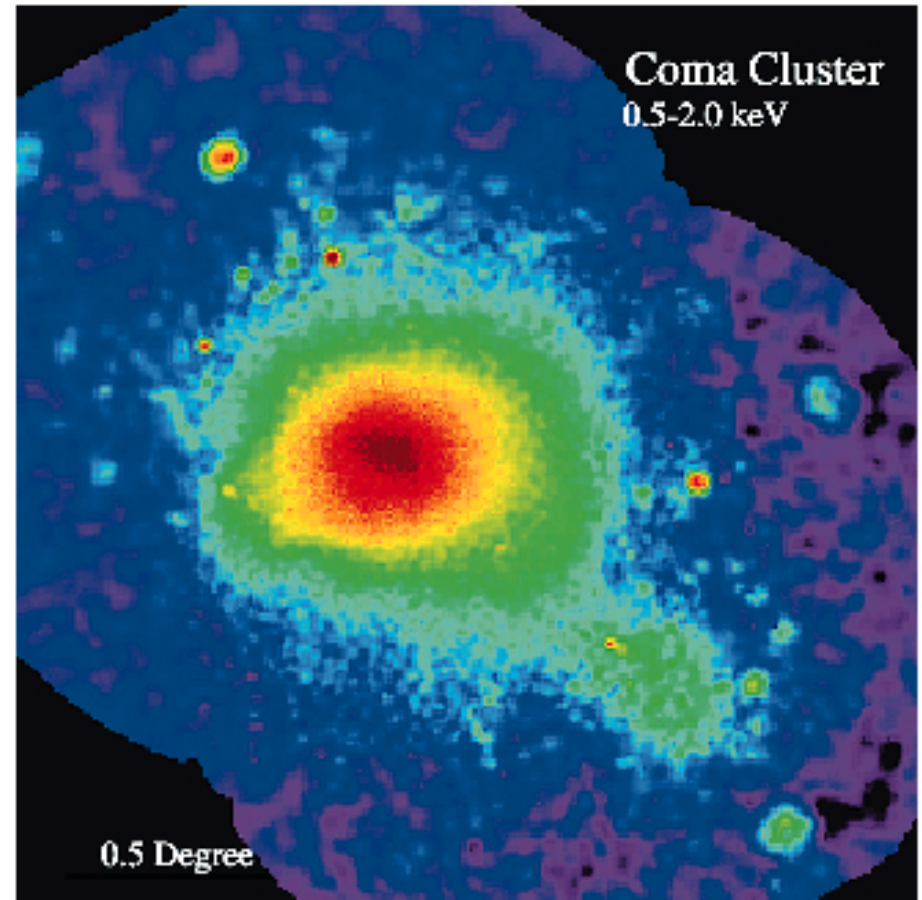


Fritz Zwicky



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clusters are full of hot gas



(a)

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(b)

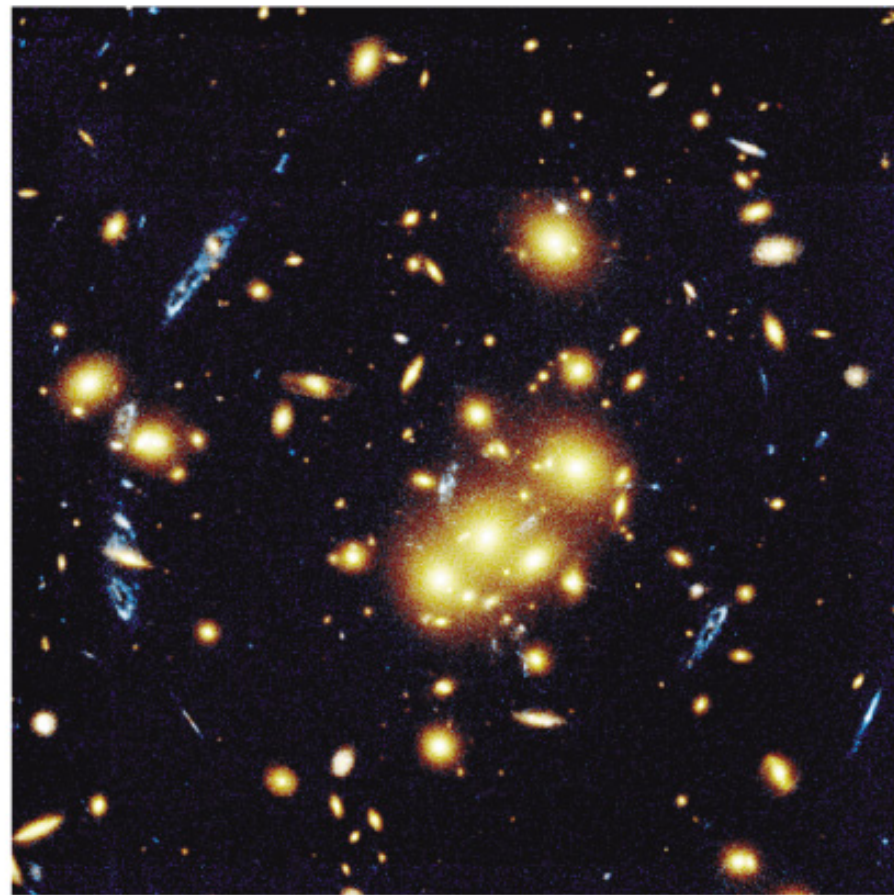
another way to weigh a cluster

- assuming that the hot gas in clusters is in gravitational equilibrium, we can use the *temperature* of the gas to estimate the mass of the cluster
- $v = (0.1 \text{ km/s}) \times (T/\text{Kelvin})^{1/2}$
- then use v in the usual formula
 - $M = (v^2 \times r)/G$

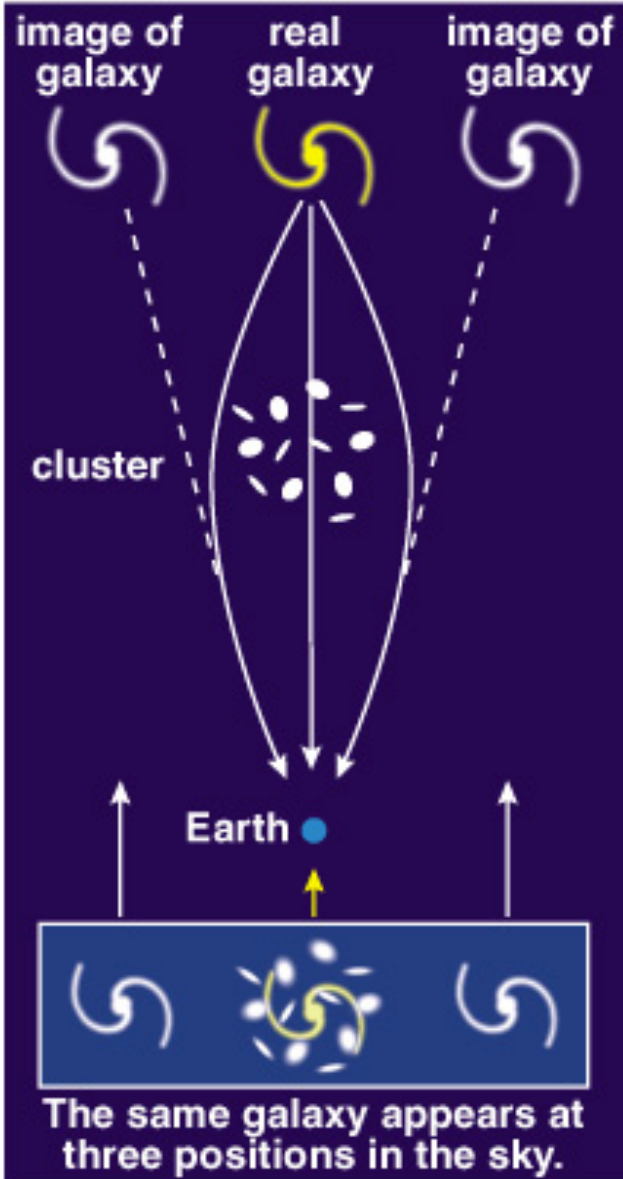
Example: the Coma cluster

The galaxies in the Coma cluster have an average orbital velocity of 1200 km/s within a radius of 1.5 Mpc. The hot gas has an average temperature of 10^8 K. Find the mass of the Coma cluster using both methods. Do they agree?

a third way: gravitational lensing

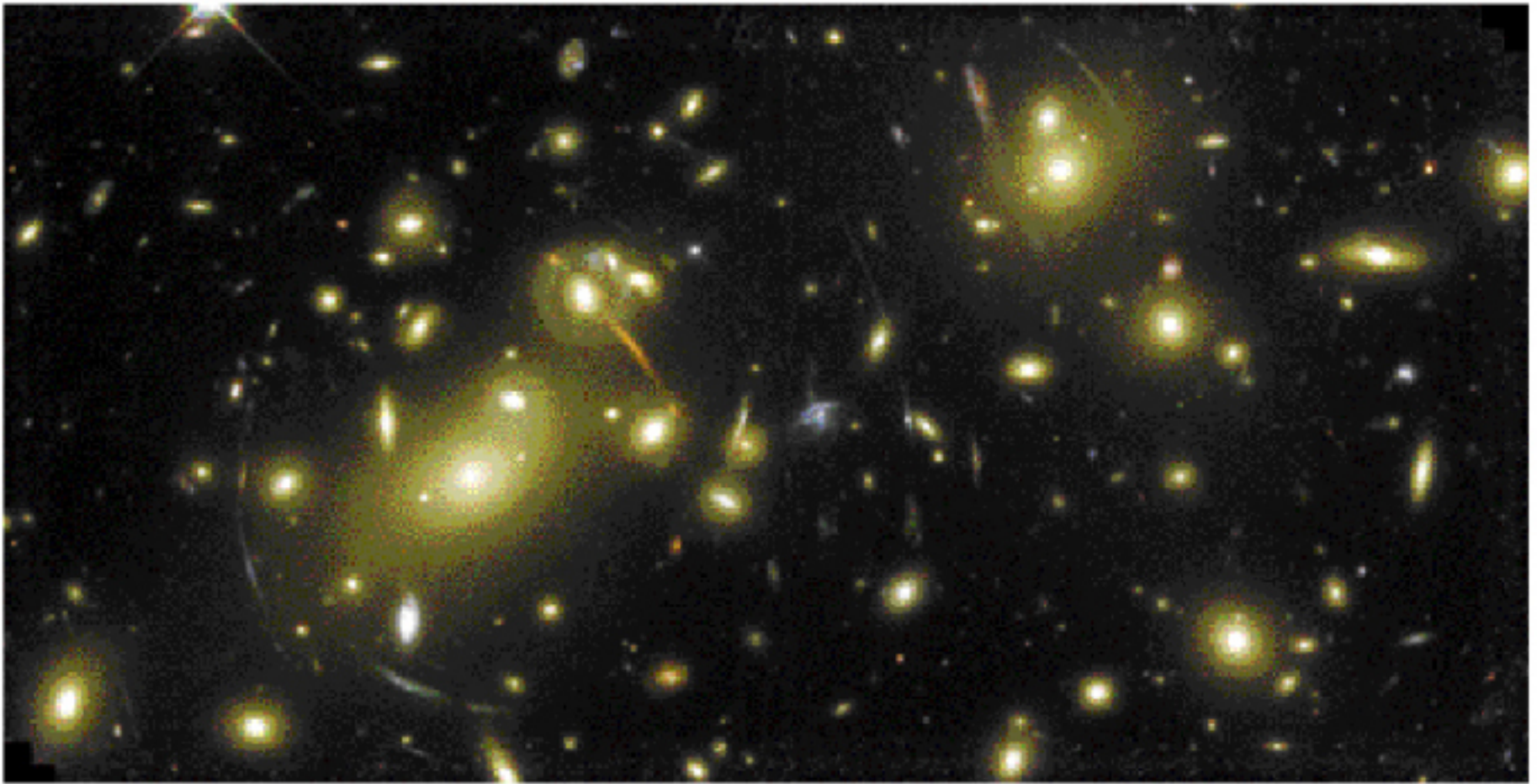


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Abell 2218

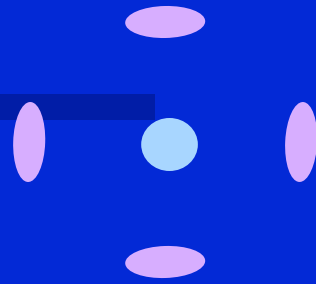
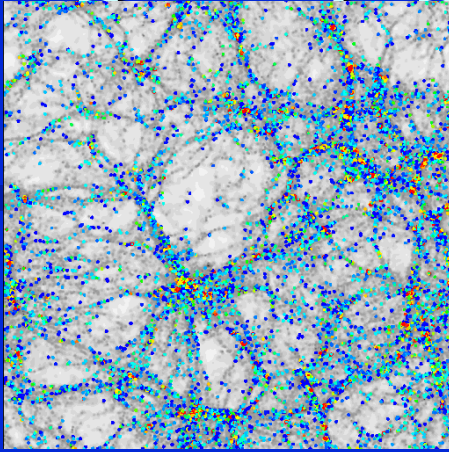


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cluster mass-to-light ratios

- all three methods (galaxy velocities, hot gas temperatures, and gravitational lensing) show that clusters have mass-to-light ratios of 100-500 $M_{\text{sun}}/L_{\text{sun}}$!

galaxy-galaxy lensing



$$R = r_L \Theta$$

$$\gamma_T = \frac{\Delta\Sigma(R)}{\Sigma_{\text{crit}}}$$

$$\Delta\Sigma(R) = \bar{\Sigma}(R) - \Sigma(R)$$

$$\Sigma_{\text{crit}} = \frac{c^2}{4\pi G} \frac{r_S}{(1 + z_L)r_L r_{LS}}$$

- dark matter around galaxies induces tangential distortion of background galaxies: extremely small, 0.1%

- ◆ Useful to have redshifts of foreground galaxies: SDSS Express signal in terms of projected surface density and transverse r

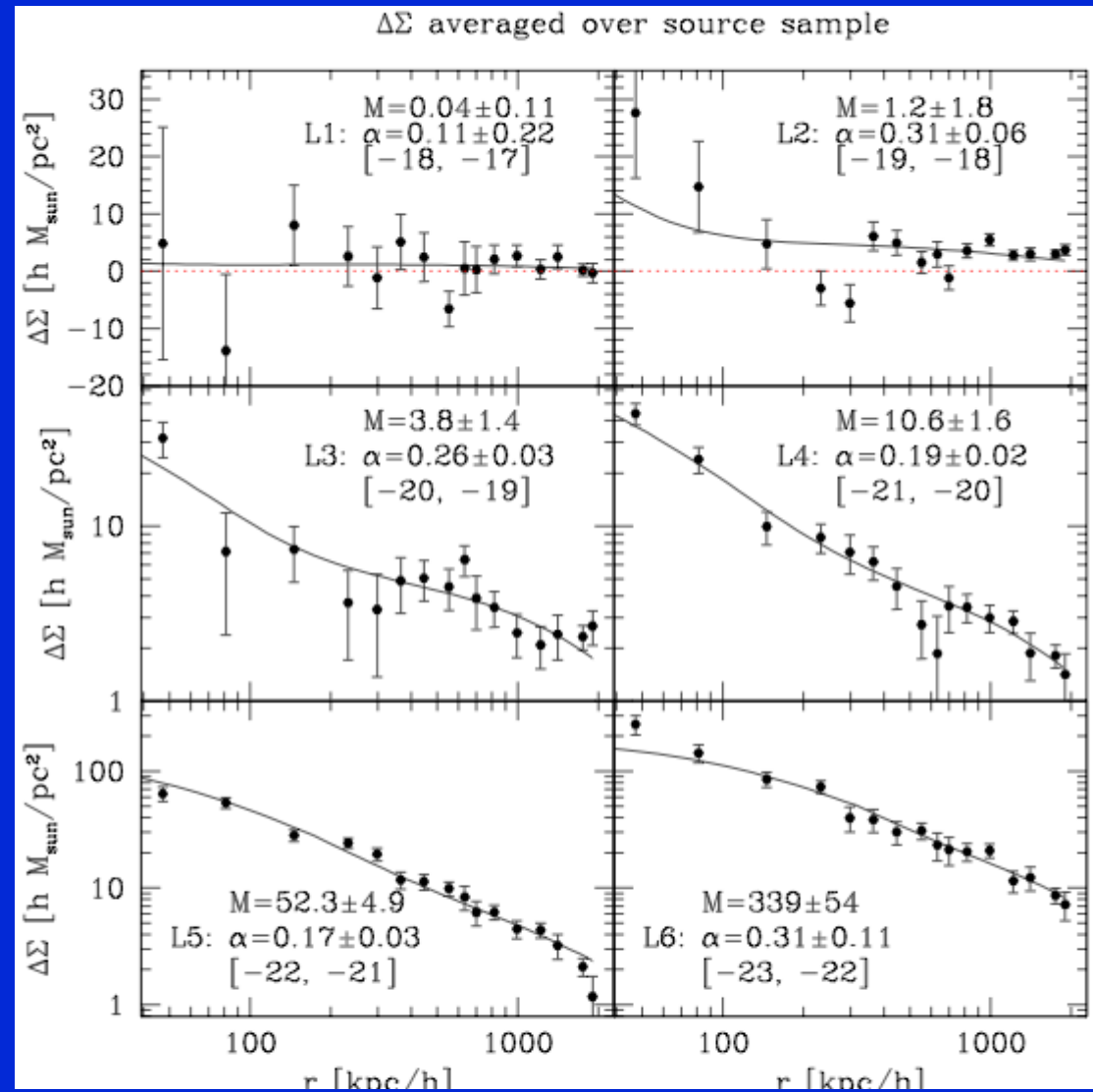
- ◆ Signal as a function of galaxy luminosity, type...

Galaxy-galaxy lensing measures galaxy-dark matter correlations

Goal: lensing determines dark matter masses

Halo mass increases with galaxy luminosity

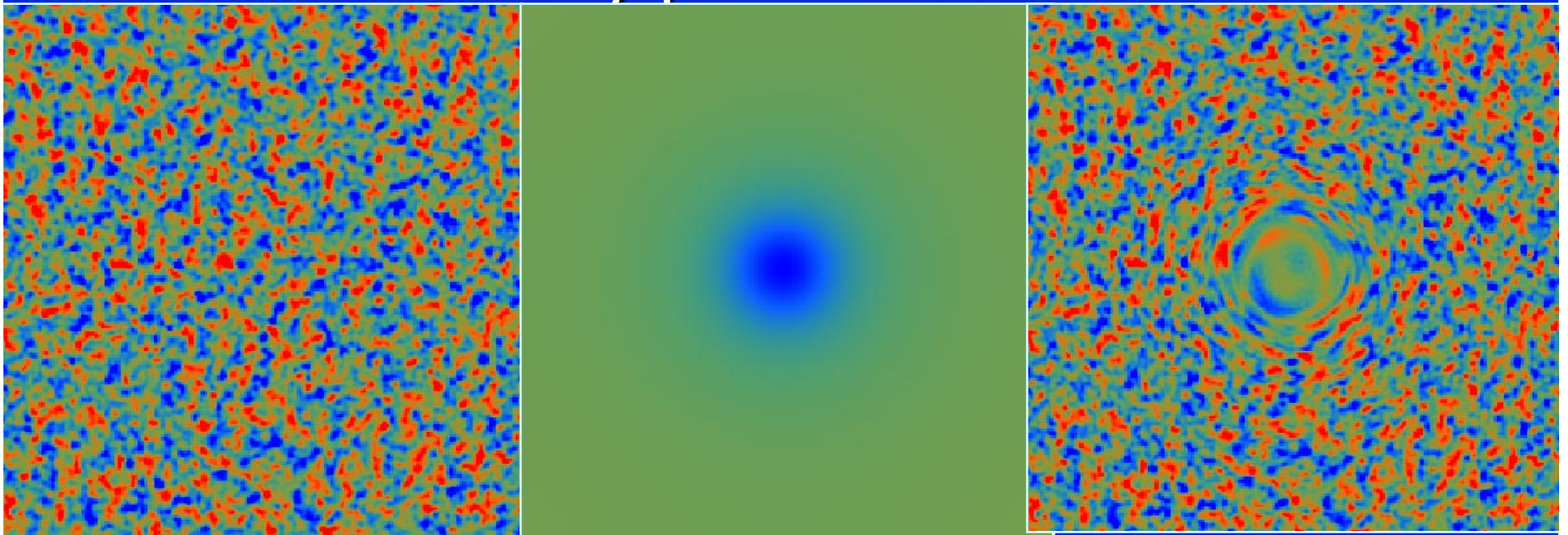
SDSS gg: 300,000 foreground galaxies, 20 million background



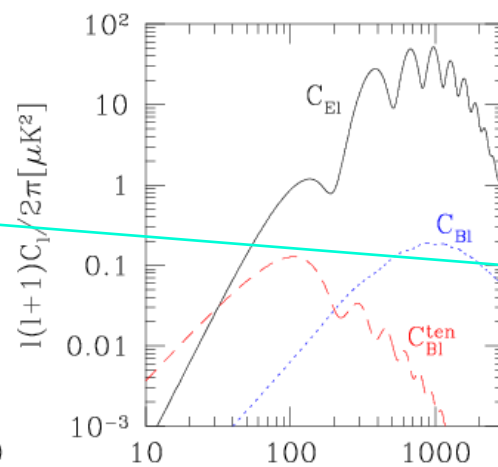
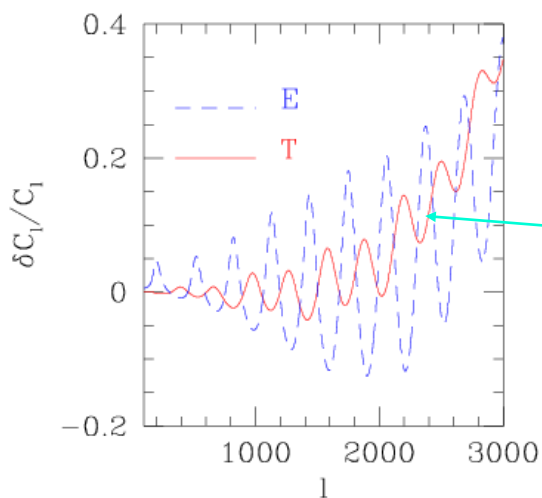
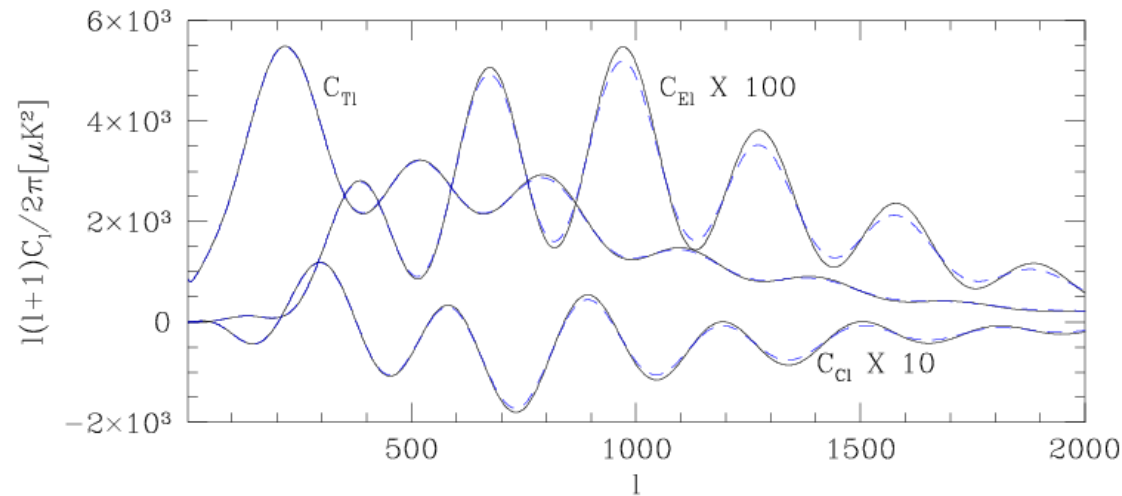
Effect of gravitational lensing on CMB

$$T_{lensed}(\vec{\mathbf{n}}) = T_{unlensed}(\vec{\mathbf{n}} + \vec{\mathbf{d}}) \quad \vec{\mathbf{d}} = -2\vec{\nabla}\nabla^{-2}\kappa$$

- Here κ is the **convergence** and is a projection of the matter density perturbation.



Lensing effect on CMB power spectra

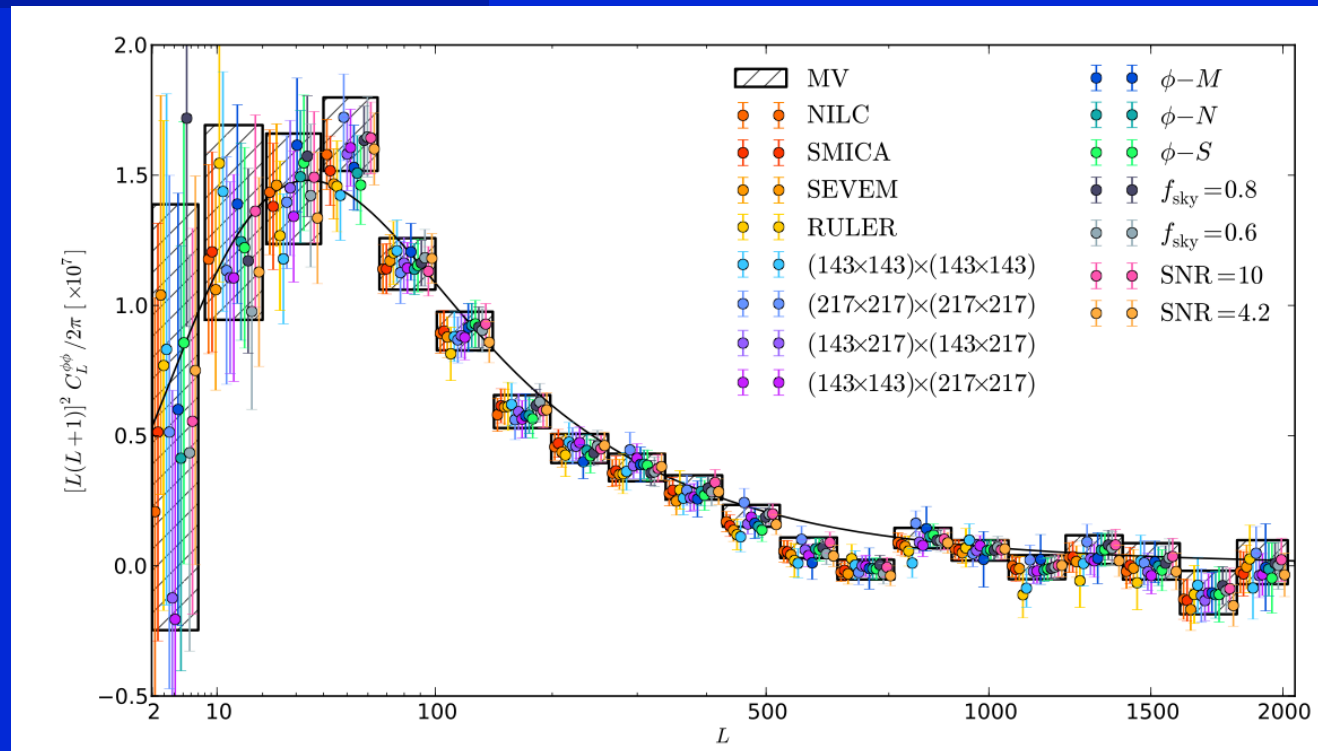


Smoothing and
power transfer

Detected by several sigma in
Planck

State of the art in CMB lensing: Planck

40 sigma in Planck 2015



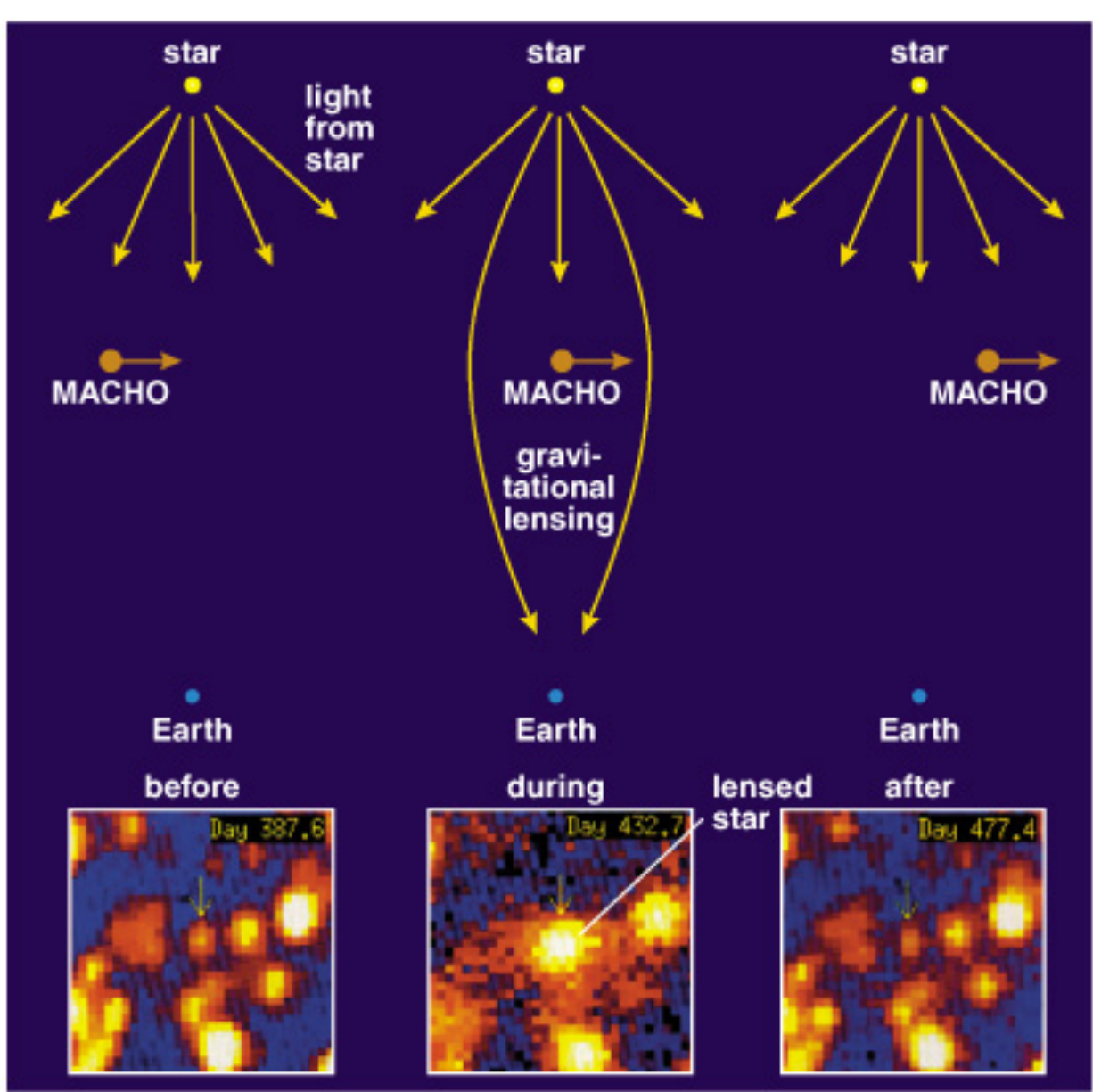
Future CMB experiments (stage 3 and 4): 200+ sigma

dark matter: what is it?

- there are two basic possibilities:
 1. *baryonic dark matter* – ‘ordinary matter’ (i.e. protons, neutrons, electrons, etc.) perhaps faint stars, brown dwarfs, planets, gas?
 2. *non-baryonic dark matter* – a new kind of particle that we have never seen directly

the search for MACHOs

- perhaps the dark “halo” of our Galaxy is made up of normal material (like faint stars or brown dwarfs)
- these are called Massive Compact Halo Objects (MACHOs).
- they might be detected by *microlensing*
- *Microlensing has been detected, but likely originates from faint stars (and a few planets)*



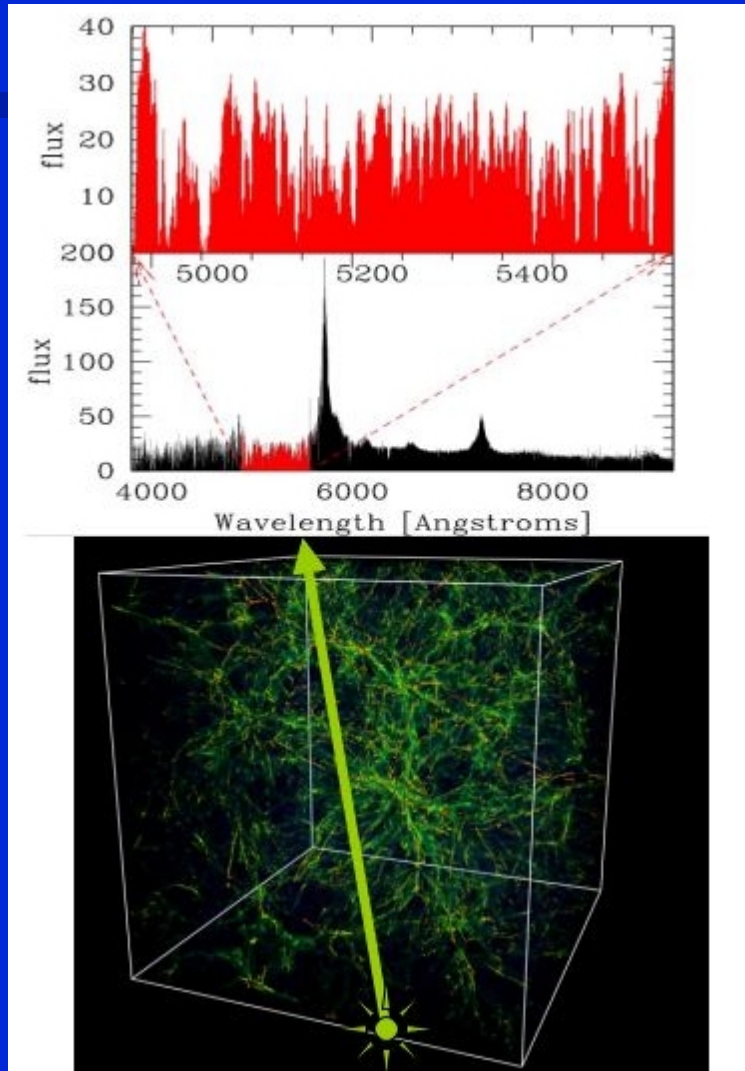
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Hot, warm and cold dark matter

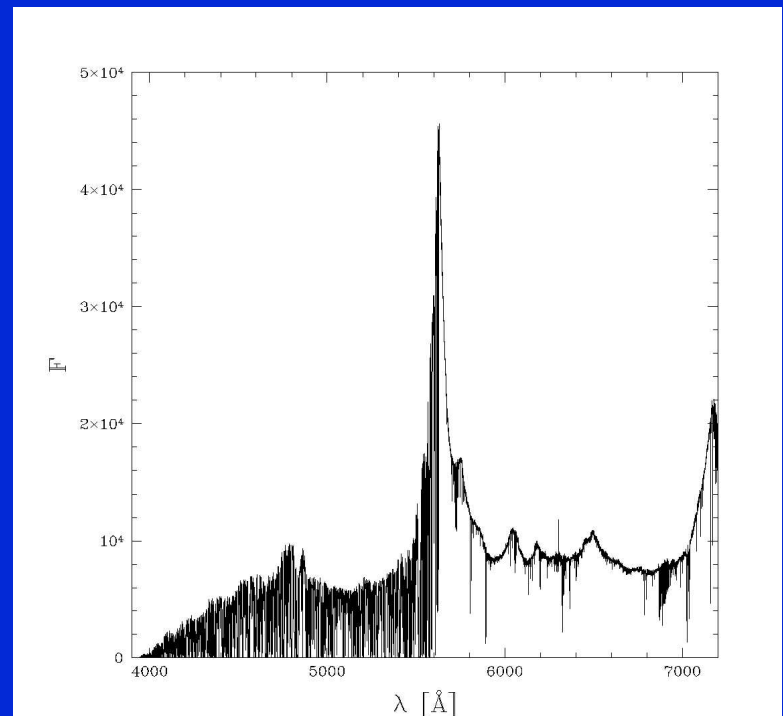
- *hot* dark matter is made of particles that move very close to the speed of light (such as neutrinos)
- *cold* dark matter is made of particles that move much slower than the speed of light
- we now think most of the dark matter must be cold or warm

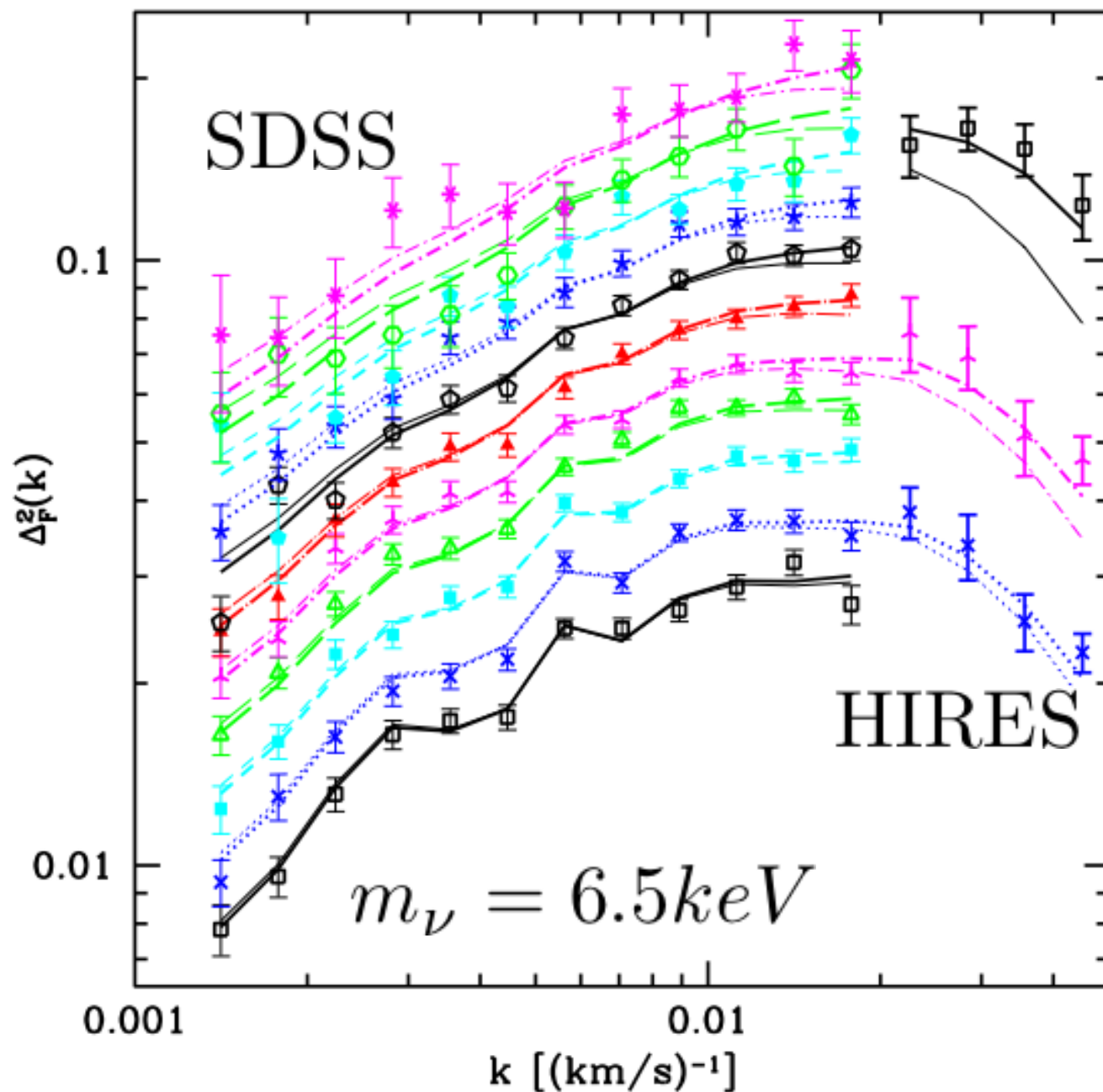
Ly-alpha forest: basics

- Neutral hydrogen leads to Lyman- α absorption at $\lambda < 1216 (1+z_q) \text{ \AA}$; it traces baryons, which in turn trace dark matter



SDSS Quasar Spectrum





WDM is a worse fit to the data

Neoclassical tests

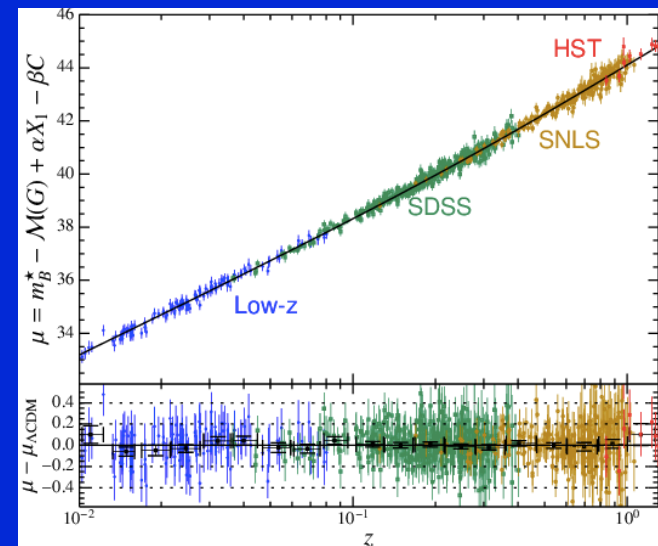
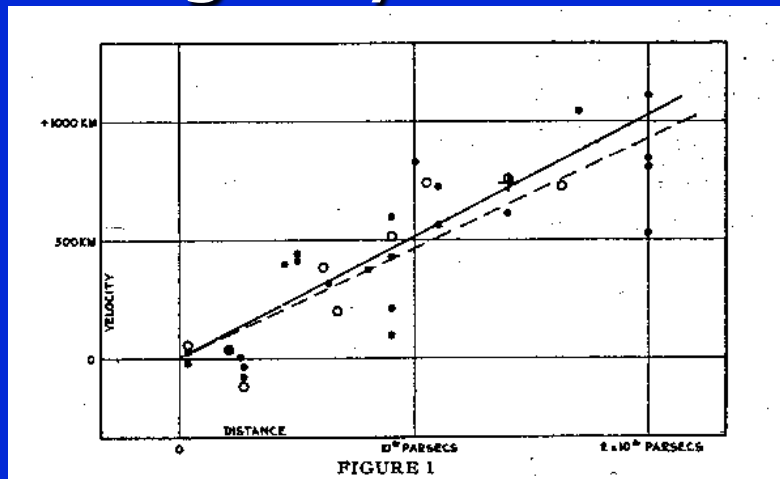
- We wish to test Friedmann equation:

$$\left(\frac{\dot{a}}{a}\right)^2 = H^2 = \frac{8}{3}\pi G\bar{\rho} - K a^{-2}$$

$$D_C(z) = \frac{c}{H_0} \int_0^z dz' \frac{H_0}{H(z')}$$

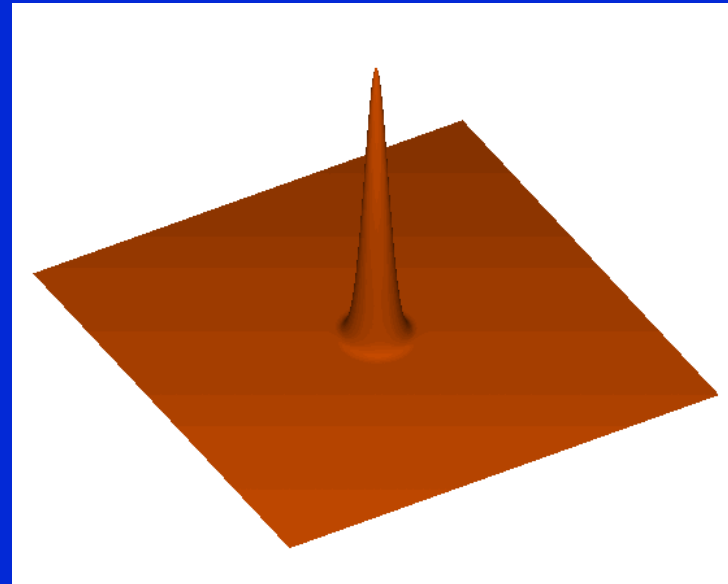
$$\bar{\rho} = \rho_m a^{-3} + \rho_{de} a^{-3(1+w)} + \rho_\gamma a^{-4} + \rho_\nu F(a)$$

- Redshift-distance relation has come a long way since the days of Hubble



Baryonic Acoustic Oscillations

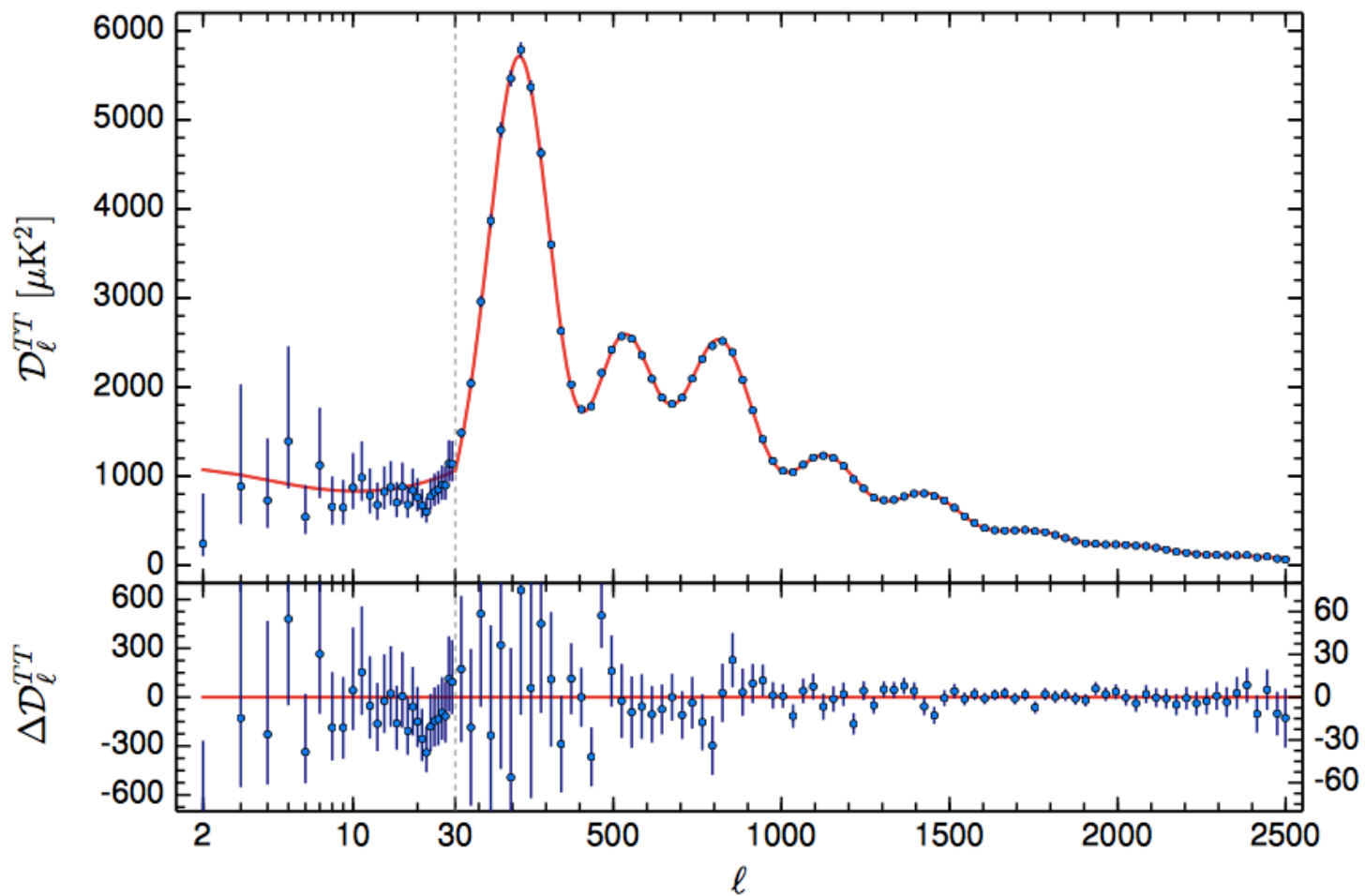
- Each initial overdensity (in DM & gas) is an overpressure that launches a spherical sound wave.
- This wave travels outwards at 57% of the speed of light.
- Pressure-providing photons decouple at recombination. CMB travels to us from these spheres.
- Sound speed plummets. Wave stalls at a radius of 147 Mpc.
- Seen in CMB as acoustic peaks
- Overdensity in shell (gas) and in the original center (DM) both seed the formation of galaxies. Preferred separation of 147 Mpc.



Sound horizon at drag epoch (from Planck) : $r_d = 147.49 \pm 0.59$ Mpc

$$r_d = \int_{z_d}^{\infty} \frac{c_s(z)}{H(z)} dz \quad c_s(z) = 3^{-1/2} c \left[1 + \frac{3}{4} \rho_b(z) / \rho_\gamma(z) \right]^{-1/2}$$

Planck: state of the art in CMB



A Standard Ruler

- The acoustic oscillation scale depends on the matter-to-radiation ratio ($\Omega_m h^2$) and the baryon-to-photon ratio ($\Omega_b h^2$)

$$r_d \approx \frac{56.067 \exp[-49.7(\omega_\nu + 0.002)^2]}{\omega_{cb}^{0.2436} \omega_b^{0.128876} [1 + (N_{\text{eff}} - 3.046)/30.60]} \text{ Mpc}$$

- The CMB anisotropies measure these and fix the oscillation scale to $<1\%$.
- In a redshift survey, we can measure this along and across the line of sight:
 - BAO along los
 - BAO tranverse
- Yields $H(z)$ and $D_M(z)$

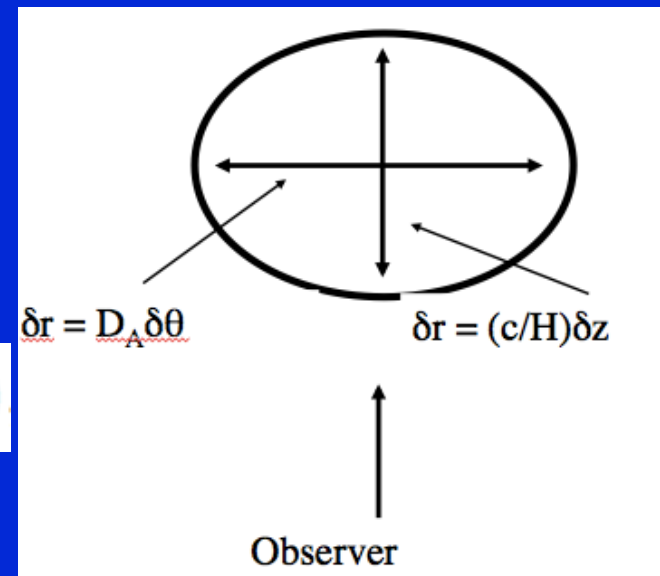
$$\Delta v_{BAO} = \frac{r_d}{1+z} H(z)$$

$$\Delta \theta_{BAO} = \frac{r_d}{1+z} \frac{1}{D_A(z)}$$

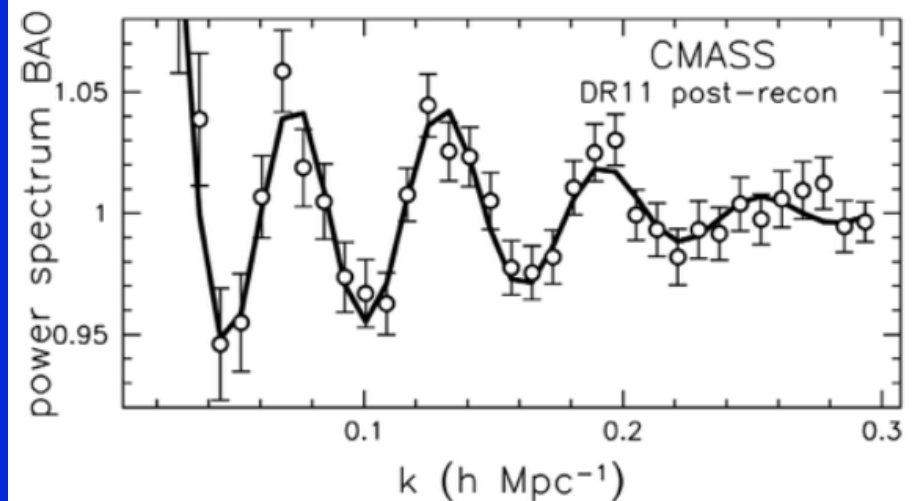
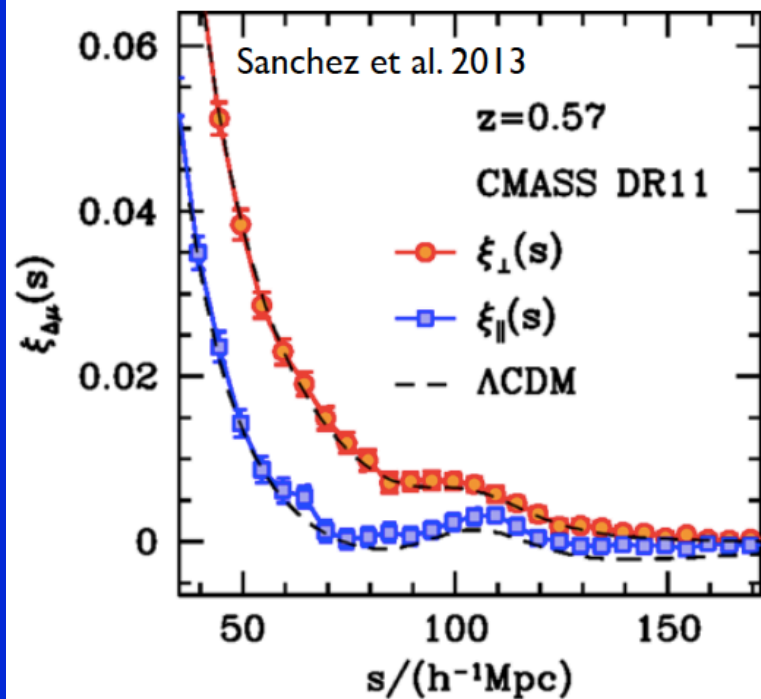
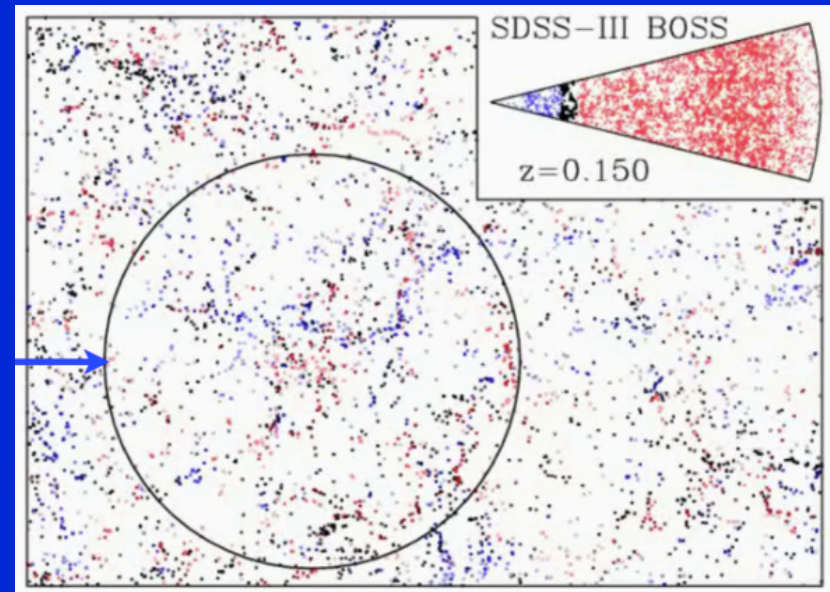
$$D_M(z) = \frac{c}{H_0} S_k \left(\frac{D_C(z)}{c/H_0} \right)$$

$$D_H(z) = c/H(z)$$

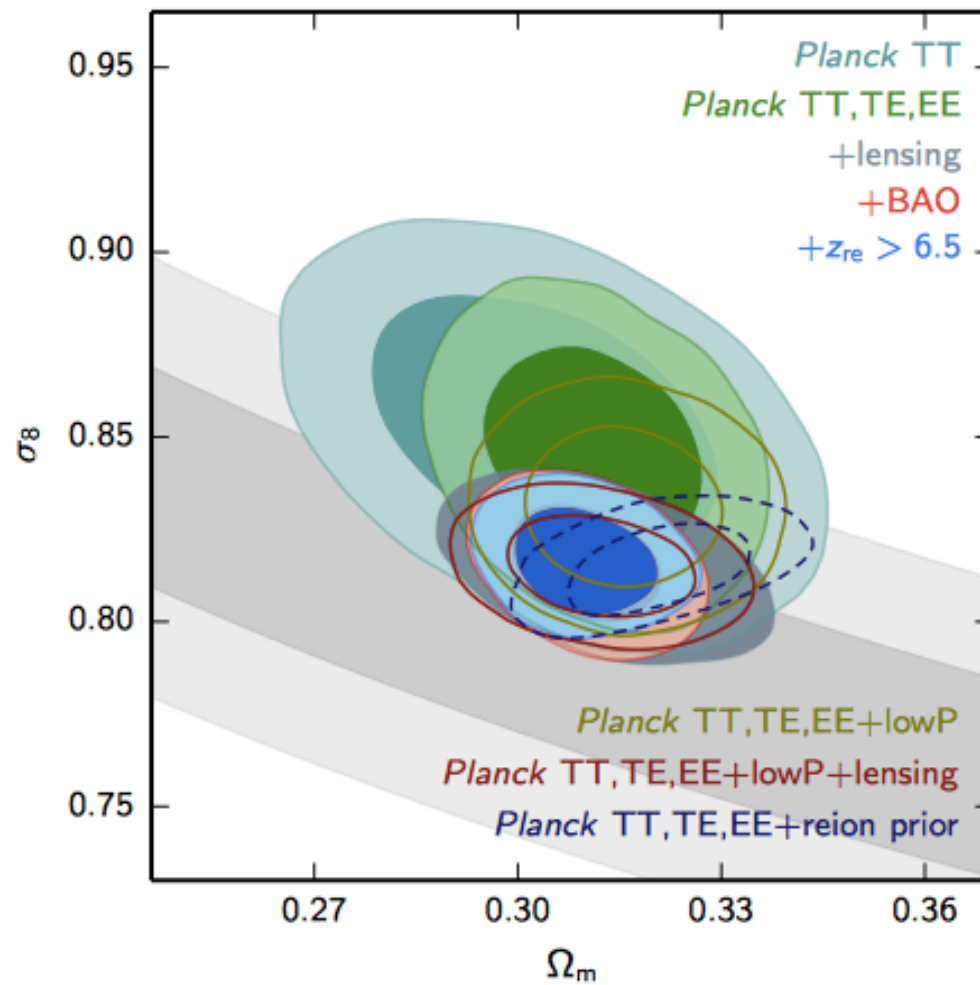
$$D_V(z) = [z D_H(z) D_M^2(z)]^{1/3}$$



Hunting for BAO in BOSS: correlation function and power spectrum

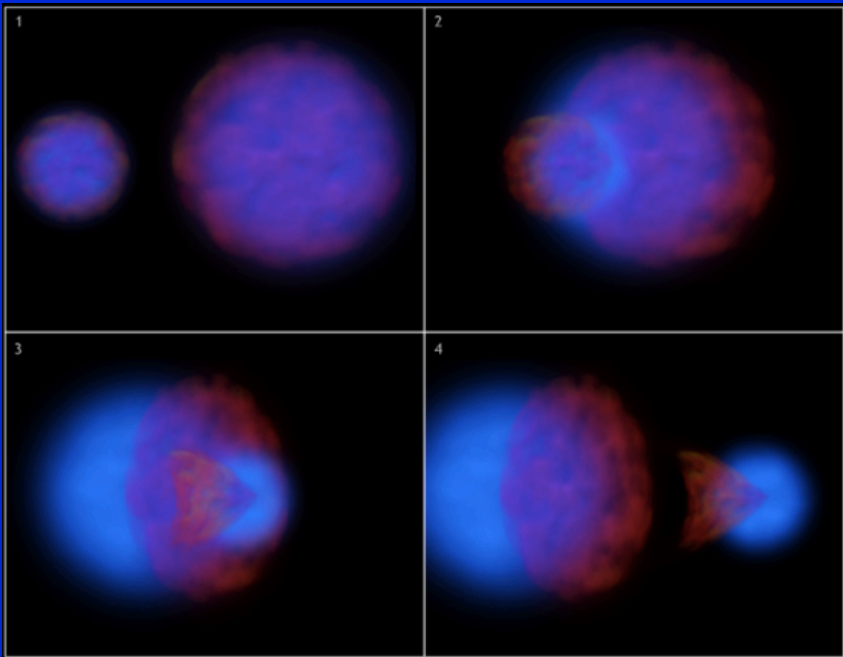


CMB+lensing+BAO



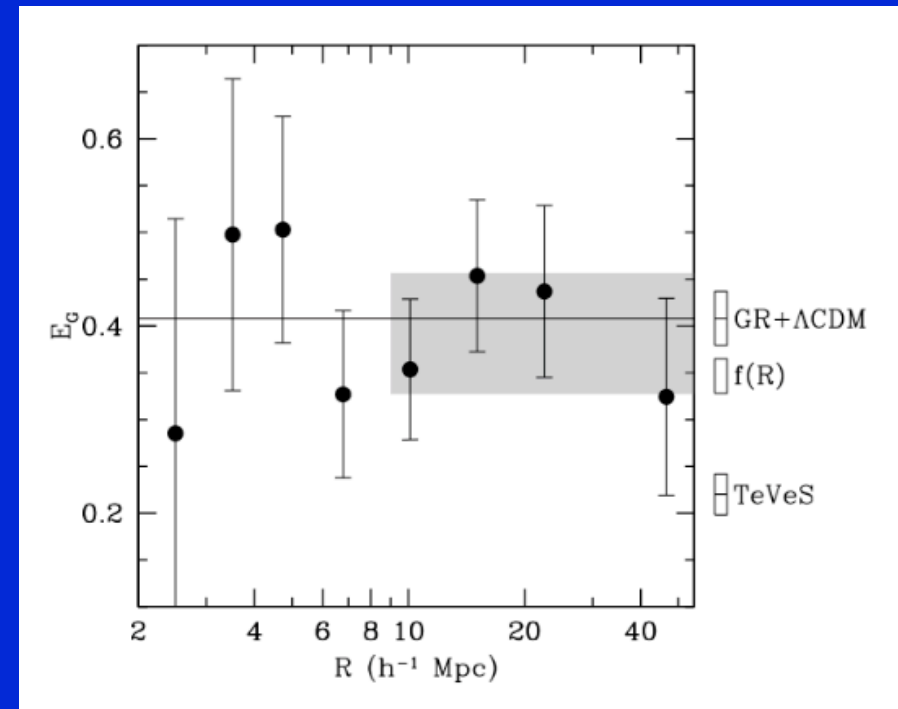
Alternatives? MOND

- Bullet cluster argues against MOND



Alternatives: TeVeS

- Lensing versus velocities modified in these models versus GR



Conclusions

- The case for dark matter is overwhelming
- It consists of 25% of critical density
- Data point to cold, non-interacting
- Possible topics: dark matter physics in CMB, LSS, self-interacting dark matter, warm dark matter, massive neutrinos as dark matter...